Title: A unified theoretical approach for biological cognition and learning

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Abstract (100-120 words)

Large-scale neural models are needed in order to understand the biological underpinnings of complex cognitive behavior. Good methods for constructing such models should provide for: 1) abstraction (analysis across levels of description); 2) integration (incorporation of simpler models to build more complex ones); 3) empirical contact (using and comparing to a wide variety of neural data); and 4) account for the varieties of learning. In this review we evaluate three prominent recent methods for constructing neural models using these four criteria. Each of these methods is being actively developed and demonstrates clear strengths along some of these criteria.

Introduction

There is general agreement that the vast majority of natural behavior is the result of the interactions between many brain areas, implicating huge numbers of neurons. Without constructing biologically detailed models that explore these complex interactions, we are unlikely to be able to understand how to help a distressed brain (Just et al., 2012), or explain how low-level biological mechanisms give rise to cognitive behavior (Beeler et al., 2012; Tyrcha et al., 2013). In short, without large-scale models, we cannot test large-scale hypotheses.

To understand biological cognition -- i.e., the link between biological mechanisms and cognitive behavior -- we need to understand the complex interactions between individual neurons as well as their integration into a behaving, cognitive agent. This is a challenging and long-term goal, but it is nevertheless helpful to consider contemporary theoretical approaches in this context to determine promising avenues for research. Addressing cognitive behaviors in a neural model typically requires a large-scale model: one simulating tens of thousands to several million neurons. This is due to the correlation between the complexity in a task and its likelihood of being deemed ‘cognitive.’ Complexity suggests that large numbers of neural resources, and often many different brain areas, are required to address the challenge embodied by the task.

Large-scale neural models are ineluctably complex. Consequently, in order for us to successfully understand and construct them, it is critical to employ systematic methods. Ideally, good methods would provide (Eliasmith & Trujillo, 2014; Eliasmith, 2013): 1) smoothly moving between levels of detail depending on questions of interest (*Abstraction*); 2) easy integration of simpler partial models (*Integration*); 3) generation of empirical predictions while providing

deeper insight into collected neural and behavioral data (*Empirical contact*) and 4) methods for including adaptation and learning (*Learning*). We review recent work at the interface of biological and behavioral modeling along these four criteria. Specifically, we focus on methods from Denève et al., efficiently implementing dynamical systems in spiking neurons (Boerlin et al., 2013), large-scale neural models proposed by Markram et al. (Markram et al., 2015), and our own work (Eliasmith, 2013).

Dynamics in spiking networks

1) *Abstraction*

Sophie Denève and her collaborators have recently developed and explored a method for constructing spiking neuron implementations of dynamical systems (Boerlin et al., 2013; Zeldenrust et al., 2013; Schwemmer et al., 2015). These researchers have shown the method can be used to build robust models of neural integrators, simple arm controllers, and optimal linear filters (e.g. the Kalman filter). Consequently, they have defined an effective means of abstracting from spiking neural networks to linear dynamical systems.

This method consists of treating subthreshold voltages of individual cells as tracking the error in the estimate of an underlying multi-dimensional state variable. When the error becomes large, a neuron in a given population representing that state variable emits a spike, updating the representation of that state. In order to ensure that neurons are efficient in their representation of such states, when a given cell spikes, it instantaneously inhibits other neurons in the population from spiking to account for that same error. Consequently, these networks can be used to represent dynamical systems defined over the represented state variables. In addition, these methods are unique in providing a clear relation to predictive coding.

These methods have been noted to have several limitations. Chief amongst these is that they apply only to linear dynamical systems. However, recent work has suggested methods for incorporating nonlinearities via dendritic computation in such networks (Thalmeier et al., 2015). It is not clear, however, if these methods will scale (Eliasmith & Anderson, 2003, p. 156). In addition, the speed of inhibition may not be biologically plausible. As well, the work has been criticized as applying to simple point neuron integrate-and-fire models only. However, it has recently been demonstrated that similar methods can be applied to sophisticated conductance based neuronal models (Schwemmer et al., 2015).

Given that the characterization of function is in terms of a state space, and that conductance models can be used, these methods provide multiple levels of abstraction. However, the methods do not yet provide abstractions for relating neural-level circuits to sophisticated, cognitive behaviour.

2) *Integration*

Integration of simpler models should be possible with this approach because of the employed state space representations. However, there are not yet clear examples of performing such an integration. Possible barriers to integration include assumptions about the nature of inhibition and excitation included in the methods, which do not apply to subcortical areas, such as basal ganglia and cerebellum. For instance, basal ganglia consists largely of inhibitory projections, while these methods assume both excitatory and inhibitory interactions are available between all neurons in the circuit.

3) *Empirical contact*

These networks exhibit several desirable traits (Boerlin et al., 2013). For instance, they naturally exhibit Poisson-like firing variability at the level of individual spike trains. As well, they are consistent with the observation that many biological circuits balance the effects of inhibition and excitation. In addition, they are highly efficient in their use of spikes and are robust to neuronal death and other perturbations. They have been shown to efficiently implement behaviorally relevant dynamical systems including integrators, oscillators, and simple arm controllers (Boerlin et al., 2013). However, there is also evidence that some networks, like those of the oculomotor integrator, do not exhibit the kind of spike train variability expected under this characterization of neural computation (Aksay, et al., 2003).

4) *Learning*

Very recently, Bourdoukan and Denève (2015) have begun to explore methods for learning connection weights in these kinds of networks. They have shown that with different local learning rules for fast and slow recurrent connections, it is possible to feedback a global supervised error signal that can tune the network.

Blue Brain Project

1) *Abstraction*

In contrast to Denève's theoretically driven approach, recent work from Henry Markram's lab has focussed on building large-scale brain models with significant biological detail. In short, the approach taken by the Blue Brain Project (Markram, 2006) and now incorporated into the Human Brain Project (HBP; Markram et al., 2012) is to build models from the bottom up, with the expectation that interesting behavioral features will emerge. This work has recently culminated with the release of a paper with 82 co-authors that describes a detailed model of a small section of rodent somatosensory cortex (Markram et al., 2015). This model includes about 31,000 cells and 37 million synapses amongst 207 different kinds of neurons.

This approach to modelling does not bear any clear relation to abstractions of neural computation. Consequently, the model is largely used to replicate low-level experimental data that does bear a clear relation to observable behavior. While addressing such data is clearly important, the approach taken does not permit developing a theory of how neural activity relates to the behavior it controls.

2) *Integration*

In the context of this project, integration is largely focussed on methods for combining individual neuron models. Connections between neurons were determined using five rules of connectivity that provide an effective means of filling in statistically matched anatomical connections between neuron types. This permits the anatomical combination of single cell models, addressing the integration of simpler neuron models into larger circuits. However, this kind of integration does not extend to functional or behaviourally relevant networks, as such networks have not been built with these methods.

3) *Empirical contact*

These methods have very extensive empirical contact with neural data since a significant amount of the modelling effort has gone into inferring parametric information based on available neural

data. There is good evidence that the rules of connectivity used in the model, along with other parameter fitting methods, are successful for generating statistically similar activity in the circuit compared to *in vivo* recordings. As well, the rules of connectivity were used to generate predictions regarding the number of connections and number of synapses per connection, as well as a wide variety of other connectivity and physiological properties of synapses.

At the circuit level, the model was used to examine the spatio-temporal patterns that result from simulated thalamic input in combination with variations in calcium levels. The model demonstrated that different levels of calcium resulted in synchronous and asynchronous neural firing in the model, in agreement with experimental results. However, it is not clear how these methods will permit relating such local activity to observable behavior.

Nevertheless, the models provided are currently unsurpassed in the amount of molecular detail provided compared to other work, providing strong empirical contact with certain areas of neuroscience.

4) *Learning*

While it should be possible to introduce neurally plausible connection strength adaptation into such a model, it is not clear how such learning rules would affect the behavior of the circuit. This aspect of neural function is unexplored with these methods at present.

Figure 1: Semantic Pointer Architecture Unified Network (Spaun). a) The neuroanatomical architecture of Spaun. Abbreviations: V1/V2/V4 (primary/secondary/extrastriate visual cortex), AIT/IT (anterior/inferotemporal cortex), DLPFC/VLPFC/OFC (dorso-lateral/ventro-lateral/orbito- frontal cortex), PPC (posterior parietal cortex), M1 (primary motor cortex), SMA (supplementary motor area), PM (premotor cortex), v/Str (ventral/striatum), STN (subthalamic nucleus), GPe/i (globus pallidus externus/internus), SNc/r (substantia nigra pars compacta/reticulata), VTA (ventral tegmental area). (b) Replacement of leaky integrate-and-fire neurons with compartmental conductance neurons in the OFC. This replacement was used to simulate the effects of TTX on cognitive behavior. (c) Input to the model is through images shown to a simulated eye. Behavioral output of the model is in the form of moving a simulated arm with muscles. Modified from Eliasmith (2013).

The NEF and the SPA

1) Abstraction

The Neural Engineering Framework (NEF) identifies three quantitatively specified principles that can be used to implement nonlinear dynamical systems in a spiking neural substrate

(Eliasmith & Anderson, 2003). Specifically, these principles provide methods for characterizing representation, computation, and dynamics in such networks. Consequently, given a hypothesis about what dynamical system a brain area might be implementing, the NEF can be used to build a spiking neural network that approximates that dynamical system. For instance, we might characterize working memory as a dynamical system that loads in a 2-dimensional representation during stimulus presentation and is stable during a delay period (Singh & Eliasmith, 2005). The NEF can then be used to efficiently build a network that will approximate those dynamics with spiking neurons, and allow careful and direct comparison to biological neural networks thought to underlie the same behaviour. These methods have been used to propose novel models of a wide variety of neural systems (Bekolay et al., 2014; Stewart et al., 2012; Trujillo et al., 2014) as well as to better understand more general issues about neural function (Tripp and Eliasmith, 2007; Parisien et al., 2008).

The NEF answers questions about *how* neural systems might compute, but it does not address the issue of *what*, specifically, is computed by biological brains. We have recently addressed this second question by proposing a general neural architecture that includes specific functional hypotheses. We call this proposal the Semantic Pointer Architecture (SPA; Eliasmith, 2013). The SPA identifies a generic means of characterizing neural representations, “semantic pointers,” that are used to capture central features of perceptual, motor, and cognitive representation. Briefly, semantic pointers are neural representations of information compressed via lossy operators. The specific operator hypothesized to be used in a neural system can vary: e.g. an image specific statistical operator in visual systems, a dimensionality reduced path planner in motor systems, or a compressive binding operator for representing cognitive structure. These representations are called ‘pointers’ because they are efficient, low-dimensional (because compressed) representations of what they point to (i.e., the uncompressed information from which they were generated). They are ‘semantic’ because the contents of the pointer (unlike a typical computer pointer) are determined by the contents of what they point to. The SPA uses semantic pointers to explain, among other things, perceptual categorization, motor control, working and long-term memory, as well as conceptual binding and structure representation. Furthermore, the SPA includes an account of cognitive control that relies on basal ganglia and thalamic interactions with cortex for understanding action selection.

The NEF/SPA approach describes brain circuits at various levels of cognitive and neural detail. The neural simulation environment Nengo incorporates these methods, allowing the simulation of different parts of the same model at different levels of detail, including: direct solution of the dynamical system; rate neurons; or as any of many spiking point neuron models (Bekolay et al., 2013). Tripp (2015) proposed the use of surrogate population models to accelerate large-scale neural system modelling in Nengo, adding a level of simulation abstraction between neurons and the direct dynamical system solution.

Furthermore, Nengo was recently used in tandem with the NEURON simulator (Hines and Carnevale, 1997) to replace simple point neurons in the Spaun model (Figure 1; see next section) with complex conductance models (Eliasmith, et al., 2016), of the type used in the HBP models. These neurons allowed the simulation of the addition of the drug TTX to frontal cortex to examine the cognitive effects of this molecular intervention. Consequently, this one model flexibly incorporates a variety of levels of detail in a single simulation. This approach thus unifies simulation across levels of abstraction, from the molecular to the cognitive.

2) Integration

To demonstrate the SPA in detail, we proposed a mechanistic, functional model of the brain that uses 2.5 million spiking neurons, has about 8 billion synaptic connections, and performs 8 different tasks (see Figure 1; Eliasmith et al., 2012; Eliasmith, 2013). We refer to this large-scale neural model as the Semantic Pointer Architecture Unified Network (Spaun). Spaun includes 20 anatomical areas with matched physiological properties for cells in those areas, four types of neurotransmitters (GABA, AMPA, NMDA, and Dopamine), and includes only known anatomical connections and structure. Spaun is the result of combining a variety of simpler past models that account for focussed behavioral results (e.g. working memory, motor control, action selection). Given the large number of connections in Spaun, it is a demonstration of the importance of recurrent communication throughout a large-scale network for accomplishing a variety of cognitive and non-cognitive tasks.

What makes Spaun unique among large-scale brain models is its functional abilities. Spaun receives input from the environment through a single eye and manipulates the environment by moving a physically modelled arm. Spaun uses these interfaces to perform activities, ranging from perceptual-motor tasks (recreating the appearance of a perceived digit) to reinforcement learning (in a gambling task) to language-like inductive reasoning (completing abstract patterns in observed sequences of digits). It can perform the tasks in any order, they are all executed by the same model, and there are no changes to the model between tasks. To watch the model perform these tasks, see <http://nengo.ca/build-a-brain/spaunvideos>.

3) *Empirical contact*

NEF models have made a variety of successful predictions. For instance, an NEF model of path integration (Conklin and Eliasmith, 2005) has been credited with predicting both grid cells (Zilli, 2012) and that path integration is independent of head direction, as confirmed by (Maurer et al, 2014).

Similarly SPA models have received broad empirical support. For instance, we have compared the performance of Spaun to human and animal data at several levels of detail (Eliasmith, et al., 2012). Along many metrics the two align; for example, the model and the brain share (1) dynamics of firing rate changes in striatum during a gambling task, (2) error rates as a function of position when reporting digits in a memorized list, (3) coefficient of variation of inter-spike intervals, (4) reaction time mean and variance as a function of sequence length in a counting task, (5) accuracy rates of recognizing unfamiliar handwritten digits, and (6) success rates when solving induction tasks similar to those found on the Raven's Progressive Matrices, among other measures.

More recently, we have developed a variety of models using the SPA that demonstrate cognitive abilities not captured by Spaun. For instance, we have demonstrated the encoding and decoding of the 114,000 concepts and their relations in the WordNet database (Crawford et al., 2015). We have shown an SPA model that matches human performance on the Raven's Progressive Matrices (RPM) intelligence test, and demonstrated its ability to capture aging effects through biological manipulation (Rasmussen & Eliasmith, 2014). More abstractly, we have described how the SPA naturally unifies the three most prevalent theories of conceptual representation (Blouw, et al. 2015). We have also shown simple models of language parsing (Stewart et al., 2014; Stewart et al., 2015), instruction following (Choo & Eliasmith, 2013), and the N-back task (Gosmann & Eliasmith, 2015). In addition, models have been built using the SPA to explain a variety of other psychological-level phenomena, such as priming (Schröder and Thagard, 2014), emotion (Thagard and Schröder, 2013; Schröder, Stewart, and Thagard, 2014),

and consciousness (Thagard and Stewart, 2014).

4) *Learning*

Because the NEF often employs a non-biological optimization method for network synthesis, it has been criticized as not accounting for learning (O'Reilly et al., 2012). However, much of our recent work has been focussed on neural adaptation in various guises. This includes simple reinforcement learning (RL) in Spaun, RL models in more sophisticated semi-Markov¹ environments (Rasmussen & Eliasmith, 2013), and the first biologically plausible spiking model of hierarchical RL (Rasmussen, 2014; Rasmussen & Eliasmith, submitted). We have also described a learning rule that is able to account for STDP effects as well as learn high-dimensional, nonlinear functions, including those posited by the SPA (MacNeil & Eliasmith, 2011; Bekolay et al., 2013). We have demonstrated a means of learning auto- and hetero-associative memories in a spiking network (Voelker et al., 2014), and provided an account of motor control that reproduces a wide variety of adaptive motor behavior (DeWolf, 2015). In short, the NEF/SPA has been used to produce examples of self-organized, error-driven, and reinforcement learning using biologically plausible rules in spiking networks. We find the most effective method of constructing large-scale models is to combine the efficient non-biological methods with less efficient biologically plausible learning in order to address whichever kinds of adaptation are of interest in a given model.

Conclusion

Building large-scale models of biological cognition is in its infancy. We have reviewed some of methods worth considering in addressing this challenge. We would argue that the NEF and SPA currently have a broader demonstrated scope than current alternatives, both in terms of scaling from biological detail to cognitive behavior, and in terms of capturing critical neural mechanisms, such as those behind working memory, action selection, motor control and learning, among others.

One common challenge for any large-scale modelling effort is accessing significant computational resources. The HBP modellers have put significant effort into developing a supercomputer infrastructure to simulate their model. Similarly, we have developed a Nengo component to compile NEF/SPA models to that same kind of infrastructure. In some sense, Nengo solves the basic technical problems involved with flexibly running many different kinds of models concurrently. This ability in Nengo is generic. However, as we have designed this software tool, we have also incorporated our theories regarding neural computation (NEF) and neural organization to generate cognitive function (SPA) that leverage the ability of the software to flexibly integrate multiple models.

More interestingly, researchers have been developing specialized, efficient “neuromorphic” hardware to run brain-like algorithms in real-time (Furber et al., 2014; Merolla et al., 2014; Benjamin et al., 2014). Nengo is able to target this hardware as well (Mundy et al., 2015; Choudhary et al., 2012) opening up the possibility of testing large-scale brain models in real-world environments -- perhaps the most challenging test of our ability to replicate the robust flexibility of biological brains.

¹ Unlike a standard Markov process, the probability of there being a change in the state for a semi-Markov process depends on how much time has elapsed since the last state change.

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