Effect of stress relaxation on distortion in additive manufacturing process modeling

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Abstract

A method for modeling the effect of stress relaxation at high temperatures during Laser **Direct Energy Deposition** processes is experimentally validated for Ti-6Al-4V samples subject to different inter-layer dwell times. The predicted mechanical responses are compared to those of Inconel[®] 625 samples, which experience no allotropic phase transformation, deposited under identical process conditions. The thermal response of workpieces in additive manufacturing is known to be strongly dependent on dwell time. In this work the dwell times used vary from 0 to 40 s. Based on past research on ferretic steels and the additive manufacturing of titanium alloys it is assumed that the effect of transformation strain in Ti-6Al-4V acts to oppose all other strain components, effectively eliminating all residual stress at temperatures above 690°C. The model predicts that Inconel[®] 625 exhibits increasing distortion with decreasing dwell times but that Ti-6Al-4V displays the opposite behavior, with distortion dramatically decreasing with lowering dwell time. These predictions are accurate when compared

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with experimental in situ and post-process measurements.

1 Introduction

Laser directed energy deposition (LDED) is a frequently used additive manufacturing (AM) process. The system allows for parts to be built up by adding metal layer-by-layer rather than subtracting material through the application of typical machining techniques. This leads to increased flexibility in manufacturing which can in turn reduce costs. The process is also useful for the repair and modification of existing parts. Unfortunately AM processes result in large thermal gradients in the workpiece, causing the emergence of residual stresses and distortion. Finite element modeling (FEM) can be used to predict distortion and residual stress levels, allowing for optimization of the build plan prior to part manufacture and thus avoiding costly trial and error iterations. Residual stresses are caused by either plasticity due to contraction of the weld region or by solid-state phase transformations present in the material [1]. To accurately predict distortion and residual stress present in a workpiece, a model should account for both.

Modeling of AM has primarily focused on predicting thermal response [2–7], predicting distortion and residual stress, [8–12], and developing distortion mitigation techniques [13, 14]. Several researchers have performed thorough model validations using in situ experimental measurement techniques [3, 9, 10, 15, 16].

The use of FEM to predict distortion and residual stress in AM originates from the prior research performed on multi-pass welding. The inclusion of transformation strains caused by solid-state phase transformation present in steels has been shown to be critical in weld modeling due to the fact that transformation strains influence bulk distortion and residual stress of workpieces, with lower martensite-start temperature yielding reduced levels of residual stress and distortion [17, 18]. Francis et al. have written a thorough review of welding residual stress present in steel and note

that transformation strains present in welded steels can completely erase the strains caused by the thermal contraction of the weld region [19]. The offsetting of strain attributable to thermal contraction by transformation strains alters the bulk residual stress distribution throughout a workpiece and has been shown to reduce bending stresses on the bottom of surface of base plates for bead-on-plate welds [20]. Because AM is a similar process to welding, the welding literature suggests that transformation strains also need to be included in AM models.

While the effect of transformation strains in steel is now well understood due to the prevalent use of the material in welding, the effect of transformation strains in Ti-6Al-4V, a material commonly used in AM, has not been extensively studied. Unlike steel which transforms from a FCC structure to a BCC structure upon cooling, two phase ($\alpha + \beta$) Ti-6Al-4V undergoes an allotropic transformation from a BCC to a HCP structure. However, similarly to steel, the difference in coefficient of thermal expansion, volume, and hardness of the two Ti-6Al-4V phases alters the stress state of the material [21]. The effect of the stress relaxation on in situ distortion and residual stress in laser deposited Ti-6Al-4V has been experimentally investigated, by comparing the mechanical responses of Ti-6Al-4V workpieces to the response of Inconel[®] 625, a material that does not undergo an allotropic phase change [22]. Inter-layer dwell times were varied as previous work by Costa et al. concluded that microstructure was highly dependent on dwell times [23]. Shorter dwell times in the Ti-6Al-4V builds, which cause higher in-process temperatures to be reached and thus greater transformation to the β phase, were shown to result in dramatically reduced levels of distortion and residual stress, a trend not seen in the Inconel[®] 625 builds. The results indicate that the transformation strains oppose the strain attributed to the contraction of the molten material, similar to what has been observed in steel, causing a relaxation of the residual stress. Currently no model presented in the literature has been validated to capture this effect for LDED processing.

This work serves to validate a method for introducing the effect of stress relaxation present

in Ti-6Al-4V into FE models of LDED. First, a transient thermal model is validated against in situ temperature measurements taken during the deposition of 42 layer high, three pass wide, Ti-6Al-4V and Inconel[®] 625 wall builds with varying inter-layer dwell times. Ti-6Al-4V is chosen due to the fact that it undergoes a solid-state phase transformation. Inconel[®] 625 should be possible to accurately model without the inclusion of transformation strains, as it does not undergo a solid-state phase transformation. Next, the constitutive model neglecting transformation strains is used to model the mechanical responses of the materials and compared with experimental in situ distortion measurements and post-process residual stress measurements. The Ti-6Al-4V builds are then simulated while accounting for the transformation strains to investigate if improved correlation with experiment is achieved.

2 Modeling Approach

The thermal history is first calculated by performing a three-dimensional transient thermal analysis. The thermal results are then input into a three-dimensional quasi-static incremental analysis which simulates the mechanical response. The thermal analysis can be performed independently of the mechanical analysis because the plastic strain energy is small compared to the laser source energy, making the analyses weakly coupled [24]. A detailed description of the model is available in reference [16].

2.1 Transient Thermal Analysis

The governing transient heat transfer energy balance in the entire volume of the material is given as:

$$\rho C_p \frac{dT}{dt} = -\nabla \cdot \mathbf{q}(\mathbf{r}, t) + Q(\mathbf{r}, t) \quad (1)$$

where ρ is the material density, C_p is the specific heat capacity, T is the temperature, t is the time, Q is the internal heat generation rate, $\mathbf{r}$ is the relative reference coordinate, and $\mathbf{q}$ is the heat flux. The Fourier heat flux constitutive relation is given by:

$$\mathbf{q} = -k\nabla T \quad (2)$$

dependent on temperature dependent thermal conductivity k .

Thermal radiation q_{rad} is accounted for using the Stefan-Boltzmann law:

$$q_{rad} = \varepsilon\sigma(T_s^4 - T_\infty^4) \quad (3)$$

where ε is the surface emissivity, σ is the Stefan-Boltzmann constant, T_s is the surface temperature of the workpiece, and T_∞ is the ambient temperature.

Newton's law of cooling describes the heat loss due to convection q_{conv} :

$$q_{conv} = h(T_s - T_\infty) \quad (4)$$

where h is the convective heat transfer coefficient.

2.2 Mechanical Analysis

The governing mechanical stress $\boldsymbol{\sigma}$ equilibrium equation is written as:

$$\nabla \cdot \boldsymbol{\sigma} = \mathbf{0} \quad (5)$$

The mechanical constitutive law is:

$$\boldsymbol{\sigma} = \mathbf{C}\boldsymbol{\epsilon}_e \quad (6)$$

Total strain $\boldsymbol{\epsilon}$, assuming small deformation thermo-elasto-plasticity, is decomposed as:

$$\boldsymbol{\epsilon} = \boldsymbol{\epsilon}_e + \boldsymbol{\epsilon}_p + \boldsymbol{\epsilon}_T + \boldsymbol{\epsilon}_t \quad (7)$$

where $\mathbf{C}$ is the fourth order material stiffness tensor, and $\boldsymbol{\epsilon}_e$, $\boldsymbol{\epsilon}_p$, $\boldsymbol{\epsilon}_T$, and $\boldsymbol{\epsilon}_t$ are the elastic, plastic, thermal, and transformation strain, respectively. The thermal strain is computed as:

$$\boldsymbol{\epsilon}_T = \boldsymbol{\epsilon}_T \dot{\mathbf{j}} \quad (8)$$

$$\boldsymbol{\epsilon}_T = \boldsymbol{\alpha}(T - T^{ref}) \quad (9)$$

$$\dot{\mathbf{j}} = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 \end{bmatrix}^T \quad (10)$$

where $\boldsymbol{\alpha}$ is the thermal expansion coefficient and T^{ref} is reference temperature. The plastic strain is computed by enforcing the von Mises yield criterion and the the Prandtl-Reuss flow rule:

$$f = \sigma_m - \sigma_y(\boldsymbol{\epsilon}_q, T) \leq 0 \quad (11)$$

$$\dot{\boldsymbol{\epsilon}}_p = \dot{\boldsymbol{\epsilon}}_q \mathbf{a} \quad (12)$$

$$\mathbf{a} = \left(\frac{\partial f}{\partial \boldsymbol{\sigma}} \right)^T \quad (13)$$

where f is the yield function, σ_m is Mises' stress, σ_y yield stress, $\boldsymbol{\epsilon}_q$ is the equivalent plastic strain, and $\mathbf{a}$ is the flow vector.

For an incremental formulation, Equation (6) is re-written as:

$${}^n\boldsymbol{\sigma} = {}^{n-1}\boldsymbol{\sigma} + \Delta\boldsymbol{\sigma} \quad (14)$$

where ${}^{n-1}\boldsymbol{\sigma}$ and ${}^n\boldsymbol{\sigma}$ are the stress at the previous and current increment. The stress increment $\Delta\boldsymbol{\sigma}$ is computed as:

$$\Delta\boldsymbol{\sigma} = \Delta\mathbf{C}({}^{n-1}\boldsymbol{\epsilon} - {}^{n-1}\boldsymbol{\epsilon}_p - {}^{n-1}\boldsymbol{\epsilon}_T - {}^{n-1}\boldsymbol{\epsilon}_t) + \mathbf{C}(\Delta\boldsymbol{\epsilon} - \Delta\boldsymbol{\epsilon}_p - \Delta\boldsymbol{\epsilon}_T - \Delta\boldsymbol{\epsilon}_t) \quad (15)$$

where left superscripts denote the time increment where a quantity is computed and $\Delta\boldsymbol{\epsilon}$ is the total strain increment corresponding to the current displacement increment.

Stress relaxation present in Ti-6Al-4V at high temperatures is accounted for when the norm of temperature of an element's Gauss points exceeds 690°C. At this occurrence the following relation is enforced:

$${}^{n-1}\epsilon_t = -({}^{n-1}\epsilon_e + {}^{n-1}\epsilon_p + {}^{n-1}\epsilon_T) \quad (16)$$

meaning that an assumption is being made that the transformation strains will completely negate the strain components that are attributable to the thermal contraction of the deposition region, a phenomenon that has been observed in the welding of steel. The relaxation of the hydrostatic strain components is likely due to volume and thermal expansion mismatches between the two phases, however the exact mechanism is not known and in situ X-ray diffraction measurements would be required to study this hypothesis. In addition, the erasing of crystal dislocations is simulated by setting ϵ_p equal to zero at 690°C.

In addition, the residual stress σ values are set to zero. The approximation was previously shown to yield accurate distortion and residual stress results for the Electron-beam Direct Manufacture (EBDM) process [16]. Ideally the transformation strain ϵ_t would be determined by applying a constitutive relation depending on phase fraction. However, an accurate constitutive model for the transformation strain in Ti-6Al-4V is not available for multi-pass depositions and the development of such a model is beyond the scope of the present work.

3 Experimental Validation

The modeling approach laid out in Section two is applied to simulate the experimental results for Ti-6Al-4V and Inconel® 625 wall builds from reference [22] in an attempt to capture the mechanical responses reported. A brief overview of the experiment is provided here.

Single wall structures were fabricated on a 12.7 mm substrate of matching material using a laser-directed energy deposition process. The two materials chosen to compare were Ti-6Al-4V and Inconel[®] 625 with the reasoning that Ti-6Al-4V undergoes an allotropic phase transformation and Inconel[®] does not. The setup allows 1 end of the substrate to be clamped and allows the free end of a cantilevered substrate to distort during the deposition. A laser displacement sensor (LDS) with a linear accuracy of $\pm 1 \mu\text{m}$ was placed to record the in situ bowing distortion in the z-direction. Thermocouples with an accuracy of $\pm 0.75 \%$ recorded the in situ thermal response of the workpiece. Figure 1(a) shows the locations of the thermocouples and LDS used for model validation.

The depositions are performed at a laser power of 2 kW and a laser scan speed of 10.6 mm/s. The laser beam spot size was measured to be 4 mm in diameter at the part surface. The laser penetration depth was found to be 1.1 mm by sectioning as recommended by Goldak [25].

Figure 1(b) shows the dimensions of each build. Each deposited 42-layer high, three-bead wide, wall was 38.1 mm tall, 101.6 mm long, and 6.7 mm wide. The substrates used measured 152.4 mm long, 38.1 mm wide, and 12.7 mm thick. After the deposition of each layer a dwell time was added to allow for a period of cooling. Dwell times of 0, 20, and 40 seconds were used for each material to expose the parts to differing amounts of cooling time. Table 1 summarizes the cases.

(a) Locations of the thermocouple 1 (A), thermocouple 2 (B), LDS (C), and blind hole drilling (B) measurements.

(b) Dimensions of the substrate and wall.

Figure 1: Illustration of the sample dimensions and measurement locations

Table 1: Description of the cases

Case	Material	Dwell time (s)
1	Inconel [®] 625	0
2	Inconel [®] 625	20
3	Inconel [®] 625	40
4	Ti-6Al-4V	0
5	Ti-6Al-4V	20
6	Ti-6Al-4V	40

In addition to the in situ distortion and temperature measurements, residual stress measurements were taken post-process. The hole drilling method was used to take a stress measurement on the substrate of each sample. Figure 1(a) shows the measurement location. The hole drilling method has an accuracy of ± 50 MPa.

4 Numerical Implementation

Figure 2 displays the three-dimensional finite element mesh, generated in Patran 2012 by MSC, used for both the thermal and mechanical analyses. The same mesh is used for all cases. The mesh contains 52,472 Hex-8 elements and 62,231 nodes. Hex-8 elements were chosen because they have been shown to yield more accurate results than tetrahedral elements when plastic deformation occurs [26]. The elements for the deposited material are allotted as two per laser spot size radius and 1 per deposition thickness, making the elements $1 \times 1 \times 0.87$ mm³ in volume. The mesh is coarsened as it moves away from the deposition. A three-step mesh convergence study was performed to confirm the suitability of the mesh, **and to insure that inaccuracy did not arise due to shear locking. The mesh used contains elements with aspect ratios of 3.175.** Each mesh used in the convergence study varied the aspect ratio. The fixture clamp is included in the model to capture heat loss through conduction.

Figure 2: Finite element mesh used for all simulations.

4.1 Solution Method

The thermal and mechanical analyses are performed using the code CUBES[®] by Pan Computing LLC. The analyses are performed in a series of time steps with the current time step taking the solution at the previous time step as an initial condition. Each time step moves the heat source a distance equal to its radius. At each time step the discrete equilibrium equations are solved using the Newton-Raphson method.

The temperature dependent material properties for Ti-6Al-4V and Inconel[®] 625 are listed in Table 2. The properties between those listed are obtained by linear interpolation over the temperature range. Properties at temperatures above and below those listed are taken as the nearest tabulated value. Density is a constant $4.43 \times 10^{-6} \text{ g/mm}^3$ and $8.44 \times 10^{-6} \text{ g/mm}^3$ for Ti-6Al-4V and Inconel[®] 625, respectively. The emissivity ε of Inconel[®] 625 is taken as 0.28 as found in reference [27]. The reference does state that the value is only an approximation, as the emissivity will vary with surface finish. The emissivity ε of Ti-6Al-4V is set as 0.25, as experimentally determined by Yang [28] for LDED processing of Ti-6Al-4V. The convective heat transfer coefficient h is taken as $18 \text{ W/m}^2/\text{°C}$ by correlating simulated and experimental results.

Table 2: Temperature dependent thermal properties of Ti-6Al-4V [29] and Inconel[®] 625 [30]

T (°C)	k (W/m/°C)	C_p (J/kg)	k (W/m/°C)	C_p (J/kg)
Ti-6Al-4V			Inconel [®] 625	
20	6.6	565	9.9	410
93	7.3	565	10.8	427
205	9.1	574	12.5	456
315	10.6	603	14.1	481
425	12.6	649	15.7	511
540	14.6	699	17.5	536
650	17.5	770	19.0	565
760	17.5	858	20.8	590
870	17.5	959	22.8	620
982	-	-	25.2	645

The temperature dependent mechanical properties for Ti-6Al-4V and Inconel 625, listed in Table 3, include the elastic modulus E , yield strength σ_y , and the coefficient of thermal expansion α .

Table 3: Temperature dependent mechanical properties of Ti-6Al-4V [8, 29] and Inconel[®] 625 [30]

T (°C)	E (GPa)	σ_y (MPa)	α ($\mu\text{m} / \text{m } ^\circ\text{C}$)	E (GPa)	σ_y (MPa)	α
Ti-6Al-4V				Inconel [®] 625		
20	104	768	8.60	208	493	12.8
93	101	735	8.66	204	479	12.8
205	94.0	685	8.75	198	443	13.1
315	88.3	636	9.08	192	430	13.3
425	82.6	586	9.40	186	424	13.7
540	77.5	542	9.55	179	423	14.0
650	72.6	501	9.70	170	422	14.8
760	67.7	459	9.70	161	415	15.3
870	62.8	417	9.70	148	386	15.8
927	-	-	-	-	-	16.2

4.2 Boundary Conditions

Convection and radiation are applied to all free surfaces of the mesh. The model substrate is mechanically constrained as cantilevered to represent the experimental conditions. The laser heat source is modeled using the Goldak double ellipsoid model [25] as follows:

$$Q = \frac{6\sqrt{3}P\eta}{abc\pi\sqrt{\pi}} e^{-[\frac{3x^2}{a^2} + \frac{3y^2}{b^2} + \frac{3(z+vt)^2}{c^2}]} \quad (17)$$

where P is the incident laser power, η is the absorbtion efficiency; x , y , and z are the local coordinates; a , b , and c are the transverse, depth, and longitudinal dimension of the ellipsoid respectively, v is the scan speed, and t is the time.

4.3 Material Deposition Modeling

A hybrid quiet-inactive element approach is used to simulate the addition of deposited material. The method was proposed in reference [31]. At the start of the simulation all deposited elements are inactive, i.e., not part of the analysis. The elements are switched to quiet, meaning that they are given properties such that they do not affect the analysis, on a layer-by-layer basis. A quiet element is made active when the following condition is met at any Gauss point of the element [31]:

$$\frac{6\sqrt{3}}{abc\pi\sqrt{\pi}} e^{-[\frac{3x^2}{a^2} + \frac{3y^2}{b^2} + \frac{3(z+vt)^2}{c^2}]} \geq 0.05 \quad (18)$$

Both surface radiation and convection are applied as a boundary condition to the evolving interface between quiet and active elements, which is identified at each time increment.

5 Modeling results and comparison to the experiment

5.1 Thermal History

The thermal response of the workpiece is calculated by the model and compared to the experimental measurements. Figure 3 shows the experimental results, as measured by thermocouples 1 and 2, compared to calculated results at nodes corresponding to the thermocouple locations for each case. Reference [22] notes that because thermocouple 1 and 2 are at different locations on the substrate, they record different thermal histories. Thermocouple 1, at the free end of the substrate, shows a lower peak temperature than thermocouple 2, at the middle of the substrate. Samples with the same dwell times display similar thermal histories independent of the sample material. For each case the sample temperatures increase for roughly the first third of the build and then begin to decrease due to the heat source moving vertically away from the thermocouple locations. Longer dwell times results in lower peak temperatures with the 40 s dwell cases (Case 3 and Case 6)

exceeding 400°C and the 0 s dwell cases (Case 1 and Case 4) exceeding 600°C.

Figure 3: In situ thermal history of each thermocouple for all wall builds. (a) Case 1, (b) Case 4, (c) Case 2, (d) Case 5, (e) Case 3, (f) Case 6.

The results of the transient thermal analyses are in close agreement with the experimental results as can be seen in Figure 3. The average percent error for the entire simulation of each case can be calculated as

$$\% Error = \frac{100 \sum_{i=1}^n \left| \frac{(x_{exp})_i - (x_{sim})_i}{(x_{exp})_i} \right|}{n} \quad (19)$$

where n is the total number of simulated time increments, i is the current time increment, x_{sim} is the simulated value, and x_{exp} is the experimentally measured value. The largest error at any thermocouple is found to be 12.0 %. Table 4 shows the percent error at each thermocouple for all cases.

Table 4: Cases examined for thermal model calibration

Case	Material	Dwell time (s)	% Error TC 1	% Error TC 2
1	Inconel [®] 625	0	7.45	12.0
2	Inconel [®] 625	20	6.37	3.24
3	Inconel [®] 625	40	9.65	4.46
4	Ti-6Al-4V	0	2.20	1.48
5	Ti-6Al-4V	20	7.12	3.85
6	Ti-6Al-4V	40	9.14	3.14

5.2 Distortion History

In situ distortion is calculated and compared to the experimental measurements of the distortion of 12.7 mm thick Inconel[®] and Ti-6Al4V substrates during laser deposition with dwell times ranging from 0 to 40 s. Figure 4 shows the final calculated distortion of Inconel[®] wall deposited with no dwell time (Case 1). The distortion is caused by the shrinking of the deposited material upon cooling. The LDS monitors the in situ distortion of the free end of the substrate. The simulated in situ distortion is recorded at a node corresponding to the LDS measurement location in the model.

Figure 4: Mechanical model showing the final distorted shape of the workpiece (4 x magnification), Case 1.

5.2.1 Inconel[®] 625

Figure 5 presents the measured and simulated distortion for the Inconel[®] 625 builds with 0 (Case 1), 20 (Case 2), and 40 s (Case 3) dwell times. Periods of decreasing distortion are caused by the thermal expansion of the top of the substrate due to heating from the laser. An increase in distortion is attributable to the shrinking of the deposited material upon cooling. Each of the Inconel[®] 625 experimental builds displays a consistent accumulation of distortion over the duration of the build which occurs independent of dwell time. The simulated distortion of the model captures these trends and is in close agreement with the experiment throughout the deposition for each case.

(a) Case 1: Inconel® 0s Dwell

(b) Case 2: Inconel® 20s Dwell

(c) Case 3: Inconel® 40s Dwell

Figure 5: Calculated in situ distortion results for the Inconel® 625 samples compared with the experimental data.

5.2.2 Ti-6Al-4V

Figure 6 shows the calculated distortion time trace for the Ti-6Al-4V samples, both with and without the inclusion of stress relaxation, compared with the experimental measurements for dwell times of 0 (Case 4), 20 (Case 5), and 40 s (Case 6). The simulations that employ the constitutive model with no transformation strain show distortion accumulating consistently throughout the deposition, similar to the trend seen in the Inconel[®] builds, but with significantly higher levels of distortion. This prediction is at odds with the experimental measurements which show significantly lower distortion levels in the Ti-6Al-4V builds when compared with the Inconel[®] builds. The fact that the model predicts a consistent accumulation of distortion with respect to time is also not in agreement with the measurements, which in the Case of the 0 and 20 s dwell cases show a reduction of distortion accumulation following the initial deposited layers. This reduction in distortion levels occurs due to the fact that the relaxation of residual stress, caused by the transformation strain negating the strain attributed to the contraction of the deposited material, manifests itself as a reduction in accumulated distortion [16].

In addition to not capturing the trend of distortion accumulation, the constitutive model neglecting transformation strain also significantly over predicts the final distortion of the workpiece. For example in Case 4 (0 s dwell), the calculated distortion of 6.39 mm over predicts the measured final distortion of 1.14 mm by 461 %. This percent error is similar to that reported in reference [16] when a constitutive model without stress relaxation was used to model the distortion of Ti-6Al-4V deposited by an electron beam.

Unlike the constitutive model that neglects transformation strain, the simulations using the constitutive model that includes the transformation strain term show that in the 0 s dwell case, Ti-6Al-4V does not consistently accumulate distortion over the duration of the build. The model actually registers a reduction of distortion after the initial layers, shown in Figure 7, followed by

little accumulation over the rest of the build. This effect is lessened when adding a 20 s dwell time and is not present at all when a 40 s dwell is added, showing consistent distortion accumulation throughout the build. These predictions, showing a strong dependence of distortion on dwell time, are in close agreement with the experimental observations.

(a) Case 4: Ti-6Al-4V 0s Dwell

(b) Case 5: Ti-6Al-4V 20s Dwell

(c) Case 6: Ti-6Al-4V 40s Dwell

Figure 6: Calculated in situ distortion results for the Ti-6Al-4V samples compared with the experimental data.

(a) Calculated in situ distortion results for Case 4 (Ti-6Al-4V 0 s dwell time, compared with experiment for the first 15 deposition layers.

(b) Calculated in situ distortion results for Case 5 (Ti-6Al-4V 20 s dwell time, compared with experiment for the first 15 deposition layers.

Figure 7: Calculated in situ distortion results for the Ti-6Al-4V samples compared with the experimental data showing the loss in accumulated distortion.

5.3 Residual Stress

Residual stress values are calculated for all time-steps during the simulation. The final calculated value for residual stress at the location of the blind hole drilling measurement is compared to the

experimental measurement for the Inconel[®] 625 and Ti-6Al-4V substrates with dwell times ranging from 0 to 40 s. The longitudinal component of stress is chosen for comparison, as it is the dominate component.

5.3.1 Inconel[®] 625

The residual stress predictions from the model are compared with the results from the blind hole drilling experiments in Figure 8. The model predicts that residual stress in the Inconel[®] 625 exhibits nearly no dependence on dwell time, showing a post-process residual stress of just over 500 MPa. The experiment shows decreasing residual stress with increasing dwell time, a trend not captured by the model likely due to the fact that temperature dependent precipitation hardening present in Inconel[®] 625 is not included in the model. Figure 9 shows the calculated residual stress (σ_{xx}) contour plots at the yz mid cross section.

Figure 8: Calculated residual stress (σ_{xx}) results for the Inconel[®] 625 samples compared with the experimental data.

(a) Inconel[®] 625 0 s dwell time.

(b) Inconel[®] 40 s dwell time.

Figure 9: Calculated residual stress (σ_{xx}) results at the mid yz cross section for the Inconel[®] 625 samples.

5.3.2 Ti-6Al-4V

Figure 10 shows the residual stress results for the model when including transformation strain and neglecting transformation strain compared with the experimental measurements. The experimental

measurements show that residual stress in the Ti-6Al-4V increases with increasing dwell time. While the model neglecting transformation strain captures this trend, it over predicts the residual stress magnitude by over 500 % in all cases. When transformation strain is incorporated into the model the residual stress results are under predicted in each case, however the calculations are all within 22 % of the measurement error bars and thus represent a significant reduction in the percent error when compared with the experiment. The under prediction of the residual stress is an expected consequence of implementing the relaxation of residual stresses instantaneously. In reality the stress relaxation likely takes place over time. Further experimental work would need to be performed to incorporate a dynamic stress relaxation into the model and improve correlation with the experiments. Figure 11 shows the calculated residual stress (σ_{xx}) contour plots at the yz mid cross section.

Figure 10: Calculated residual stress (σ_{xx}) results for the Ti-6Al-4V samples compared with the experimental data.

(a) Ti-6Al-4V 0 s dwell time.

(b) Ti-6Al-4V 40 s dwell time.

Figure 11: Calculated residual stress (σ_{xx}) results at the mid yz cross section for the Ti-6Al-4V samples.

6 Conclusions

Being able to predict the mechanical response of AM workpieces is important if expensive trial and error iterations are to be avoided. A model has been validated to adequately account for

the transformation strain present in Ti-6Al-4V, a common alloy used in direct metal deposition. The model was validated by varying inter-layer dwell times, which are known to impact sample temperature and thus phase transformation effects, for Ti-6Al-4V and Inconel[®] 625 wall builds. The in situ temperature, in situ distortion, and post-process residual stress predictions were compared with experimental measurements. The Inconel[®] 625 builds can be adequately modeled without the inclusion of transformation strain, as the alloy does not undergo a solid-state phase transformation. However, for Ti-6Al-4V which does undergo solid-state phase transformation, neglecting the effect of transformation strain incurs errors of over 500% when predicting post-process residual stress and distortion, and also does not capture the distortion accumulation trends observed during the in situ measurements. Modeling that the transformation strain caused by solid-state phase transformation in Ti-6Al-4V acts to fully relax the residual stress at temperatures above 690°C, leads to close agreement with experimental measurements. This modeling effort highlights the need for future work focusing on further development of a high-temperature constitutive model for Ti-6Al-4V. High temperature Gleeble testing could provide insight into the dynamic nature of the strain relaxation noted in Ti-6Al-4V. Better understanding of the relationship between temperature, microstructure, and material properties is needed to develop a more physically realistic constitutive model.

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