Using albedo to reform wind erosion modelling, mapping and monitoring

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Abstract

Wind erosion and dust emission models are used to assess the impacts of dust on radiative forcing in the atmosphere, cloud formation, nutrient fertilisation and human health. The models are underpinned by a two-dimensional geometric property (lateral cover; L) used to characterise the three-dimensional aerodynamic roughness (sheltered area or wakes) of the Earth's surface and calibrate the momentum it extracts from the wind. We reveal a fundamental weakness in L and demonstrate that values are an order of magnitude too small and significant aerodynamic interactions between roughness elements and their sheltered areas have been omitted, particularly under sparse surface roughness ($0.001 < L < 0.1$). We describe a solution which develops published work to establish a relation between sheltered area and the proportion of shadow over a given area; the inverse of direct beam directional hemispherical reflectance (black sky albedo; BSA). We show direct relations between shadow and wind tunnel measurements and thereby provide direct calibrations of key aerodynamic properties. Estimation of the aerodynamic parameters from albedo enables wind erosion assessments over areas, across platforms from the field to airborne and readily available satellite data. Our new approach demonstrated redundancy in existing wind erosion models and thereby reduced model complexity but improved fidelity. We found that the use of albedo enabled an adequate description of aerodynamic sheltering to characterise fluid dynamics and predict sediment transport without the use of a drag partition scheme (R_t) or threshold friction velocity (u_{*t}). We applied the calibrations to produce global maps of aerodynamic properties which showed very similar spatial patterns to each other and confirmed the redundancy in the traditional parameters of wind erosion modelling. The global maps identified regions of small aerodynamic roughness previously thought to be susceptible to wind erosion because of their erodibility. We evaluated temporal patterns of predicted horizontal mass flux at locations across Australia which revealed variation between land cover types that would not be detected using traditional models. Our new approach provides new opportunities to investigate the dynamics of wind erosion in space and time and elucidate aeolian processes across scales.

1. Introduction

Wind erosion and dust emission are driven by the turbulent transfer of momentum from the fluid to the land surface (Shao et al., 2015). The aerodynamic turbulence is influenced by surface roughness across a range of scales from the soil grain (mm) to the landscape (km). At these scales, roughness elements comprise individual landforms (e.g., dunes), vegetation (trees, shrubs, grasses) which may be photosynthetic or non-photosynthetic, and the exposed soil surface which may be rough or smooth depending on the presence of physical, chemical or biogenic crusts, the soil texture, natural structures (rocks) or management-induced features (clods, furrows). All of these roughness elements have a spatial arrangement (or spatial dependence) originating from the processes which formed them. Dunes are aligned with wind flows (Lancaster, 2013), vegetation may be aligned with wind, water or nutrient flows (Okin et al., 2015) and the soil surface may have structure within and between vegetation patches due to natural or human-induced patterns (Webb and Strong, 2011). All of these roughness elements are temporally variable or dynamic. Within any particular timeframe the surface roughness causes a highly anisotropic extraction of wind momentum relative to its direction. Natural heterogeneous mixtures of roughness elements produce highly variable aerodynamic turbulence and momentum extraction which are responsible for the magnitude and spatial patterns of wind erosion and dust emission (Gillette, 1999).

The seminal work of Bagnold (1941) provided the foundation for numerous subsequent field studies to investigate the relation between wind velocity profiles, aerodynamic turbulence and point-based sediment transport. Much of the knowledge about the spatial and temporal variation of aerodynamic turbulence across scales is gained from point-based field work and wind tunnel studies (e.g. Marshall, 1971; Gillette and Stockton, 1989; Wolfe and Nickling, 1996; Lancaster and Baas, 1998; Gillies et al., 2000, 2007; Crawley and Nickling, 2003; King et al., 2006; Brown et al., 2008; Webb et al., 2014). Wind tunnel studies have also replicated the fieldwork and isolated the controlling factors to improve our understanding of aerodynamic turbulence, roughness (z_0) and transport feedbacks (Duran et al., 2011; Charru et al., 2013; Jenkins and Valance, 2014). Accurate estimation of

48 sediment transport rates is dependent on capturing the aerodynamic roughness feedbacks to saltation, which
49 affect the scaling of transport rates with the area-integrated (areal) momentum flux and ultimately the
50 magnitude of dust emissions from given areas.

51 At the landscape scale, wind velocity profiles have been used to determine the aerodynamic roughness for
52 diverse vegetation and surface roughness conditions (e.g. MacKinnon et al., 2004; Gillette et al., 2006). These
53 measurements include heterogeneous combinations of roughness scales, orientations and anisotropic responses
54 to roughness elements. However, little consideration has been given to the upstream area, and therefore which
55 mixtures of roughness elements, influence z_0 and hence which scale has contributed most. Andre and Blondin
56 (1986) and Taylor (1987) suggested that the integrated roughness length is strongly influenced by its spatial
57 variability. Wieringa (1993) indicated that relatively rough patches contribute more to the effective aerodynamic
58 roughness of a surface than their area fraction. The confounding anisotropic interaction between wind direction,
59 contributing area and roughness scale is consistently omitted from studies (Chappell et al., 2010; Smith et al.,
60 2016). Raupach and Lu (2004) questioned the extent to which wind erosion and dust emission models, developed
61 to represent processes at the point scale, are applicable to heterogeneous situations over large areas or pixels.
62 Although improved accuracy of measurement and statistical modelling (Bauer et al., 1992) has reduced
63 uncertainty in the estimation of z_0 from wind velocity profiles, this standardisation may have distracted research
64 in this field from establishing the uncertainty from the many sources of variance. For example, if masts of
65 anemometers were placed at different locations within a given area or pixel (measuring at the same time without
66 interfering with the wind flow) they would most likely provide wind velocity profiles with different z_0 ; its spatial
67 variability. If those estimates of z_0 from within that area were unbiased samples and adequately represented the
68 spatial variation, then the average and variance of z_0 would accurately and precisely characterise the area.
69 Similarly, it is difficult to use a wind velocity profile from a single location to estimate the surface shear stress of
70 an area if it is influenced by spatially varying soil surface roughness and heterogeneous vegetation elements.

71 There is evidently a need to establish the spatial variability or the areal average (integrated) of aerodynamic
72 properties to more accurately account for their influence on wind erosion and dust emission. Researchers have
73 looked to remote sensing to provide area average estimates of z_0 on the basis that light is scattered in proportion
74 to the size and number of roughness elements within a pixel. However, the challenge, in common with many
75 aspects of remote sensing, is to find a property that can be retrieved from reflectance data, which is related to z_0 ,
76 robust across scales and may be transferred to other places or times. Greeley et al. (1991) linked wind velocity
77 profile estimates of z_0 to radar backscatter cross sections from airborne and space borne platforms (Greeley et al.,
78 1997). Marticorena et al. (2006) showed significant relations between radar backscatter coefficients and z_0 and
79 proposed an empirical relation to retrieve z_0 using radar observations in the C band from operational sensors.
80 Marticorena et al. (2004) suggested a proportional relationship between the protrusion coefficient derived from a
81 bi-directional reflectance model and geometric roughness and then to z_0 . Chappell et al. (2010) established a
82 physically-based relation between sheltered area and single scattering albedo from bi-directional reflectance
83 models. These approaches have all shown promise for overcoming the limitations of field measurements of z_0 and
84 direct application in representing momentum transfer in wind erosion and dust emission models.

85 Perhaps one of the most influential approximations in aerodynamic turbulence is that momentum extracted by
86 roughness elements can be represented by roughness density (lateral cover or the frontal area index L ; Marshall,
87 1971; Wooding et al., 1973). However, L omits the interaction between roughness elements i.e., ignores the
88 orientation of objects and assumes that they are isotropic within a pixel. In practice, the estimation of L over large
89 areas (regions, continents) is difficult and often approximated using classifications of cover and vegetation type
90 from satellite remote sensing and in the case of bare surfaces, using geometry (cf. Shao et al., 1997; Marticorena
91 et al. 2006). These practical approximations create discontinuities between land surface classes for the models
92 and largely exclude heterogeneity due to mixtures of different surface types. This uncertainty is significant
93 because these models are used to predict regional and global wind erosion and dust emission (e.g., Marticorena
94 and Bergametti, 1995; Alfaro and Gomez, 1995; Shao, 2001).

95 There remains a need to reduce the uncertainty associated with the estimation and parameterisation of
 96 aerodynamic turbulence for aeolian process studies using a holistic approach that works across scales of
 97 roughness. The objectives of this paper are to: outline the basis for the established method of reducing the
 98 complexity of aerodynamic turbulence using lateral cover (Raupach et al., 1993), reveal weaknesses in the lateral
 99 cover and thereby provide the rationale for a new approach based on shadow (Section 2); outline the foundation
 100 for the shadow-based approach and describe its physically-based development from Raupach's concept and show
 101 how it can be used to estimate key aerodynamic parameters (section 3); demonstrate how wind erosion
 102 modelling can be more parsimonious whilst retaining the fidelity of the processes (Section 4); illustrate the use of
 103 shadow with estimates from the Moderate Resolution Imaging Spectroradiometer (MODIS) (every 8 days and
 104 every 500 m) to map and monitor areal aerodynamic parameters for wind erosion (sediment flux) across a range
 105 of land surface types and demonstrate their dynamics in space and time (Section 5); consider the implications and
 106 opportunities that this new approach provides for aeolian research across scales of variation (grain to landscape;
 107 section 6).

108 2. Lateral cover and its weaknesses for wind erosion modelling

109 In his seminal work, Raupach (1992) reduced the complexity of aerodynamic roughness by characterising the
 110 wake of an isolated roughness element placed on the surface using an effective shelter area (A ; Figure 1a). He
 111 used cylinders to represent roughness elements, assuming that they were an adequate approximation of the
 112 plant structure. He reasoned that the ground surface shear stress (τ_s) within A should be zero and idealised A as a
 113 wedge-shaped "shadow" in the lee of the roughness element (Figure 1a). Raupach (1992) provided a physical
 114 basis for this scaling (Hypothesis I) in which the shear layers bounding the wake spread at an elevation angle of
 115 order $\alpha = U_h/u_*$ (where U_h is the mean wind velocity at height h) to the streamwise direction, similar to the inner
 116 layer of modified wind flow over a hill (Finnigan et al., 1990).

120 **Figure 1** The (a) Raupach (1992) concept for reducing the complexity of aerodynamic roughness and its
 121 representation (b) using shadow by Chappell et al., (2010) to enable an approximation using remote sensing.
 122 Reproduced from Shao et al. (2015).

123 Raupach (1992) assumed that the ground surface shear stress reductions in the wake of an element are spread
 124 over a region considered large relative to A (Hypothesis II). This assumption considers the interaction between
 125 the elements and potential element wakes to be dependent on the roughness density (defined in the next
 126 paragraph) and not on the arrangement of roughness elements at the surface as demonstrated by Marshall's
 127 (1971) empirical study. Raupach (1992) described how neither of his hypotheses were an exact statement, but

that both physically-based approximations permitted a straightforward analysis. Raupach's approximations represent a "quantum fluid" approach which generalises the influence on wind flow of an individual roughness element to estimate the total effect for all roughness elements in a given area (Shao et al., 2015).

However, there is an inconsistency between the approximations and the application which we explain next. The roughness density or lateral cover (L) is the frontal (silhouette) area of roughness elements. For cylinders this reduces to

$$L = nbh/S \quad (\text{Eq. 1})$$

where n is number of roughness elements, b is their breadth, h their height and S the ground surface area in which the roughness element frontal area (bh ; b is breadth and h is height) is projected to a smooth plane. In this approach L is projected (implicitly) at an angle of 45° (L_{45}) which is fixed for all surface roughness which implies that

$$L_{45} = A_{45}/S = nbh \tan(45)/S \quad (\text{Eq. 2})$$

(recall $\tan(45)=1$ hence $L=nbh/S$). In contrast, Raupach (1992) described in general

$$A_\alpha = c_1 bh U_h/u_* \quad (\text{Eq. 3})$$

where $c_1 = c'_1(b/h)^p$ and which implies that

$$L_\alpha = nbh \tan(\alpha)/S. \quad (\text{Eq. 4})$$

When calculated using Marshall's (1971) data (for simplicity setting $U_h = U_f$ the freestream velocity, $p=0$ and $c_1=1$) we found $A_\alpha/S = L_\alpha$ and that $A_\alpha/S \neq L_{45}$. Using Marshall's (1971) experiments of roughness elements, the L_{45} was an order of magnitude smaller than that of L_α . The L_{45} was always <1 and the length of A_{45} ($h=2.54$ cm) did not exceed the spacing of the roughness elements in any of Marshall's configurations. In contrast, α ranged between elevation angles of $2-5^\circ$ (zenith angle $85-88^\circ$). For clarity, this means that the length of the shelter area is 11-27 times either half the width of the roughness elements (1.27-12.7 cm) and ranged 9-164 cm, or 11-27 times the height of the roughness element (2.54 cm) and hence ranges between 29-68 cm. In the latter case L_α is greater than L_{45} in approximately one third of Marshall's surface roughness configurations. The length of A_α exceeded the spacing between the roughness elements in all but the sparsest configurations (13 of the 37 experiments considered). Evidently, the best approximation of lateral cover is L_α which produces interactions between sheltered areas and downstream roughness elements for the majority of Marshall's experiments. The implications of these findings are that (i) interactions between roughness elements have been hidden from previous researchers by the longstanding tradition of using L_{45} ; and (ii) configuration of roughness elements is important for the calculation of the surface shear stress and drag partition. However, we show next that L_α cannot be used to replace L_{45} .

Recall that total force F acting on S of a rough surface can be partitioned between a force acting on the roughness elements (F_R) and that acting on the substrate surface (F_S ; in the absence of any roughness elements) such that $F = F_R + F_S$ (Schlichting, 1936). These forces are divided by S to produce their respective stresses:

$$\tau = \rho u_*^2 = \tau_R + \tau_S \quad (\text{Eq. 5})$$

where ρ is the air density and u_*^2 the square of the wind friction velocity. Shao and Yang (2008) suggested that the total drag should be partitioned into three components and should include the canopy friction drag (τ_C). Notably, their drag partition requires L_{45} and the fraction of cover (a_c) as input parameters. Given the fundamental flaw in L_{45} demonstrated previously, we do not pursue this additional component. Following Raupach et al. (1993) τ_S is normalised over the total ground area S rather than the exposed (erodible) ground area S' . The difference $S-S'$ is the total basal area of the roughness elements on S . The stress per unit exposed ground area τ'_S is

$$\tau'_S = (S/S')\tau_S = \frac{\tau_S}{1-\sigma_L} \quad (\text{Eq. 6})$$

where σ is the ratio of roughness-element basal area to frontal area, so that $\sigma L = 1 - S'/S$ is the basal area index (basal area per unit ground area). Following Raupach et al. (1993), the stress partition between the roughness elements and the substrate surface can be derived from any of the shear stress ratios τ_R/τ , τ_S/τ or τ'_S/τ . Using Marshall's data, the first two shear stress ratios can be obtained directly from the measurements. In contrast, the third shear stress ratio is dependent on the inverse of the basal area index which includes L . This ratio was adopted by Raupach et al. (1993) to describe the drag partition:

$$R_t = \sqrt{\tau'_S/\tau}. \quad (\text{Eq. 7})$$

If τ'_S is calculated with the fixed and incorrect L_{45} then it will not include any interactions between roughness elements and wakes in the drag partition (Figure 2; black diamonds). The values of L_{45} occur mainly $0.0001 < L_{45} < 0.1$. However, when τ'_S is calculated using L_α , the sheltering is an order of magnitude larger than L_{45} (mainly $0.01 < L_\alpha < 1$) and the interactions and therefore the impact of roughness configuration are evident in the broader scatter and values $0 > R_t > 1$ (white square symbols; Figure 2). In other words, all previous wind erosion estimates made using L_{45} are likely to either have been over-estimated (or tuned inappropriately against measurements to achieve the correct sediment flux).

184

Figure 2. Marshall's (1971) wind tunnel measurements used to calculate lateral cover (L_{45} and L_α) and plotted against the drag partition R_t^2 (so that $R_t \leq 0$ can be included) to illustrate the previously hidden effect of roughness configuration.

The influence of roughness element configuration on the drag partition e.g., regular grid, staggered, random or clumped (e.g., Marshall, 1971; Minvielle et al., 2003; Raupach et al., 2006) is masked by the use of L_{45} . Equation 1-2 is invalid when $L_\alpha \gg 1$ because when inverted in the basal area index, negative τ'_S are produced (Figure 2). Equation 2 is only valid if the length of the sheltered area is truncated by the downstream roughness elements. That is, the length of $A \leq$ roughness element spacing. Consequently, it appears from these results that historically L_{45} has been chosen to ensure that these truncations occur when the spacing of roughness elements in the wind tunnel is less than or equal to the height of the roughness elements (used in Marshall's experiments). These truncations (representing wake interactions) between roughness elements cannot be expressed by the simple

196 geometric formulation of L_α . A finding consistent with Raupach's (1992) scepticism that the model of L_{45} could
197 describe adequately the highly three-dimensional flow amongst roughness elements. We therefore propose that
198 lateral cover (L_{45} or L_α) should be replaced by an alternative, appropriate approach which we describe in the next
199 section.

200 Okin (2008) avoided the use of L by extending Raupach's (1992) approach to develop a drag decay function over
201 space, dependent on information about the separation between roughness elements. This approach provides the
202 opportunity to include the spatial variation of drag, and the potential to better represent the area-integrated
203 (areal) transport (Webb et al. 2014). To parameterise the model, ground-based measurements of roughness
204 distribution and height are made relatively easily at the plot scale or for small (10 m²) areas. However, these data
205 can become prohibitively expensive to acquire when sampling is required to adequately represent spatial
206 variability particularly over large regions. Collection of these data is therefore often not feasible at broad
207 (regional) scales and requires approximations using remote sensing or other ancillary or indirect information
208 similar to those of L , to parameterise the model.

209 3. Using shadow to approximate sheltered area interactions and aerodynamic properties

210 Chappell and Heritage (2007) introduced the notion of using shadow to approximate sheltered areas and
211 aerodynamic turbulence primarily because of the need to make estimates of sediment transport for
212 heterogeneous roughness across spatial scales (e.g., Marticorena and Bergametti, 1995; Alfaro and Gomez, 1995;
213 Shao, 2001). Chappell and Heritage (2007) were concerned with the anisotropic nature of the aerodynamic
214 turbulence which, for a heterogeneous surface, must be different for different wind directions (Figure 1b). For a
215 given number and object geometry, the L_{45} or L_α will be the same but the sheltered area, and shear stress
216 partition, may be quite different. Chappell and Heritage (2007) questioned whether models tested against
217 roughness lengths measured from field wind velocity profiles are indeed valid and suggested that there was a
218 need for a method to independently predict the directional aerodynamic turbulence characteristics across scales.
219 Following Arya (1975) and Raupach (1992), they suggested that the length of a sheltered area behind an isolated
220 obstacle was a function of wind velocity (at a reference height) and roughness element height. Chappell and
221 Heritage (2007) calculated the sheltered area as shadow by invoking relative roughness (common in fluvial
222 hydrology) to approximate the illumination angle. They showed a relation between shadow and wind tunnel
223 estimates of aerodynamic roughness length obtained by Dong et al. (2002).

224 Chappell et al. (2010) reconstructed the configurations of hemispheroids used to represent surface roughness in
225 the wind tunnel study of Dong et al. (2002) and then illuminated the surfaces for a range of zenith angles (for a
226 given azimuth angle). The approach of Chappell et al. (2010) has a similar physical basis to that described by
227 Raupach (1992). Instead of calculating the projection of the frontal area from its side the same calculation is made
228 from above and can use the projection angle α (Raupach, 1992; Figure 1b). Shadow is sensitive to configuration of
229 roughness objects. In other words, the proportion of shadow will depend on the proximity of objects to each
230 other, their height, width, and the direction of the illumination (continuing the analogy with wind direction).

231 Following the approach of Chappell et al. (2010), here we reconstructed Marshall's (1971) wind tunnel
232 experiments of regular cylinders using digital elevation models of hemispheroids and illuminated each surface
233 across a range of zenith angles (0-90°). The hemispheroids were used in place of cylinders, the bluff wall of which
234 created an artefact unlikely to be found in reality (Chappell and Heritage, 2007). The ray-casting for a range of
235 illumination angles was viewed at nadir and integrated to approximate the direct beam directional hemispherical
236 reflectance (or black sky albedo ω). We used the inverse to reveal the shadow ($1-\omega$) and normalised by the black
237 sky albedo of the surface when illuminated and viewed at nadir ($\omega_n = (1 - \omega)/\omega_0$). This normalisation approach
238 removed the influence of spectral reflectance on the results. We also calculated $\omega_{n45}=(1-\omega_{45})/\omega_0$ to represent the
239 projection at 45°, $\omega_{n\alpha}=(1-\omega_\alpha)/\omega_0$ to represent the projection at $\alpha=U_h/u^*$ and $\omega_{n87}=(1-\omega_{87})/\omega_0$ to represent the
240 projection of α but at a fixed angle of 87°. There is so little variation in α across the large range of Marshall's
241 roughness surfaces that ω_{n87} provided a precise approximation of $\omega_{n\alpha}$. We also found that both measures (ω_{n87}
242 and $\omega_{n\alpha}$) were similar to, but had less variability than, the integration ω_n . The ω_{n45} was the worst approximation.

243 An arising implication which we elaborate in the final section is that future studies (e.g., wind tunnel and field
 244 work) can make use of the straightforward relation between illumination angle and at-nadir viewing to
 245 approximate the aerodynamic properties. The ω_n provided a measure which adequately represented projections
 246 at α and produced the least variation when plotted against the key aerodynamic properties used in wind erosion
 247 and dust emission models. It was adopted here because of the relative ease with which it can be replicated by
 248 available MODIS products. It was rescaled (ω_{ns}) from the normalised range ($\omega_{nmin}, \omega_{nmax}$ of a given waveband v)
 249 to that of the calibration data ($a=0$ to $b=1$) using the following equation:

$$250 \quad \omega_{ns} = \frac{(a-b)(\omega_n(v) - \omega_n(v)_{max})}{(\omega_n(v)_{min} - \omega_n(v)_{max})} + b. \quad (\text{Eq. 8})$$

251 The relations with the aerodynamic properties are shown in Figure 3.

252 Although above we recommended avoiding the use of L_{45} in modelling wind erosion, we provide it here for
 253 completeness. There is a strong positive relation between ω_{ns} and L_{45} . When L is large the proportion of shadow
 254 is large and as L decreases so ω_{ns} decreases. The L_{45} has values which are only slightly larger than those of ω_{ns} .
 255 This small difference is caused by the shadow overlapping part of the downstream roughness elements. The L_{45}
 256 has a fixed angle which is designed so that the predicted shelter areas do not interact with the downstream
 257 roughness elements even when the spacing between roughness elements is very small (i.e. minimum spacing is
 258 set to roughness element height). Even though L_{45} is not projected at the correct angle α it provides a reasonable
 259 approximation of the sheltered area when roughness elements (with the same geometry) are regularly spaced as
 260 with Marshall's experiments. However, as shown above (Figure 2) L_{45} masks the effect of configuration.

263 **Figure 3.** The relations between key aerodynamic properties used in wind erosion and dust emission models and
 264 normalised albedo (proportion of shadow). We illuminated each of Marshall's (1971) surfaces across the range of

zenith angles to approximate the direct beam directional hemispherical albedo (or black sky albedo ω ; viewed at nadir). We normalised ω by the reflectance of the surface, illuminated and viewed at nadir (ω_0), to remove any spectral influences, used the inverse to reveal the shadow $\omega_n=(1-\omega)/\omega_0$ and then rescaled (ω_{ns}). The key aerodynamic properties include (a) the lateral cover; (b) the drag partition (R_t) derived from Marshall's (1971) data; (c) the wind shear stress scaled by the velocity at a freestream height (u^*/U_f); (d) aerodynamic roughness length scaled by the roughness height (z_0/h). Equations of the curves fitted to the data used in b, c and d are provided in the formula in section 4. Note that the cluster of data omitted by Raupach et al. (1993) in their analysis has also been omitted in our analysis.

When we consider the drag partition (R_t) calculated from Marshall's (1971) data using equation 1-2 with L_{45} there is a strong relation with ω_{ns} (Figure 3b). This is to be expected because of the strong relation between L_{45} and ω_{ns} . Moreover, it suggests that R_t can be estimated directly using the shadow at the (land) surface. We showed that L_{45} is incorrect but when R_t is calculated using the best approximation L_α (Eq. 1) R_t cannot be modelled well (Figure 2). Instead we calculated R_t using albedo since the exposed area is equivalent to ω_{ns} and its inverse $1 - \omega_{ns}$ is shadow. This enables calculation of the surface shear stress following:

$$\tau'_S = (S/S')\tau_S = \frac{\tau_S}{1-\omega_{ns}}. \quad (\text{Eq. 9})$$

We used these new shadow-based estimates of τ'_S for Marshall's study to calculate R_t following Eq. 9. We then plotted the albedo-derived R_t on Figure 3b. Notably, for intermediate and dense roughness (large ω_{ns} equivalent to $L_{45}>0.001$) the values of R_t calculated using shadow are slightly smaller than those calculated using L_{45} . This is because the shadow is correctly representing the larger sheltered area than that estimated using L_{45} . Although subtle when plotted in this way, the difference in the values represents the previously hidden influence of roughness configuration on R_t . The impact is negligible at very small roughness density because the sheltered area is a very small proportion of the total erodible area. Similarly, at very large roughness density the impact is negligible because there is little space between the roughness elements. The model displayed (solid line) was fitted to the R_t values calculated using shadow (Eq. 4) using a Levenburg-Marquardt non-linear optimisation (RMSE=0.05839).

There is a strong relation between ω_{ns} and the measured shear stresses (total u_{T*} , objects u_{R*} , surface u_{S*} and erodible surface $u_{S'*}$) scaled by the freestream velocity U_f (Figure 3c) and between ω_{ns} and the calculated aerodynamic roughness length scaled by roughness element height (z_0/h ; Figure 3d). In both cases this strong relation is to be expected because of the strong relation between L_{45} and ω_{ns} and provides the first indication of redundancy in information content which we exploit below. The displayed models (solid lines) were fitted to the data using the same as previous non-linear optimisation (RMSE= 0.0027 and 0.0064, respectively). These data show little evidence of the expected reduction in shear stress at large ω_{ns} (in either z_0/h or u^*/U_f) due to skimming flow. For consistency with the observations we fitted models which did not include a reduction in shear stress when $\omega_{ns}>0.1$. We also established relations between ω_{ns} and the shear stresses and between ω_{ns} and aerodynamic roughness for objects (u_{R*} and z_{0R}/h) and surface (u_{S*} and z_{0S}/h) scaled by the freestream velocity (U_f) and height respectively. There are two notable findings: (1) erodible surface shear stress ($u_{S'*}$) did not differ from that of the surface shear stress (u_{S*}) when scaled by U_f (differences were evident when not scaled by U_f); (2) surface aerodynamic roughness decreases as lateral cover increases which indicates that the smooth aerodynamic roughness length (z_{0s}) is not fixed and constant everywhere as assumed by Marticorena and Bergammetti (1995).

4. Using shadow to reformulate wind erosion modelling

4.1 Reducing the complexity and retaining fidelity of sediment transport

Our analyses in Section 3 reveal a direct relation between shadow (ω_{ns}) and the key aerodynamic properties used in wind erosion and dust emission schemes. The implication here is that such schemes can be simplified without losing any information content and thereby parameterised more effectively. We illustrate this improvement using

the scheme of Shao et al. (2004) where the horizontal (saltation mass) flux Q_h for uniform particles of size D is calculated as:

$$Q_h(U_f, u_{T*}, z_0, D, L_{45}, w) = c_{shao} \frac{\rho_a u_{T*}^3}{g} \left(1 - \left(\frac{u_{*t}}{u_{T*}}\right)^2\right). \quad (\text{Eq. 10})$$

The parameter c_{shao} in Owen's (1964) original formulation was found empirically and in typical situations (e.g., soil grain size $D=150 \mu\text{m}$; $u_* = 0.8 \text{ m s}^{-1}$) c_{shao} is around 0.8 (Shao et al., 1997), ρ_a is the air density (kg m^{-3}), u_{s*} is the surface friction velocity (m s^{-1}), g is acceleration due to gravity (m s^{-2}) and u_{*t} the threshold friction velocity. In theory u_{s*} should be used, but in practice it is not available. Instead u_{T*} is either obtained from an external source such as numerical weather prediction models or similar based on an estimate of the aerodynamic roughness length z_0 . The u_{T*} should be converted to u_{s*} using R_t

$$u_{T*} = u_{s*} / R_t \quad (\text{Eq. 11})$$

but in practice this may not occur. We show later in this section, the consequences of using u_{T*} instead of the correct values of u_{s*} . Here the u_{T*} scaled by the freestream velocity (U_f ; m s^{-1})

$$\frac{U_f}{u_{T*}}(z_0, L_{45}) = \frac{1}{k} \ln\left(\frac{del}{z_0}\right), \quad (\text{Eq. 12})$$

is estimated using von Kármán's constant (k), del the approximation of boundary layer depth provided by Wooding et al. (1973; p. 295) for use with Marshall's data and roughness height h and breadth b .

$$del(L_{45}) = 3.3 + 15(L_{45}(\frac{h}{b})^{0.38})^{0.43}. \quad (\text{Eq. 13})$$

We estimated z_0 scaled by h using the empirical relation with L_{45} suggested by Marticorena et al., (1997) and updated by Marticorena et al. (2006)

$$\log\left(\frac{z_0}{h}\right) = \begin{cases} 1.31 \log(L_{45}) + 0.66 & L_{45} < 0.045 \\ -1.16 & L_{45} \geq 0.045 \end{cases}. \quad (\text{Eq. 14})$$

The u_{*t} is calculated as the bare soil threshold friction velocity $u_{*ts}(D)$ adjusted by the Raupach et al. (1993) drag partition correction $R_t(L_{45})$ and soil moisture (w) via the function $H(w)$

$$u_{*t}(D, L_{45}, w) = \frac{u_{*ts}(D)H(w)}{R_t(L_{45})}. \quad (\text{Eq. 15})$$

The u_{*ts} of a given D includes A_N a scaling coefficient, ρ_p is the particle density (kg m^{-3}), g acceleration due to gravity (m s^{-2}), Γ is a parameter accounting for the cohesive force (kg s^{-2})

$$u_{*ts}(D) = \left(A_N \left(\frac{\rho_p g D}{\rho_a} + \frac{\Gamma}{\rho_a D} \right) \right)^{-0.5}. \quad (\text{Eq. 16})$$

The $R_t(L_{45})$ includes parameters for the σ_v the ratio of vegetation roughness element basal area to frontal area, m_v accounts for the non-uniformity of the surface stress, β_v is the ratio of vegetation roughness element to surface drag coefficients (Raupach et al., 1993)

$$R_t(L_{45}) = (1 - \sigma_v m_v L_{45})^{-0.5} (1 + m_v \beta_v L_{45})^{-0.5}. \quad (\text{Eq. 17})$$

A straightforward function H (dimensionless) was proposed by Shao et al., (1997) to account for the volumetric soil moisture content w ($\text{m}^3 \text{m}^{-3}$)

$$H(w) = e^{22.7w} \quad w \leq 0.03. \quad (\text{Eq. 18})$$

Details of this scheme and its similarity with the other commonly used scheme of Marticorena and Bergametti (1995) can be found in Darmonova et al. (2010). The estimate of the total shear stress u_{T*} requires information about the freestream wind velocity (U_f) and the aerodynamic roughness length (which itself requires information

on its scaling height z_0/h). Often, u_{T*} is established independently in an atmospheric model and with no connection to the aerodynamic roughness used in the wind erosion scheme. Here we estimated z_0/h and then estimated u_{T*}/U_f accordingly.

We reduce the number of parameters in the above scheme by using the common relation with ω_{ns} and thereby establish consistency between the aerodynamic properties and avoid disconnecting u_{T*} from z_0/h . Furthermore, we avoid the need for z_0/h and use the model parameters (assuming they too are fixed) of the relation between u_{T*}/U_f and ω_{ns}

$$\frac{u_{T*}}{U_f}(\omega_{ns}) = 0.0497 \left(1 - \frac{e^{-\omega_{ns}^{1.326}}}{0.0027} \right) + 0.038. \quad (\text{Eq. 19})$$

Perhaps most importantly, the drag partition scheme of Raupach et al. (1993), with its difficult to estimate parameters and reliance on the erroneous values of L_{45} , can be replaced with the relation between R_t and ω_{ns} and constants to represent all scales of the drag partition

$$R_t(\omega_{ns}) = 0.9516 \left(\frac{e^{-\omega_{ns}^{1.1869}}}{0.0039} \right) + 0.048. \quad (\text{Eq. 20})$$

This means that u_{*t} is no longer a function of L_{45} and instead is a function of ω_{ns}

$$u_{*t}(D, \omega_{ns}, w) = \frac{u_{*ts}(D)H(w)}{R_t(\omega_{ns})}, \quad (\text{Eq. 21})$$

which we show in the next section makes an important difference to the estimates of Q_h .

The complexity of the model may be reduced still further by estimating Q_h

$$Q_h(U_f, D, \omega_{ns}, w) = c_{shao} \frac{\rho_a u_{S*}^3}{g} \left(1 - \left(\frac{u_{*ts}H(w)}{u_{S*}} \right)^2 \right), \quad (\text{Eq. 23})$$

simplifying

$$\frac{u_{*t}}{u_{T*}} = \frac{u_{*ts}H(w)/R_t}{u_{S*}/R_t} = \frac{u_{*ts}H(w)}{u_{S*}}, \quad (\text{Eq. 24})$$

estimating directly the shear stress at the soil surface (u_{S*})

$$\frac{u_{S*}}{U_f} = 0.0311 \left(\frac{e^{-\omega_{ns}^{1.131}}}{0.016} \right) + 0.007, \quad (\text{Eq. 25})$$

and the bare soil threshold friction velocity (u_{*ts}) as before.

This last reduced complexity (shadow) model (Eqs. 23-25) no longer requires the threshold friction velocity u_{*t} and thereby the Raupach et al. (1993) drag partition R_t (L_{45}) (Eq 17) is also not used. Conceptually, this model is consistent with that employed by Okin (2008) and Webb et al. (2014).

4.2 The significance of using surface shear stress in sediment transport modelling

We calculated horizontal flux (Q_h) using u_{T*} and u_{S*} separately in three different ways using: (1) Marshall's (1971) aerodynamic measurements; (2) the traditional approach following Shao (2004) and (3) the shadow-based approach. For the purpose of illustration, we followed the approach of Darmanova et al. (2010) and used values they suggested for the roughness parameters in the Raupach et al. (1993) drag partition scheme ($\beta_v = 202$; $\sigma_v = 1.45$; $m_v = 0.16$; model 1). For simplicity, the values of the other parameters were fixed in the three approaches including setting $U_f = 20.3 \text{ m s}^{-1}$, $D = 63 \text{ }\mu\text{m}$, $A_N = 0.0123$, $\rho_p = 2650 \text{ kg m}^{-3}$, $c_{shao} = 1$, $\rho_a = 1.23 \text{ kg m}^{-3}$, $g = 9.81 \text{ m s}^{-2}$, $\Gamma = 1.65 \times 10^{-4} \text{ kg s}^{-2}$, $H(w) = 1$. For simplicity (in equation 13) we set $h = 0.0254 \text{ m}$ to the height of the roughness elements in Marshall's (1971) experiments and $b = 0.05 \text{ m}$ which was the average breadth of the roughness elements used. Setting these parameters to the values of Marshall's data ensured that the range of horizontal mass flux using L_{45} was similar to that produced using ω_{ns} .

Figure 4a shows the potential fluxes (circles) using u_{T^*} . At very sparse roughness the flux based on Marshall's experiments is predicted at around $0.05 \text{ g m}^{-1} \text{ s}^{-1}$ and as roughness increases the flux increases at an accelerating rate and reaches a maximum flux around $L_{45}=0.05$ before decreasing sharply to $0 \text{ g m}^{-1} \text{ s}^{-1}$. The model based on L_{45} (dashed line) shows flux increasing rapidly as lateral cover increases and then decreases slowly. The shadow-based model (solid line) passes through the symbols (is not fitted), reaches a maximum at an L_{45} similar to the flux based on Marshall's experiments and decreases rapidly.

Figure 4b shows predicted fluxes and models using u_{S^*} . At very sparse roughness there is little difference in flux estimated using either u_{T^*} (Figure 4a) or u_{S^*} . However, as lateral cover increases flux calculated using Marshall's measurements decreases (circles). The model based on shadow passes through the symbols (not fitted). By comparison with the maximum flux in figure 4a modelled sediment flux is ten times smaller using u_{S^*} . The model based on L_{45} (model 1) shows flux at around 2.5 times larger than the shadow model and describes increasing flux as lateral cover increases. We replaced the values of the Raupach drag partition parameters (model 1) with those described in Raupach et al. (1993; $\beta_v = 170$; $\sigma_v = 2$; $m_v = 1$; model 2). The sediment flux reduced and was similar to that of the shadow model. The difference in Raupach drag partition model parameter values evidently explained most of the deviation from sediment flux using Marshall's data and the shadow model. The remaining variance was due to approximations in z_0/h to obtain u_{T^*} (Eqs. 12-14).

(a)

(b)

Figure 4. Horizontal flux estimated using the model of Shao et al. (2004) with the aerodynamic measurements from Marshall's experiments (circles), the traditional lateral cover (L_{45}) and the new approach using shadow (ω_{ns}) with u_{T^*} (a) and u_{S^*} (b) plotted against flux. The flux model based on L_{45} used Raupach (1992) drag partition parameters fixed at $\beta_v = 202$; $\sigma_v = 1.45$; $m_v = 0.16$ (model 1) following Dargavva et al. (2010) and fixed at

403 $\beta_v = 170$; $\sigma_v = 2$; $m_v = 1$ (model 2) following Raupach et al. (1993). The shadow model used the previously
 404 described calibrations with ω_{ns} to estimate flux.

405 Using u_{T^*} in these calculations of flux implies that sparse vegetation cover promotes flux to such an extent that it
 406 is larger than under bare conditions. However, flux decreases exponentially using u_{S^*} as L_{45} (or ω_{ns}) increases.
 407 Notably, between the two approaches there is no difference in the values of the terms $(u_{*t}/u_{T^*})^2$ or $(u_{*ts}/u_{S^*})^2$ used
 408 in Q_h . The absence of difference demonstrates that the drag partition is working correctly when using measured
 409 shear stress or when using the drag partition scheme which closely approximates that of Marshall's R_t data. These
 410 findings instead suggest that when the drag partition is correct, previous studies which used u_{T^*} within a rough
 411 canopy (e.g., wind velocity profile in a vegetated area) have considerably over-estimated flux (also demonstrated
 412 by Webb et al., 2014). However, outside a rough canopy (e.g., over sand on dunes) $u_{S^*} \approx u_{T^*}$ and hence the use of
 413 u_{T^*} in the transport equation will be adequate for estimating the correct flux. We return to these implications in
 414 the final section. Similarly, these findings show that when an incorrect estimate of the wind friction velocity is
 415 used with a drag partition scheme, the flux may be considerably over-estimated. Given the sensitivity of the
 416 results to either adjustments of u_{T^*} or to the vagaries of the correct parameterisation of R_t , it seems prudent to
 417 avoid these terms completely by using the shadow model (Eqs. 23-25).

418 4.3 A empirical albedo-based sediment transport model

419 Notably, when we changed particle size $50 \mu\text{m} < D < 500 \mu\text{m}$ (keeping ρ_p constant) in the previous experiments
 420 with u_{S^*} (Figure 4b) we found that there was almost no difference in flux using either L_{45} or shadow. We
 421 investigated the shadow model for different U_f and D and found that the flux estimates were sensitive mainly to
 422 U_f . Consequently, we tried to model flux using ω_{ns} and U_f . We used the same as previous Levenberg–Marquardt
 423 non-linear optimisation to fit (RMSE=0.0088 g m⁻¹ s⁻¹) the following exponential model based on ω_{ns} to the flux
 424 calculated from Marshall's data (Figure 5)

$$425 \quad Q_h(D) = m \left(\exp\left(-\frac{\omega_{ns}^{1.48}}{p}\right) \right), \quad (\text{Eq. 27})$$

$$426 \quad \text{where } m = 0.00044U_f^2 - 0.0091U_f + 0.0476 \text{ and} \quad (\text{Eq. 28})$$

$$427 \quad p = 0.0001U_f^{0.85}. \quad (\text{Eq. 29})$$

428 The magnitude parameter m varied with U_f and was fitted best by a quadratic polynomial ($R^2=0.93$) and the shape
 429 parameter p varied with U_f and was fitted best ($R^2=0.99$) with a power function. The power used to raise ω_{ns} was
 430 fixed at the constant 1.48. The implication of this modelling is that horizontal mass flux requires only precise
 431 estimates of ω_{ns} and U_f , and that u_{*t} is not required. We will discuss these implications in the final section. Note
 432 the discrepancy in calculated flux at large values (small ω_{ns}).

Figure 5. Horizontal flux estimated using the scheme of Shao et al. (1996) with the aerodynamic measurements from Marshall's experiments (circles), the new approach using the shadow model (solid line) and the empirical model based on U_f (Equation 8).

The flux predicted using Marshall's experiments was based on measured u_* and did not include L_{45} . The variability in fluxes for a given lateral cover (or ω_{ns}) therefore cannot be attributed to the influence of roughness configuration unless it is inherent in the measurements. The variability in predicted fluxes is most likely explained by the precision of the wind tunnel experiments (measurements, wind speed variation etc.) and the use of squared and cubed terms in the transport equation. Consequently, the scatter provides the uncertainty (average RMSE=0.0088 g m⁻¹ s⁻¹ for the current simulations) and the most likely limit of detectable change in area-integrated (areal) sediment flux over space and time. It is very unlikely that a similarly small uncertainty in areal flux could be obtained in current field measurements, particularly those measured at one or even few locations within a given area. We discuss the implications of this finding in the final section. In the next section we show how the direct calibrations of ω_{ns} with aerodynamic properties improve the estimation of wind erosion and how the aerodynamic properties can be estimated across scales of variation using ω_{ns} .

5. Using shadow to estimate wind erosion across scales of variation

5.1 Retrieving aerodynamic properties across scales of variation

The ω_{ns} can be retrieved directly over an area, across a range of scales (mm to km) because when albedo is integrated across scales it is linearly additive. Albedo is available from a range of extant approaches and platforms e.g., wind tunnel or field measurements from pyranometers and model estimates from angular reflectance on aircraft or satellites. Of perhaps the greatest opportunity and that which is illustrated here, is to use albedo products from NASA's Moderate Resolution Imaging Spectroradiometer (MODIS). The global nature of the MODIS albedo product (MCD43A1), its moderate resolution in space (500 m) and time (8 days) and data archive from the year 2000-present, enables a >15-year database of ω_{ns} from which the key aerodynamic properties can be estimated for modelling, mapping and monitoring of global wind erosion, investigating the impact of global land management and for constraining Land Surface Models, amongst other applications.

The operational MODIS bi-directional reflectance distribution function (BRDF) albedo algorithm makes use of a kernel-driven linear BRDF model, which relies on the weighted sum of an isotropic weighting parameter (f_{iso} ; dimensionless) and two functions (or kernels) with parameters of viewing and illumination geometry (Roujean et al., 1992). The parameter f_{iso} represents the spectral contribution. The kernel weights that best fit the majority situation are selected (Lucht et al., 2000; Schaaf et al., 2002) and used to produce the at-nadir BRDF-adjusted reflectance (NBAR) product (MCD43A4). Once an appropriate BRDF model has been retrieved, integration over all

view angles results in a directional–hemispherical ‘black-sky’ albedo called the direct beam (*dir*). It is a spectral-dependent (v) direct beam albedo $\omega_{dir}(\theta, v)$ and a function of solar zenith angle θ in the absence of a diffuse component. For a given waveband v we assume that the MODIS $\omega_{dir}(0^\circ, v)$ and integration of view angle information was reciprocal to our ray-casting model which uses at-nadir view angle and integrates illumination angle information. The shadow is the inverse $1 - \omega_{dir}(0^\circ, v)$ and we removed the spectral influence by normalising it with f_{iso} :

$$\omega_n = \frac{1 - \omega_{dir}(\theta, v)}{f_{iso}(v)} = \frac{\omega_{dir}(\theta)}{f_{iso}} \quad (\text{Eq. 30})$$

We found that there is little difference in ω_n between MODIS bands and adopted MODIS band 1 (*B1*). To enable the MODIS ω_n to predict the aerodynamic properties we needed to make it consistent with the calibration relations established from the ray-casting and Marshall’s (1971) wind tunnel. So we translated and scaled the data (ω_{ns}) using Eq. 8.

We processed the current MODIS (MCD43A1) global archive to estimate $\omega_{ns}(f_{iso}, v_{B1})$ and to predict aerodynamic properties following the approach outlined above. We illustrate the information content of these aerodynamic properties by displaying maps of the spatial variation of the aerodynamic properties (Figure 6). Firstly, we noted that the maps contained almost identical information (for the selected day). This redundancy is consistent with the reduced complexity we demonstrated in the calculation of mass flux (Eqs. 23-25). Regardless of property, there is a clear distinction between those areas which have small aerodynamic roughness (at 500 m pixel scale) and thereby are most susceptible to mass flux, and those which are not. The regions with e.g., the smallest u_{s*}/U_f are in the highest latitudes where the land surface is covered in snow and ice. Regions with the smallest aerodynamic roughness uncovered by snow and ice are in a mega-region which extends across North Africa, the Arabian Peninsula, across Persia, and into northern western China and Mongolia. This mega-region is ‘Barren or Sparsely Vegetated’ following the MODIS global land cover classification. Regions which have slightly larger aerodynamic roughness include most of Australia, the southern and eastern countries in Africa, most of Argentina and northern Chile, coastal Peru, northern Mexico, western USA and southern Canada. These regions are associated with the MODIS land cover class ‘Open Shrublands’. Furthermore, many parts of Europe include small aerodynamic roughness e.g., southern Portugal, most of Spain, Turkey, northern France, western Germany, south-eastern UK and Iceland. These regions are classified as either Cropland or Grassland. Many of these regions have well documented wind erosion (Goossens et al., 2001). However, the prevailing thinking is that wind erosion is caused by the regions’ erodibility i.e., silt- and sand-sized material available for transport (e.g., EU project Wind Erosion on European Light Soils: WEELS). We know that particle size may have very little influence on horizontal mass flux. Our results therefore demonstrate that the main influences on horizontal mass flux in these regions is their small aerodynamic roughness (notwithstanding the influence of free stream wind velocity and soil moisture). There is much similarity in the aerodynamic roughness of these European regions despite cutting across considerable differences in soil type and specifically soil colour. The similarity in the aerodynamic roughness provides additional confirmation that the normalisation by f_{iso} has successfully removed the influence of spectral information.

Figure 6. Maps of (a) lateral cover (L_{45}), (b) aerodynamic roughness length scaled by surface height (z_0/h), (c) surface friction velocity scaled by freestream wind velocity (u_{*}/U_f) and (d) drag partition (R_t) from MODIS (MCD43A1; 22 September 2009) using the established methodology.

5.2 Exposing the limitations of L_{45} in sediment transport modelling

To illustrate the ability of the shadow-based approach for estimating sediment flux across scales of variation, we selected 33 pixels (500 m) from across the main agro-ecological systems in Australia to model wind erosion and to subsequently monitor (every 8 days) wind erosion 2000-present. Some of these pixels are located in highly vegetated (tropical and temperate) regions where little or no wind erosion occurs. We selected four of the available 33 pixels for detailed spatial and temporal analysis (Figure 7).

Figure 7. Locations of 500 m pixels in Australia chosen to consider change over time. We focused on a desert site with little ground cover and loose sand (Simpson, Northern Territory), a cultivated site covered with a crop until harvest and then grazed by sheep (Anameka, Western Australia), a site in a mainly dry playa (Lake Eyre, South Australia) and another cultivated site in the Mallee region where wind erosion occurs frequently (Merrinee, New South Wales). The inset images are approximately 1.5 km² to illustrate the heterogeneity in land surface erodibility that occurs between 500 m pixels.

For the entire period (ca 25,000 days) we retrieved the aerodynamic properties from MODIS (MCD43A1) and estimated the horizontal mass flux using the Shao scheme based on (i) L_{45} (Eqs. 10-18) and (ii) ω_{ns} (Eqs. 23-25). The bare soil threshold friction velocity (u_{*ts}) was common to both approaches and was fixed over space and time. We ensured u_{*s} was used in the former approach where u_{T*} was estimated from z_0/h by adjusting it using R_t . To ensure compatibility between the two approaches we replaced the parameter values used by Darnenova et al. (2010) for Raupach's drag partition scheme, with those fixed at $\beta_v = 170$; $\sigma_v = 2$; $m_v = 1$ (model 2) following Raupach et al. (1993).

In the first approach we estimated lateral cover following Shao (2004; CL_{45}) using the relation:

$$CL_{45} = -c \ln(1 - a_c) \quad (\text{Eq. 31})$$

where c is an empirical coefficient which represents the shape of the vegetation type and a_c is the cover fraction and may be represented using photosynthetic cover. In the Shao scheme the parameter $c = 0.35$ was determined empirically from a field in Australia with a crop stubble (Shao et al., 1996). In practice, this parameter value is kept constant in the absence of any other information about vegetation type (Darnenova et al., 2010). We calculated CL_{45} from Marshall's data and plotted it against L_{45} (Figure 8). We assumed that values of L_{45} were correct for CL_{45} and inverted Eq. 31 to estimate variable c . The results show that CL_{45} estimated by keeping the shape coefficient fixed (symbols), is a reasonable approximation (with bias) of a varying shape coefficient (thick line).

Figure 8. Lateral cover (L_{45}) of Marshall's (1971) roughness configurations against L estimated using fractional cover.

In our calculation of flux we estimated a_c using only the photosynthetic fraction of vegetation. When a_c was 0, we set a lower limit of $L_{45}=0.0001$.

Figure 9a shows that there is some similarity in the horizontal mass flux between the two approaches. However, across the range of flux estimated by the shadow model there is a limited range of flux estimated by the model based on L_{45} . The horizontal lines of symbols are artefacts of the discontinuities and lack of resolution which exist in the fractional cover data used in Eq. 31 and the bias we described in Figure 8. To elucidate the sources of difference between the flux estimates we plotted L_{45} against flux estimated using the L -based approach and the shadow-based approach (Figure 9b). The pattern of flux predicted using shadow was similar to that of the flux calculations based on Marshall's aerodynamic measurements (Figure 5). This is to be expected since there is an almost 1:1 relation between L_{45} and ω_{ns} . However, using the L -based approach the majority of values exceeded $L_{45}=0.1$ and the magnitude of L_{45} was larger than the shadow model. In contrast, the shadow-based model had the majority of values between $0.001 < L_{45} < 0.1$.

In the L -based model the estimates of L_{45} have a strong influence on flux because they are used to estimate z_0/h and u^* . To determine the extent to which L_{45} was causing the difference in horizontal flux (under the given simulation conditions), we replaced it with estimates of L_{45} using ω_{ns} . This replacement removed the dependency of L_{45} on fractional cover estimates and a relation emerged between the flux estimates (Figure 9c). The discontinuity in the flux estimates is due to the piecewise model of z_0/h (Eq. 14). These differences may be even larger in practice when the wind friction velocity (u^*) is obtained from an atmospheric model, with roughness separate (disconnected) from the wind erosion scheme. We plotted L_{45} against flux and although little changed in the magnitude the distribution of data were similar. We proceeded to replace the other aerodynamic model parameters (R_t , z_0/h and u_{T^*}) in the same manner. The changes to flux were very minor and are not shown here. A final replacement of u_{T^*} confirmed that the models were performing as expected because the fluxes for each approach matched exactly and the plot of L_{45} against flux showed flux which coincided exactly for both models.

Figure 9. Horizontal flux estimated using the model of Shao et al. (2004) with the traditional lateral cover (L_{45}) and the new approach using shadow (ω_{ns}). The Raupach drag partition model parameters were fixed at $\beta_v = 170$; $\sigma_v = 2$; $m_v = 1$ following Raupach et al. (1993). For simplicity, we assumed that at all pixels (500 m) and all times the freestream velocity $U_f = 20.3 \text{ m s}^{-1}$ and the particle size was $63 \mu\text{m}$. We estimated flux using CL_{45} and ω_{ns} , and compared the differences (a). To isolate the major causes of difference in the model we replaced L_{45} with that predicted using ω_{ns} (b) which removed most of the noise (c) and demonstrated that most of the remaining difference in flux was small (d) and due to small differences in the aerodynamic properties between the two approaches.

5.3 Estimating sediment transport across scales of variation

To demonstrate how this albedo-based approach can be used for wind erosion monitoring, we made estimates of Q_h (every 8 days) over time (2000-2015) for selected pixels in Australia (Figure 7). These estimates of Q_h are made under the same simulated conditions as above and in the previous section and are used here to illustrate the potential Q_h averaged monthly (Figure 10a), summed monthly (Figure 10b), averaged annually (Figure 10c) and summed annually (Figure 10d). The largest average monthly flux was produced at the 500 m pixel or site chosen in Lake Eyre (Figure 7). Similar amounts of average monthly flux was produced consistently over the year at that pixel and also in the Simpson Desert dunes. Flux at the field near Merrinee in the sandy cropping region of New South Wales (NSW) Mallee, and at the sandy agricultural (wheat-sheep) field near Anameka in Western Australia (WA), showed a distinct management practice related decline in flux during the southern hemisphere winter-spring. The monthly total flux showed a slightly different pattern. Although the largest flux persists from Lake Eyre, Anameka had similarly large total flux in autumn. This may be associated with grazing of stubble by sheep after the harvest January-February.

Figure 10. For locations across Australia showing monthly average (a), and total (b) flux and annual average (c) and total (d) flux estimated with a wind erosion model (Shao et al., 2004) using ω_{ns} .

Recall that $U_t=20.3 \text{ m s}^{-1}$ was held constant for the simulations and therefore changes in sediment flux represented the important seasonal and inter-annual variability in surface roughness detected using ω_{ns} . The average annual horizontal flux at the selected locations estimated using ω_{ns} was shown in Figure 10c. However, the total annual flux provides more information (Figure 10d). The temporal pattern of predicted sediment flux appears to be consistent with measured inter-annual rainfall variability across Australia. Above average rainfall in central and eastern Australia occurred to 2002 and 2010/2011 which contributed to large vegetation cover and small predicted erosion at these times for the Lake Eyre and Merrineee sites. Peaks in predicted sediment transport are consistent with below average rainfall and declines in vegetation cover starting in 2002/2003 through to the large La Niña event in 2010 and subsequent drought in eastern Australia from 2012 through 2015 (<http://www.longpaddock.qld.gov.au>). Southwestern Australia, around the Anameka site, experienced average or below average rainfall for much of the period 2000-2015, while above average rainfall in 2005/2006 and 2011/2012 appeared not to have a significant effect on the predicted sediment transport rates.

5.4 The robustness of the empirical albedo-based sediment transport model

To summarise the performance of the empirical model we compared it with the shadow model and in both cases made predictions of horizontal flux using all of the 25,000 measurements of albedo and hence ω_{ns} (Figure 11). However, we perturbed both models using randomly generated particle sizes D (50-500 μm) and freestream wind velocities U_f (0-40 m s^{-1}). The results show good general agreement with the shadow model and little response to D in that range. The deviation from the 1:1 line is caused by the difference we noted previously (Figure 5). The empirical model (Eq. 8) is not provided as a definitive description of flux, rather it is presented to show that flux

can be calculated to a reasonable approximation using a straightforward empirical calibration based on ω_{ns} and U_f (notwithstanding the need for u_{*ts} and $H(w)$).

Figure 11. Horizontal sediment flux predicted using the shadow model (Eq. 6) and the empirical model (Eq. 7) using normalised albedo (ω_{ns}) at each of the 33 pixels (500 m) from across the main agro-ecological systems in Australia every 8 days between 2000 to present (around 25000 values). Random numbers for a range of both freestream velocities (U_f ; 0-40 m s⁻¹) and particle sizes (D ; 50-500 μ m) were generated for model perturbation (or model testing). A linear regression model was fitted to these data (dashed line) and compared with the 1:1 line (solid).

6. Implications of using shadow for wind erosion modelling, mapping and monitoring

6.1 Benefits of approximating aerodynamic shelter using shadow

Accurate representation of the turbulent transfer of fluid momentum to the land surface is critical for wind erosion and dust emission modelling. Considerable uncertainty remains, however, in the spatial patterns and magnitude of predicted dust emissions due to the parameterization of surface roughness effects on the drag partition. These uncertainties relate to parameter estimation and scaling, which do not adequately account for the important effects of roughness distribution and wake interactions. The reduced complexity approach of Raupach (1992) was advanced here using albedo to enable an approach for the direct estimation of scalable area-integrated (areal) estimates of aerodynamic properties from Marshall's (1971) wind tunnel measurements. This approach addresses these uncertainties and provides a common and precise framework across scales (field, region to continent) for investigating aeolian processes in space and time and for improving the accuracy of wind erosion and dust emission models.

Perhaps one of the most influential approximations in dust emission modelling is that surface momentum extraction can be represented by L_{45} , the lateral cover of roughness elements (Raupach et al., 1993). We showed here that L_{45} is inadequate to represent the interactions between roughness elements because: (i) its geometric formulation is too simplistic; and (ii) the approximation of sheltering as L_{45} does not allow for shelter areas to interact with downstream roughness elements. The implication is that previous studies which estimated wind erosion using L_{45} have under-estimated L and consequently over-estimated sediment flux. Although this is a bold

statement, we can be confident that it has occurred because in the traditional Shao scheme L_{45} is pervasive influencing total shear stress u_{T*} (Eq. 12), the boundary layer height del (Eq. 13), z_0/h (Eq. 14) and u_{*t} (Eq. 15) because it is based on the Raupach et al. (1993) drag partition correction R_t (Eq. 17). The wind erosion scheme of Marticorena and Bergametti (1995) is similarly affected because L_{45} is similarly pervasive there too. The common practice of tuning model predictions against measured sediment flux (parameters A_n and $cshao$; Eqs 16 and 23, respectively) may well have masked this effect. If model parameterisation continues to be of minor consideration by comparison with the emphasis placed on model tuning then wind erosion modelling may simply use an empirical model (like that which we propose here). In contrast, if the purpose of developing and applying physically-based wind erosion models is to improve the understanding of the processes then much less emphasis should evidently be placed on the model tuning. Overall, wind erosion and dust emission models based on L_{45} have hitherto been hindered by its inadequacies, which have been compounded by the difficulties in estimating L_{45} over large areas.

We demonstrated a direct calibration of the normalised surface albedo or its inverse shadow (ω_{ns}) to measured aerodynamic properties (z_0/h , u_*/U_t , R_t). The approach provided a methodology to account for momentum extraction by surface roughness using albedo data. These data are readily measured in an illuminated wind tunnel or the field from standard pyranometers which can ‘view’ small or large areas depending on their (mast) height and from aircraft or satellite platforms where those data are available globally from MODIS every 8 days at 500 m. These global data will most likely also be available in the near future at 30 m from bi-directional reflectance parameters (MCD43A) and Landsat Thematic Mapper (TM) and Enhanced Thematic Mapper (ETM+) surface reflectance used to generate Landsat albedo (Shuai et al., 2011). For clarity, the methodology also demonstrated that a single zenith illumination angle at 87° viewed at nadir could be used instead of albedo to produce an adequate estimate of the aerodynamic properties. In addition to reducing the complexity of wind erosion models, the approach reduces the uncertainties compounded through parameter estimates for the drag partition schemes. Critically, the approach provides areal information for each pixel that is sensitive to roughness distribution.

6.2 Reduced complexity leading to new opportunities in aeolian research

Of greatest significance is the evident redundancy of information used in the current wind erosion schemes. We showed how the four aerodynamic parameters in the original, widely used Shao wind erosion scheme (L_{45} , R_t , u_*/U_f and z_0/h ; Eq. 5) can be reduced (Eqs. 23-25) so that only u_{S*}/U_f is needed to estimate sediment mass flux. This approach also ensures consistency in the predictions of surface shear stress (previously via z_0/h and often externally sourced) with measurements of ω_{ns} . We found that small changes to the parameters of the Raupach drag partition scheme had a considerable influence on the flux estimates. Furthermore, our results (Figure 4) show that total shear stress (u_{T*}) should not be used to estimate mass flux with the Raupach drag partition because flux inappropriately increases with increasing lateral cover (cf Webb et al., 2014). With the correct drag partition, the use of measured u_{T*} from within rough canopies (e.g., wind velocity profile in a vegetated area) or even modelled u_{T*} for a pixel of rough canopies will over-estimate flux. In these situations, u_{T*} should be converted to u_{S*} using R_t , with R_t obtained from the calibration with ω_{ns} . Combining the precision of the wind tunnel calibration with the precision of ω_{ns} measurements should reduce considerably the uncertainty in modelled sediment mass flux for a range of platforms and across scales. The implication is that measurements of (or modelled) ω_{ns} can be used to predict areal flux with information on only U_f . Notably, there is scope to retrieve D from remote sensing and more specifically using bi-directional soil reflectance modelling (Pinty et al., 1989; Okin and Painter, 2004; Chappell et al., 2007; Wu et al., 2009). Similarly, soil moisture is also readily retrieved from reflectance measurements (e.g., Soil Moisture Active Passive satellite; global every 9 km and every 7 days). The combination of these additional measurements with the approach described here would finally enable remote sensing of wind erosion (Chappell et al., 2006).

The simplicity of our remote sensing approach presents new opportunities for modelling, mapping and monitoring of wind erosion. For example, our new approach is readily applicable to large area global or regional land surface models (LSMs) which currently do not include any wind erosion and therefore no feedbacks between

the loss (or gain of soil) and changes to soil biogeochemical (e.g., C cycling) or biophysical processes (e.g., infiltration or moisture holding capacity) and which may have profound impacts on models and their outcomes (Chappell et al., 2015; Kutra et al., 2016). The many and varied applications of e.g., Revised Wind Erosion Equation (RWEQ) could be similar targets for our empirical wind erosion model based on MODIS albedo and would require far fewer parameters and input data layers. Facilitating the adoption of wind erosion models by other research communities will raise awareness of the significance of wind erosion and provide new and collaborative opportunities for integrating aeolian research in to Earth System Models (Shao et al., 2011) and agricultural-system sciences.

6.3 Current limitations in sediment flux modelling

Perhaps the greatest weakness of our work is that the new models are not demonstrated against measured sediment flux. Instead they are compared with sediment flux calculated from the aerodynamic measurements of Marshall's (1971) wind tunnel. Nonetheless, this approach enables perhaps the greatest precision possible in the calculation of sediment flux (particularly areal fluxes) because of the carefully controlled laboratory conditions of Marshall's (1971) data evident from its enduring use in the literature. Our new approach improved upon the existing modelling approach in terms of the identified weaknesses and redundancy in information content. However, it did not enable an examination of the nature or form of the model which could arise when compared with compatible areal sediment flux measurements. These types of areal flux measurements are, to our knowledge, not available. We also recognise that the sediment transport equation we modified for use with areal ω_{ns} measurements has evolved from point measurements. It could be argued that we should have used existing point flux measurements regardless. However, we believe that this would introduce considerable uncertainty to the comparison because of the large spatial variability in point flux measurements within a given area (Webb et al., 2016). Our implication is therefore that existing flux measurements do not adequately represent areal sediment flux estimates because of the following, all too common, sampling problems associated with their measurement:

- (1) too few sediment flux samples are used to adequately estimate the average for a given area, and typically as the area increases so the variability increases (to some point = spatial dependence);
- (2) sampling variance is not quantified and consequently there is no information to inform the number of samples to use and to contribute to a rigorous framework for detecting change or difference (over time and / or in space);
- (3) inherent bias in existing sampling towards locations where flux occurs – for a given area, flux is measured away from large (vegetation) roughness elements biasing the average flux towards an environment without those influences.

Solutions to these sampling problems have been developed over the last 10 years in soil science and have already been applied in aeolian research and other fields (Chappell et al., 2003a & b; Li et al., 2015; Chappell et al., 2015). We suggest that these solutions should become a routine and essential component of field work in aeolian research. For examples, a new national programme of wind erosion monitoring in the USA (Webb et al. 2015, 2016) has used rigorous sampling designs. When these and other unbiased estimates of areal sediment flux are available in the near future, it would be timely to revisit the point-based sediment transport equation and evaluate a new form for areal sediment flux and validate our shadow-based approach.

6.4 Challenges for future aeolian research

It is important to note that our work and that of others before us (e.g., Raupach's drag partition) is built on the foundation that the results of wind tunnel experiments are general or universal across scales. To our knowledge this is assumed in most aeolian research and particularly in sediment transport and dust emission modelling. On this basis, the main strength of our reduced-complexity approach to estimating aerodynamic properties and sediment mass flux is the link between the precision of wind tunnel studies and the precise and scalable measurement (or bi-directional reflectance models) of albedo that enable area-integrated (areal) estimates of aerodynamic properties. We showed (in several ways e.g., Figure 9a) that using ω_{ns} to establish the key

aerodynamic properties improved the precision with which flux can be estimated using an existing wind erosion scheme. The main benefit shown here was in replacing the use of L_{45} . However, under different circumstances it is very likely that the disconnection of the aerodynamic roughness and wind friction velocity (u_*) by the use of separate external modelling resources would most likely be a source of considerable uncertainty. With the shadow model, that disconnection is unnecessary and therefore the uncertainty is eliminated. Here we showed that the largest uncertainty in sediment flux was caused by the precision of Marshall's (1971) aerodynamic measurements. The influence of roughness configuration on the sediment flux estimates was removed by avoiding L_{45} and the Raupach drag partition scheme. Under the simulated conditions, we reported an uncertainty of area-integrated (areal) sediment flux to be approximately $0.01 \text{ g m}^{-1} \text{ s}^{-1}$. That precision is repeatable over large areas and in different locations using measurements of albedo and our shadow model, because of its direct calibration and thereby the inherited precision of Marshall's (1971) wind tunnel experiments.

Consequently, this work suggests a future testable hypothesis that there is more precision (less uncertainty) in this albedo-based approach to the estimation of areal aerodynamic properties and sediment flux than there is using current approaches to field measurements particularly if they use a single wind velocity profile in heterogeneous roughness to estimate u_{T*} and represent its variation for an unknown contributing area of roughness. This hypothesis represents a challenge to the aeolian research community to quantify the complete uncertainty of the wind erosion measurement 'system' which will identify areas of field-based research which need to be strengthened to avoid misleading conclusions about detecting change in space and time.

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