**FABRIC-REINFORCED CEMENTITIOUS MATRIX BEHAVIOR AT
HIGH-TEMPERATURE: EXPERIMENTAL AND NUMERICAL RESULTS**
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ABSTRACT

The use of externally applied composite systems to upgrade, strengthen or rehabilitate masonry or concrete structures is well established. However, structural strengthening with organic type composites, such as fiber-reinforced polymer (FRP) systems, may be impractical when the element is exposed to high-temperature service conditions, due to significant degradation of the organic resin. Instead, the use of an inorganic matrix, as in the case of fabric-reinforced cementitious matrix (FRCM) composites, may overcome this problem.

The purpose of this study is to evaluate the mechanical behavior under high-temperature conditions of FRCM systems. Different FRCM composites are evaluated and include carbon fabrics ranging from dry to highly-impregnated with an organic resin. The experimental spectrum is comprised of uniaxial tensile and double-shear bond tests performed under temperatures ranging from 20 to 120°C to determine the influence of temperature over the FRCM mechanical properties. Furthermore, SEM analysis was used to study the damage processes at the fiber-matrix interface post tensile testing. Experimental results show variations in the FRCM mechanical properties if tested at high temperature conditions (caused by the deterioration of the resin coating at the interface fiber-matrix) while residual performance after exposure to elevated temperatures remains unchanged. FRCM reinforced with dry fabrics has proven not to be affected by temperatures up to 120°C.

A numerical model using a fracture variational approach, based on incremental energy minimization, was also developed to simulate the FRCM behavior in double shear tests under different temperatures exposition.

Keywords:

FRCM, Temperature, Organic Coating, Strengthening, Damage Mechanics, Variational Modelling.

Nomenclature

<u>Geometrical parameters</u>		<u>Materials parameters</u>	
A	sectional area of the yarn	G	fracture toughness
b_1	thickness of the 1 st layer of mortar	B	size of the process zone
b_2	thickness of the yarn in numerical simulation	q	exponent of the interface damage energy
b_3	width of the FRCM in numerical simulations	E_m	elastic modulus of the mortar
h	FRCM anchorage length in double shear tests	E_2	FRCM elastic modulus in the cracked phase
l_1	mean length of the internal isostatic lines	E_f	tensile elastic modulus of the yarn
l_2	mean length of the external isostatic lines	μ, λ	Lamé's coefficients
l_m	internal length of the damage surface	k	elastic coefficient of interface springs
β	geometrical ratio	<u>Forces and stresses</u>	
Ω_f	yarn domain	f_{max}	peak load in double shear tests
Ω_m	matrix domain	σ	tensile normal stress in the yarn
Λ	interface domain	τ_e	maximum shear stress at the interface
<u>Variables</u>		τ_r	residual shear stress at the interface
α	damage parameter	σ_e	tensile strength of the mortar
$\mathbf{u}$	displacement field	σ_u	FRCM ultimate tensile strength
<u>Displacements and strains</u>		τ_1	shear stresses along the internal isostatic lines
s	fabric total displacement	τ_2	shear stresses along the ext. isostatic lines
δ	yarn displacement in numerical simulations	f	longitudinal force in the yarn
ε_2	FRCM ultimate tensile strain		

1. Introduction

The use of fiber-reinforced polymer (FRP) systems to reinforce masonry or concrete structures may be impractical when the element is exposed to high-temperature service conditions. FRP mechanical properties can be drastically reduced if the temperature exceeds the glass transition temperature (T_g) of the organic resin used for fiber impregnation and bond to the substrate. Experimental studies showed a severe reduction of FRP tensile strength, stiffness and bond properties to the substrate when exposed to elevated temperatures due to a rapid deterioration of the FRP-substrate adhesion when the temperature exceeds the T_g of the resin (typically around 60 to 80 °C), resulting in delamination of the composite and loss of efficacy of the reinforcement [1-5].

Studies conducted by Bisby and co-workers [6] on the mechanical characterization of FRP materials at high temperature showed that half of the tensile strength of the FRP was lost when tested near the T_g of the epoxy matrix. Lap-splice tests showed that the FRP-to-FRP bond strength was affected even more by temperature exposure near T_g with 90% loss in lap-splice strength.

Al-Salloum and co-workers [7] suggested to not exceed the FRP T_g in order to avoid serious consequences. In case temperature is allowed to reach up to 200 °C (thus greatly higher than T_g), the ultimate capacity of FRP-strengthened members should be kept at less than 25% of its corresponding value at room temperature.

For this reason, the use FRP composites in construction, where high temperature exposure is critical, may be limited and additional information is needed when selecting strengthening solutions. For example, the use of insulation to maintain the temperature on the FRP surface

below T_g is possible, although not always practicable [8,9]. Hence, alternative solutions need to be explored and evaluated.

FRCM systems use inorganic matrices, which are less susceptible to high temperature and may result cost effective compared to FRPs [10-15]. However, the bond between fibers and inorganic matrix is a critical issue in FRCM composites and is strongly influenced by the ability of the cementitious matrix to saturate dry fiber yarns; also affected is the bond between internal and external fibers within the yarns and between external fibers and matrix in case of dry fabrics and possibly between coating and matrix in case of coated fabrics. FRCM for structural strengthening applications is a relatively new material and durability is an important aspect to be considered. Factors affecting the durability of FRCM composite systems must consider the environmental performance of each of its components and their interfaces: the cementitious matrix, the fabric reinforcement, the fabric-matrix interface and the matrix-substrate interface are the different elements that need to be considered in relation to the service environments in which they are expected to perform [16]. FRCM is expected to overcome some of the issues that are typically found in FRP because of the better performance of the cementitious matrix to high temperatures. However, limited experimental and analytical studies have been conducted to evaluate the behavior of FRCM under high temperatures and the residual performances after exposure to elevated temperatures.

An experimental study on the effect of high temperature on the performance of carbon fiber-reinforced polymer (CFRP) and FRCM confined concrete element was conducted by Trapko [17], using concrete cylinders reinforced with CFRP sheets and FRCM mesh and exposed to temperature ranging from 40 to 80 °C. In the case of polymer jackets, 40 °C increase in temperature resulted in 20% decrease of the load-bearing capacity. The compressive strain of specimens tested in 80 °C was approximately half of the strain in specimens tested at 40 and 60 °C. Load-bearing capacity decrease by 5–10% was observed for FRCM confined elements upon temperature increase from 40 to 80 °C. Also, compressive strain decrease by approximately 11% was observed upon temperature increase from 40 to 60 and 80 °C.

FRCM performances at high temperature exposure may change when fabrics are pre-impregnated with polymeric resins. Experimental studies showed that the use of a polymer coating applied on carbon fabric may significantly increase the mechanical capacity of FRCM systems for both tensile and shear bond strengths when applied to masonry or concrete supports [18-20]. However, when the textile reinforcement is coated with a polymer, the bond performance between fibers and matrix is strongly affected by temperature [21].

Recent studies by Silva and co-workers [22] using FRCM reinforced with carbon fibers showed a polymer interlocking mechanism between filaments and matrix when heating the polymer coated fibers up to 150 °C. This mechanism results in significant increases in the maximum pullout load. Krüger and Reinhardt [23] performed fire tests on four different I-shaped mortar beams reinforced with AR-glass and carbon textiles. The investigation was focused on the load bearing capacity of the composite during a fire test under constant load. In one of the cases a SBR (Butadien-Styrol) thermoplastic resin was used as coating in the fiber. The results showed to be very dependent on the fire behavior of the used fibers. Due to the softening of the SBR coating (around 90 °C) the fiber–matrix interface rapidly deteriorated, resulting in fiber pullout and, subsequent, failure.

Michels and Motovalli [24] presented experimental results of the tensile strength decrease of coated carbon fiber yarns after high temperature exposure up to 1000°C. The investigation was performed at room temperature on carbon fiber yarns after having been thermally subjected to

constant temperature of 300, 500, 700 and 1000 °C in a tube furnace for 30 minutes. It was observed that an exposure at 300°C for 30 minutes does not affect the mechanical properties of the analyzed reinforcement. However, a further increase in temperature results in significant damage to the material performance at 500 °C and no residual strength at 700 °C. Tests on a reinforced concrete slab strip strengthened with a shotcrete layer including a composite mesh as tensile reinforcement was also investigated. Under a constant service load, the slab was exposed to fire with a temperature rise according to a European standard curve (ETK) for two hours. The slab could withstand the applied load under fire exposure, during which the composite mesh reached a temperature of about 440 °C.

This study aims at understanding FRCM behavior under high-temperature conditions as provided by an environmental chamber. Specimen reinforcement included fabrics made of carbon fibers ranging from dry to highly impregnated with an organic resin. A series of uniaxial tensile tests and double shear bond tests were performed under temperatures up to 120 °C to understand the influence of temperature over the mechanical properties of the FRCM and, in particular, the variation of bond between fabric and matrix when organic resin pre-impregnation was applied to the fabric.

To better understand the experimental results, a variational damage model has been numerically implemented in a finite element code, and simulations have been performed, reproducing the FRCM different behaviors observed in double shear bond tests at different temperatures and different fibers impregnation. Modeling investigations have been conducted also in [25-27] to have an insight into experimental results. However, FRCM behavior based on variation damage models has never been reproduced.

The model proposed in this paper falls into the category of phase-field models, which, in the last decade, have been object of many researches, and have been applied to several problems of material science. The phase-field approach was first proposed in [28] for regularizing the Griffith's theory of brittle fracture, formulated as a minimum problem [29]. The sharp fracture of Griffith's theory is approximated by a smeared fracture, described by layers of finite thickness where the material damages and strains localize. An auxiliary scalar field α is introduced into the material internal energy functional, which plays the role of a damage field assuming values $\alpha=0$ for sound material and $\alpha=1$ for totally damaged material, and an intrinsic length scale parameter controls the thickness of the damaged zone. When the length scale parameter goes to zero, the thickness of the damaged layer shrinks to zero, and sharp Griffith's fracture is recovered. Including both displacement and damage smooth fields, the model accounts for a straightforward implementation by standard finite elements. Since the formulation [28], many improved and enriched models have been proposed. Among the many, we mention [30], where the variational problem [28] has been reformulated in the more general framework of finite elasticity, [31], where the bulk energy has been decomposed into non damageable spheric and damageable deviatoric parts to reproduce shear fractures, and [32,33], where fracture under tensile and compression stress states has been differentiated.

Here, a phase-field model is developed for the double shear test, which is schematized by a two-dimensional problem. Different energies are assigned to the cementitious matrix, to the fibers and to the matrix-fibers interface. While the fibers are supposed to be unbreakable, and thus they are purely elastic, the matrix is breakable. Its internal energy accounts for an elastic and a damage term. This latter is sum of a dissipative local contribution, a linear function of α , and a non-local contribution depending on the gradient of α , as in [34]. Materials with this energy

exhibit a brittle-elastic mechanics. They deform elastically as long as a maximum stress value is attained, and, afterwards, they brutally damage and break.

A damageable elastic springs distribution is applied at the matrix-fibers interface. Its damage energy is sum of a local and a non-local gradient term, and the local contribution is a non-linear power function of α . To our knowledge, the expression of the local damage energy is a novelty, never proposed in literature, and it allows of describing initial purely elastic regimes followed by stress-softening phases. Moreover, it allows of accounting for residual strength when large relative sliding displacements are attained, thus interpreting the frictional behavior observed in pullout tests. While the matrix and fibers material parameters are kept fixed, the parameters characterizing the interface vary with respect to temperature and type of fibers (dry or pre-impregnated with organic resin). Thus, in the model, thermal and fibers impregnation affect only the interface parameters.

For a system characterized by these energies, the displacement and damage evolution, when certain loads are applied and increased, is determined by solving a constrained incremental minimization problem. Incremental minimization is a powerful mathematical tool to capture local minima in evolution problems, and it has been applied to problems of fracture [35], plasticity [36,37], and crystal plasticity [38,39]. Here it is solved numerically by implementing a Sequential Quadratic Programming algorithm.

The paper is organized as follows. In Section 2 the experimental investigation is explained. Section 3 describes the variational damage model used to reproduce the experimental results of double shear bond tests. In Section 4 the experimental results are reported and compared with numerical simulations in Section 5. Conclusions are drawn in Section 6.

2. Experimental investigation

Tensile tests were performed using a MTS 651 environmental chamber at temperatures of 20, 80 and 120 °C. A clevis grip system was used to anchor the specimens by means of metal plates epoxied to the ends of the FRCM coupons, in order to allow the slippage of the fabric within the matrix and to better investigate the influence of a coating when the system is exposed to high temperatures [AC434 - Acceptance criteria for masonry and concrete strengthening using fabric-reinforced cementitious matrix (FRCM) composite systems]. In this case, the load is transferred only through the matrix to the fabric.

Double shear bond tests were also performed to evaluate the bond capacity of FRCM applied on clay brick substrate and the behavior at the fabric-mortar interface when exposed to the aforementioned temperatures.

2.1 Materials

In order to study the effects of enhancing the bond at the fabric-matrix interface with an organic coating on the FRCM fabric and the mechanical behavior of the system when exposed to different temperatures two kinds of carbon fabric are used: dry and highly impregnated with epoxy resin plus sand (HS), (Figure 1).

Figure 1. Dry and coated (HS) carbon fabrics

The enhancement of the bond is made by coating the fabric with a flexible epoxy and by applying a layer of quartz sand on the surface. Table 1 summarizes some of the geometrical and mechanical properties of the carbon fabric as obtained from the manufacturer. Values regarding mechanical properties of the carbon yarns (used in numerical analysis) were evaluated experimentally by means of tensile tests, according to EN ISO 10618/2005. The characteristics of the epoxy used as coating are reported in Table 2.

Table 1. Carbon Fabric characteristics

Dry carbon fabric, bidirectional, balanced	
Resistant area (for each direction) ¹	0.052 mm ² /mm
Fabric weight ¹	180 g/m ²
Fiber tensile strength ¹	4900 MPa
Fiber elastic modulus ¹	240 GPa
Fiber break elongation ¹	2 %
Yarn tensile strength ²	1850 MPa
Yarn elastic modulus, E_f ²	150 GPa
Yarn Poisson ratio, ν_f ¹	0.3

¹obtain from manufacturer

²experimentally obtained [EN ISO 10618/2005]

Table 2. Coating characteristics obtain from manufacturer

Two component epoxy system	
Tensile strength	0.8 MPa
Density	1.12 g/m
Max recommended operating temperature	50 °C
Strain at break	70 %
Exothermic peak	58-68 °C
Resin viscosity at 25°C	6000 mPas
Hardener viscosity at 25°C	1350 mPas

The inorganic matrix used is a commercially available cementitious mortar, herein referred to as Mortar-45. The compressive and splitting tensile strengths were evaluated according to ASTM C109 and ASTM C496 [40,41] at 28 curing days, on 50 mm cubes and 50x100 mm cylinders, respectively. The Elastic modulus was evaluated according to ASTM C580 [42] and the average results of 5 repetitions are reported in Table 3.

Table 3. Mechanical properties of the mortar used as FRCM matrix

Mortar 45 - Fiber-reinforced, structural repair mortar	
Compressive strength	50 MPa
Elastic modulus, E_m	34.5 GPa
Splitting tensile strength, σ_e	6.2 MPa
Unit weight	2275 kg/m ³
Yarn Poisson ratio, ν_m	0.2

2.2 Temperature profile

A temperature profile along the length of the FRCM specimen was obtained, using type J thermocouples embedded in the mortar at four different locations (Figure 2). This allowed the possibility of measuring the temperature at the fabric-mortar interface when exposed to 80 and 120 °C, while also understanding the effect of the metal tabs used to grip on the specimen.

Results depicted in Figure 3 shows a smooth increase of temperature of the FRCM specimen when no load is being applied, where after two hours the center of the specimen reached 88 and 90% of the peak applied temperature corresponding to the 80 and 120 °C profile, respectively.

Figure 2. Application of thermocouples at the fabric-matrix interface

Figure 3. Heat development at the fabric-mortar interface of a FRCM coupon when exposed to 80 and 120 °C

Observation: the curve ai2 fits almost perfectly with the curve ai3, for this reason is not easily observable in the graph.

2.3 Tensile and double shear bond test at high-temperature exposure

FRCM behavior under high temperature exposure have been investigated by means of the two main tests to characterize this material: tensile test as described by AC434 Annex A and double shear bond test (RILEM TC250-CSM).

Tensile coupons 410x60x10mm were prepared and left to cure for 28 days at 20 °C and 70% relative humidity. Metal tabs were then adhered with epoxy to the ends of the specimens with an anchor length of 150 mm, by using a special high-temperature epoxy able to withstand up to 150 °C.

A total of 18 uniaxial tensile tests were conducted using a screw-driven universal test frame with a maximum capacity of 130 kN and a MTS 651 Environmental Chamber. A clevis-type grip system was used and axial deformation was measured using a clip-on extensometer with a 100 mm gauge length, attached to the metal tabs surface. The load was applied under displacement control at 0.3 mm/min. Tensile tests were initiated after conditioning the specimens in the chamber for 100 minutes, so as to ensure the internal temperature at the center of the specimen failure zone was approximately 90% of the oven temperature, either 80 or 120 °C.

A total of 12 double shear bond tests were performed on clay bricks substrates. Specimens were fabricated with dry and coated carbon bidirectional fabrics, using the same type of cementitious mortar (Mortar-45). The bond length was kept constant and equal to 100 mm. The fabric was wrapped around a rigid steel cylinder and the specimens were tested at 20 °C and after being exposed to 120 °C for 100 minutes by means of an environmental chamber. The load was applied under displacement control at 0.5 mm/min. The double shear test set-up and the principal failure mode by slippage of the fabric within the mortar are shown in Figure 4.

Furthermore, 3 double shear bond tests have been performed to evaluate the residual capacity of FRCM after being exposed to high temperature. Specimens were placed in oven at 120 °C for 60 minutes, cooled down and tested at 20 °C. A test matrix that summarizes all experimental tests is illustrated in Table 4.

Table 4. Test matrix

Test	Carbon fabric	# Tests	Temperature of testing (°C)	Description
Tensile Test	DRY	3, 3, 3	20, 80, 120	Specimens have been tested after being exposed to the reference temperature for 100 minutes
	HS	3, 3, 3	20, 80, 120	
Double shear bond test	DRY	3, 3	20, 120	
	HS	3, 3	20, 120	
	HS	3	20	Specimens have been tested at room temperature after being exposed at 120 °C for 60 minutes

Figure 4. Double shear bond test set up and slippage failure mode

3. Variational damage model for FRCM

In this section, the variational damage model used to reproduce the experimental results of the double shear bond test is presented. In Sect. 3.1, the geometry of the experiment is simplified into a two-dimensional scheme, where the hypothesis of plane strain state is assumed. The energy assigned to the sample is discussed in Sect. 3.2, and, in Sect. 3.3, the damage evolution problem is formulated as an incremental energy minimization problem, and the numerical solving strategy is briefly recall.

3.1 Geometrical scheme for double shear bond test

We consider a single yarn embedded in a cementitious matrix, as represented in Fig. 5a. The system is fixed to a rigid support (clay brick substrate) on one lateral side, and the yarn is subject to a constant displacement δ . It generates a tensile normal stress σ in the yarn and a shear stress τ at the interface with the matrix, which flows toward the clamped sample side. The isostatic lines of shear stress in a transverse cross-section are schematically drawn in Fig. 5b. The amounts of shear stress flowing from the internal and external yarn faces (the half-surfaces opposite to the clamped and traction-free matrix sides, respectively) are determined as follows. Let us consider the green and blue isostatic lines of Fig. 5b, which flow from points placed on the internal and external yarn face, respectively, and whose lengths l_1 and l_2 are approximately mean lengths among all the lines flowing from the internal and external faces. For a sample portion of infinitesimal thickness dy , we estimate the vertical shear stresses flowing through the surfaces projection of the green and blue isostatic lines (green and blue surfaces in Fig. 5c). A schematic plane representation of these surfaces is drawn in Fig. 5d. Given a longitudinal force f (per unit thickness) in the yarn, the shear stresses τ_1 and τ_2 flowing through the green and blue regions of length l_1 and l_2 , are

$$\tau_1 = \frac{\beta}{1+\beta} \frac{df}{dy}, \quad \tau_2 = \frac{1}{1+\beta} \frac{df}{dy}, \quad \text{with } \beta = \frac{l_2}{l_1}. \quad (1)$$

They are determined by solving the equilibrium equation $\tau_1 + \tau_2 = \frac{df}{dy}$, and the kinematical

compatibility condition $\frac{\tau_1}{G} l_1 = \frac{\tau_2}{G} l_2$, with $G = \frac{E}{2(1+\nu)}$ the shear modulus. Since l_1 and l_2 are

mean lengths, the ratios $\beta/(1+\beta)$ and $1/(1+\beta)$ in (1) give estimates of the tensile force rates transmitted to the clamped surface through the internal and external faces of the yarn, respectively. Thus, supposing a constant distribution of σ in the yarn cross-section, stresses in the red yarn portion of area $\beta A/(1+\beta)$ are transmitted through the internal part of the matrix, while the stresses in the rose portion of area $A/(1+\beta)$ are transmitted through the external and lateral parts of the matrix. In D'Antino and Carloni [43,44], the authors tested some single-lap shear FRCM specimens with and without the external matrix layer in order to study the role of the different matrix layers in the stress-transfer mechanism. It was found that the external layer increases the bond strength of about 10%. Accordingly, in the model we set $\beta=9$, so that 9/10 of the tensile force is transmitted to the support through the internal cementitious layer, and 1/10 through the external layer.

We restrict the study to the sample portion between the yarn and the clamped side of the sample, where the most severe stress state is attained. Accordingly, we limit to the cross-section part drawn in Fig. 5e, where only the yarn portion of area $\beta A/(1+\beta)$ is considered (red area). It is supposed to be rectangular. Sliders at the boundaries reproduce the confining effect of the excluded part of the sample, and the isostatic lines simplify in equispaced straight lines, parallel each other. For this simplified geometry, the strain state is plane, belonging to planes parallel to the x - y plane. The geometry of the plane problem is plotted in Fig. 5e, with $h=100$ mm, $b_1=5$ mm, $b_2=0.23$ mm (determined for $A=1.04$ mm² and $b_3=4$ mm).

Figure 5. Problem geometry. (a) Yarn-matrix geometry of the shear bond test. (b) Shear stress isostatic lines in a cross section. (c) Infinitesimal portion of the sample and representative isostatic surfaces (d) Shear stresses in the green (internal) and blue (external) isostatic lines. (e) Cross-section portion. (f) Transversal section subject to plane strain state.

3.2 Energies

We refer to the geometrical scheme drawn in Fig. 5f, with Ω_m the matrix domain, Ω_f the yarn domain, and Λ the matrix-yarn interface. The tensile displacement δ applied at the upper side of Ω_f monotonically increases from $\delta_0=0$ to a final positive value. Body loads are neglected, and the hypothesis of plane strain states is assumed. For a given Cartesian coordinate system $(O;x,y)$, the displacement field is $\mathbf{u}(\mathbf{x}) = [u(x, y), v(x, y)]^T$. We assign the following energies to Ω_m , Ω_f , and Λ .

Yarn energy. Ω_f is supposed to be made of an isotropic linearly elastic material. Its strain energy is

$$E_f(\mathbf{u}) = \int_{\Omega_f} (\mu_f (\nabla \mathbf{u})^2 + \frac{\lambda_f}{2} (\text{div} \mathbf{u})^2) d\mathbf{x}, \quad (2)$$

where μ_f and λ_f are the Lamé's coefficients.

Matrix energy. The cementitious matrix Ω_m is supposed to be brittle, and its energy is

$$E_m(\mathbf{u}, \alpha) = \int_{\Omega_f} (W_s^-(\mathbf{u}) + (1-\alpha)^2 (W_s^+(\mathbf{u}) + W_D(\mathbf{u}))) d\mathbf{x} + \int_{\Omega_f} d \left(\alpha + \frac{l_m^2}{2} (\nabla \alpha)^2 \right) d\mathbf{x}. \quad (3)$$

It depends on the displacement $\mathbf{u}$ and on the additional scalar field $\alpha(x): \Omega_f \rightarrow [0,1]$, which plays the role of a damage parameter. When $\alpha=0$, the material is intact, and, when $\alpha=1$ the material is completely fractured. The first integral in (3) represents the elastic strain energy. W_s^+ and W_s^- are the spherical parts of the energy, evaluated in points where volume expansion ($\text{div}\mathbf{u} > 0$) and contraction ($\text{div}\mathbf{u} < 0$), respectively, are attained, and W_D is the deviatoric part of the energy, whose expressions are

$$W_s^\pm(\mathbf{u}) = \left(\frac{\mu_m}{3} + \frac{\lambda_m}{2} \right) (\text{div}^\pm \mathbf{u})^2, \quad W_D(\mathbf{u}) = \mu_m (\nabla \mathbf{u})^2 - \frac{\mu_m}{3} (\text{div} \mathbf{u})^2, \quad (4)$$

with $\text{div}^+ \mathbf{u} = \max(\text{div} \mathbf{u}, 0)$, $\text{div}^- \mathbf{u} = \max(-\text{div} \mathbf{u}, 0)$.

The second integral in (3) represents the damage energy, and it is sum of a local linear term and a quadratic non-local gradient term. Energies of the form (3) have been proposed in [32,33] for materials exhibiting different damage evolutions in the case of expansion and compression. When (3) is minimized, a competition is engaged between the first integral term, the elastic bulk strain energy, and the second integral term, the damage energy. The strain energy is minimized for fixed $\mathbf{u}$ by $\alpha=1$, while the damage energy is minimized by $\alpha=0$. However, the transition from $\alpha=0$ to $\alpha=1$ is associated with a non-null value of $\nabla \alpha$, indeed penalized by the second integrand of the damage energy, which represents an interface energetic term. Since $(1-\alpha)^2$ multiplies $(W_s^+ + W_D)$ in the first integral, only the strain energy associated to expansion and shear enters into the competition with the damage energy. Thus, in the body regions where the volume change is negative, only the deviatoric part of the strain energy can be released by the creation of damage, and thus shear mode failures are energetically convenient (mode II failure). On the contrary, in the regions with positive volume change, the whole elastic energy may redeem the increments of the damage energy, and, as a result, mixed cleavage and shear failures evolve.

In [34,45], the minimum problem associated to the functional (3) has been solved in the one-dimensional setting of a tensile test, and the following simple formulas have been deduced

$$d = \frac{\sigma_e^2}{E}, \quad l_m = \frac{B}{2\sqrt{2}}, \quad G = \frac{4\sqrt{2}}{3} dl_m, \quad (5)$$

which relate the constitutive parameters d and l_m , characterizing the damage energy in (3), to easily measurable experimental data, obtained from tensile tests, i.e., the normal stress σ_e attained at the end of the elastic phase, the fracture toughness G , the Young's modulus E , and the size B of the so called process zone, i.e., that zone where damage develops and coalesces in a fracture surface. Formula (5)₂ clearly show that l_m is an internal length of the material related to the width B of the damage bands. In the simulations we determine d and l_m from (5)_{1,2}, and (5)₃ gives an estimate of the fracture toughness.

In (2) and (4), Lamé's coefficients μ and λ are related to the Young's modulus E and Poisson's ratio ν by the formulas $\mu = \frac{E}{2(1+\nu)}$, $\lambda = \frac{E\nu}{(1+\nu)(1-2\nu)}$.

Interface energy. A distribution of damageable elastic springs are assumed at the matrix-yarn interface Λ , whose energy is

$$\mathbb{E}_s(\boldsymbol{\delta}, \alpha) = \int_0^h (1-\alpha)^2 \frac{1}{2} \mathbf{K} \boldsymbol{\delta} \cdot \boldsymbol{\delta} dy + \int_0^h a \left(\frac{1}{q} ((1-\alpha)^{-q} - 1) + \frac{1}{2} l_s^2 (\nabla \alpha)^2 \right) dy. \quad (6)$$

It depends on the displacement jump at the interface $\delta(y) = [\delta_x(y), \delta_y(y)]^T = [u_f(b, y) - u_m(b, y), v_f(b, y) - v_m(b, y)]^T$, and on the interface damage $\alpha(y)$, with $y \in (0, h)$. As in (3), the first integral represents the elastic energy and the second integral accounts for the damage energy. The elastic coefficients k_x and k_y of the springs in the normal and tangential directions to the interface are collected in the elastic tensor $\mathbf{K} = \begin{bmatrix} k_x & 0 \\ 0 & k_y \end{bmatrix}$.

The damage energy is sum of two contributions, a power function of α , and a non-local quadratic function depending on $\nabla \alpha$. To characterize the coefficients a and q in the damage energy, we solve the problem of an infinitesimal interface of length dy , subject to a shear stress τ . If we suppose that $\delta_x = 0$, the elementary interface energy is

$$dE_s(\delta_y, \alpha) = ((1-\alpha)^2 \frac{1}{2} k_y \delta_y^2 + \frac{a}{q} ((1-\alpha)^{-q} - 1) - \tau \delta_y) dy, \quad (7)$$

where the last term is the external energy due to the imposed shear load τ . To determine an equilibrium configuration we require the energy first variation to be non-negative, $\delta dE_s(\delta_y, \alpha; \lambda, \beta) \geq 0$, for any admissible perturbations (λ, β) such that $\beta \geq 0$. Following a standard variational procedure, we obtain the equilibrium relations

$$\tau = (1-\alpha)^2 k_y \delta_y, \quad -(1-\alpha) k_y \delta_y^2 + a(1-\alpha)^{-(q+1)} \geq 0. \quad (8)$$

The first equation is the linear load-displacement relation due to the springs. The second relation is a damage criterion analogous to the criterion discussed in [34,45] for the uniaxial traction problem. The damage can evolve, when (8)₂ is satisfied as an equality, and it cannot, if (8)₂ is a strict inequality. In a process of increasing τ , starting from an unstressed undamaged initial configuration $\tau = \delta_y = \alpha = 0$, (8)₂ is strictly satisfied for $\alpha = 0$ and $\delta_y < \sqrt{a/k_y}$, or, equivalently, $\tau < \sqrt{ak_y}$. Thus, for $0 < \tau \leq \sqrt{ak_y}$, the evolution is purely elastic. The elastic undamaged phase ends when $\tau = \tau_e = \sqrt{ak_y}$ (and $\delta_y = \delta_e = \sqrt{a/k_y}$), from which we obtain

$$a = \tau_e^2 / k_y. \quad (9)$$

This relation is used to calibrate the constitutive parameter a , since the right-hand side quantities are easily measurable from experiments. In the subsequent damage phase $\tau > \tau_e$, α grows, and (8)₂ is satisfied as an equality. We say that the evolution is stress-hardening (-softening) if $d\tau/d\alpha > 0$ (< 0), that is, if the stress increases (decreases) for α growing. From (8), the evolution is stress-hardening if $q > 2$ and stress softening if $-2 < q < 2$. In Fig. 6, dimensionless δ - τ curves are plotted for different values of q . If we solve (8) with respect to α and q , for given values of $\delta_y = \delta_r$ and $\tau = \tau_r$, we obtain the expression

$$q = -2 \left(\frac{\log(k_y \delta_r^2) - \log a}{\log \tau_r - \log(k_y \delta_r)} + 1 \right), \quad (10)$$

where $\log$ stands for the natural logarithm. Suppose that a pair (δ_r, τ_r) is known from experiments. For instance, τ_r is the residual shear stress mainly due to friction attained at a large relative

shear displacement δ_r (see the pair (δ_r, τ_r) in the curve $q=-1$ of Fig. 6). Then (10) is used to calibrate the parameter q .

Figure 6. Response curves for different values of q .

The internal length l_s in (6) is related to the length of the detachment front D , where α grows from 0 to 1, by the relation [34,45]

$$l_s = \frac{D}{const}, \quad \text{with } const = \int_0^1 \sqrt{\frac{q}{(1-\alpha)^{-q} - 1}} d\alpha. \quad (11)$$

If we assume $q=-2$ of a brittle interface, we get $const = \pi\sqrt{2}/2$, and thus $l_s \approx 0.45D$.

Total Energy. The internal energy of the system is sum of the energies (2), (3) and (6)

$$E(\mathbf{u}, \alpha) = E_f(\mathbf{u}) + E_m(\mathbf{u}, \alpha) + E_s(\delta(\mathbf{u}), \alpha). \quad (12)$$

Since volume and surface forces are null, it coincides with the total energy of the system.

3.3 Incremental energy minimization

The evolution of $\mathbf{u}$ and α , for increasing δ , is determined by means of incremental energy minimization. We introduce an evolution “time”-like parameter t , and suppose that δ , $\mathbf{u}$ and α depend on t . In particular, δ is a monotonic increasing function of t . A subscript is used to indicate dependence on t , and a dot indicates derivative with respect to t , i.e., given a function $v=v_t(\mathbf{x})$, $\dot{v}=dv/dt$. Time is discretized into intervals of length τ , and within each time step $t \rightarrow t + \tau$, we suppose that $\mathbf{u}$ and α are linear functions of τ

$$\mathbf{u}_{t+\tau} = \mathbf{u}_t + \tau \dot{\mathbf{u}}_t, \quad \alpha_{t+\tau} = \alpha_t + \tau \dot{\alpha}_t, \quad (13)$$

and that the energy (12) is approximated by the second-order development

$$E(\mathbf{u}_{t+\tau}, \alpha_{t+\tau}) = E(\mathbf{u}_t, \alpha_t) + \tau \dot{E}(\mathbf{u}_t, \alpha_t; \dot{\mathbf{u}}_t, \dot{\alpha}_t) + \frac{1}{2} \tau^2 \ddot{E}(\mathbf{u}_t, \alpha_t; \dot{\mathbf{u}}_t, \dot{\alpha}_t). \quad (14)$$

This latter rewrites in the form

$$E(\mathbf{u}_{t+\tau}, \alpha_{t+\tau}) = E(\mathbf{u}_t, \alpha_t) + \tau F(\dot{\mathbf{u}}_t, \dot{\alpha}_t), \quad (15)$$

with $F(\dot{\mathbf{u}}_t, \dot{\alpha}_t)$ a quadratic functional of $(\dot{\mathbf{u}}_t, \dot{\alpha}_t)$. If $(\mathbf{u}_t, \alpha_t)$ at the instant t is known, the solution (13) at $t+\tau$ is obtained by finding the pair $(\dot{\mathbf{u}}_t, \dot{\alpha}_t)$, which solves the constrained quadratic programming problem

$$(\dot{\mathbf{u}}_t, \dot{\alpha}_t) = \arg \min \{ F(\dot{\mathbf{u}}_t, \dot{\alpha}_t), \quad \dot{\alpha}_t \geq 0, \quad + \text{boundary conditions} \}. \quad (16)$$

A numerical code has been developed to solve the above problem. Discretized by linear triangular finite elements, the solution of (16) has been determined at each time step by means of an alternate iterative minimization procedure that consists in iterating the double minimization of F , first with respect to $\dot{\mathbf{u}}_t$, keeping $\dot{\alpha}_t$ fixed, and then with respect to $\dot{\alpha}_t$, for fixed $\dot{\mathbf{u}}_t$. Iterations are stopped when the L_∞ -norm difference of two consequent solutions is smaller than a certain tolerance. Convergence and computational performances of this numerical scheme are thoroughly discussed in [46].

4. Experimental results

4.1 Tensile test results

FRCM specimens with coated carbon fabrics were significantly affected by external thermal exposure. Table 5 shows the average results based on three test repetitions. Even if the number of specimens tested was limited from a statistical point of view, and results should be confirmed by a larger experimental programme, the emerging line seems quite clear and it allows the considerations reported below. The decrease in mechanical properties of the FRCM system with coated fabrics when exposed to high temperatures is significant compared to those at room temperature when the ultimate tensile strength (σ_u) at 80 and 120 °C was found to be 70% lower compared to that at 20 °C for the coated fabric, while the reduction of the ultimate strain (ϵ_2) was substantial, from 26000 to 4000 $\mu\epsilon$ when the specimen was tested at 120 °C. The failure by slippage was the same of the dry fabric FRCM. On the other hand, the FRCM systems with uncoated (dry) fabric only experienced a drop of 11% in tensile strength when subjected to 120 °C.

Table 5. Tensile test results [according to AC434, Annex A]

Mortar	Fabric	Temp. (°C)		E_2 (GPa)	% change E_2^*	σ_u (MPa)	% change σ_u^*	ϵ_2 (%)	Fail. mode
Mortar-45	Dry	20	Average	-	-	986	-	0.010	S
			COV (%)	-	-	9	-	30	
		80	Average	-	-	955	-3	0.012	S
			COV (%)	-	-	11	-	18	
		120	Average	-	-	874	-11	0.008	S
			COV (%)	-	-	12	-	12	
	HS	20	Average	49	-	1366	-	0.026	F/S
			COV (%)	25	-	18	-	22	
		80	Average	36	-27	411	-70	0.012	S
			COV (%)	14	-	6	-	10	
		120	Average	35	-29	407	-70	0.004	S
			COV (%)	17	-	10	-	22	

S) Slippage of the fabric within the matrix

F) Fabric failure

*Percentage change relative to room temperature conditions (20 °C)

4.2 SEM analysis

The interface between coated carbon yarn and surrounding mortar was observed by SEM (at a magnification ranging from 30x to 50x), on samples cured at room temperature (Figure 7a) and after being tested at 120 °C (Figure 7b).

The post-tensile test detachment of the yarn from the matrix resulting in the consequent slippage of the fabric within the mortar is visible. The coated yarn is free to slip within the mortar after the resin has exceeded the T_g , while the sand grains used to improve the interface bond remain attached to the cementitious matrix.

Figures 7. SEM analysis at yarn-matrix interface before (a) and after (b) tensile test

4.3 Double shear bond test results

Double shear tests confirmed the undesirable effect of the enhancement of coating the FRCM fabric on the mechanical properties of the FRCM system when subjected to high temperature conditions. Results of the maximum peak load and relative displacements are reported in Table 6. At room temperature, the FRCM enhanced with coated fabric had higher shear bond strength than the dry counterpart; however, when exposed to high temperatures the bond at the fabric-mortar interface for fibers with epoxy coating is reduced as seen in the displacement-load graph shown in Figure 8. The reduction in both load carrying capacity and displacement of the fiber-coated FRCM system is due to the exposure to 120 °C temperature.

Table 6. Double shear test results [according to RILEM TC250-CSM]

Mortar	Fabric	Temp (°C)		Peak Load (per side) f_{max} (N)	% change f_{max}	Slip at peak load (mm)	Peak stress in the textile $\sigma_f = f_{max}/A_f$ (MPa)
Mortar-45	Dry	20	Average	1976	-	2.89	633
			COV (%)	10		5	10
	HS	120	Average	2094	+ 6	3.37	671
			COV (%)	9		8	9
		20	Average	2503	-	4.18	802
			COV (%)	2		2	2
		120	Average	961	- 62	3.12	308
			COV (%)	8		6	8

A comparison between FRCM specimens exposed and not to temperature, both tested at 20°C, is shown in Figure 9. Results reported in Table 7 show that the maximum peak load is almost the same, even after the specimens have been exposed to 120 °C for 60 minutes. The decrease of the peak load is of 7%, while the ultimate slip remained unchanged. This study showed that the use of FRCM reinforced with coated fabric is able to maintain a good shear-bond resistance even after being exposed to high temperature conditions. Temperatures up to 120 °C are not able to decompose the selected coating and after cooling the epoxy regains its integrity.

Figure 8. Double shear bond test: comparison between FRCM reinforced with dry and coated (HS) fabrics at different temperatures

Figure 9. Double-shear bond test: FRCM residual performance after exposure to high temperature (120 °C) for 60 minutes

Table 7. Double shear test results after exposure to 120°C
[according to RILEM TC250-CSM]

Mortar	Fabric	Temperature of testing (°C)		Peak Load (per side) f_{max} (N)	% change f_{max}	Slip at peak load (mm)	Peak stress in the textile $\sigma_f=f_{max}/A_f$ (MPa)
Mortar- 45	HS	20	Average	2503	-	4.18	802
			COV (%)	2		2	
		20 Aft.exposure	Average	2325	- 7	4.19	745
			COV (%)	4		4	

5. Numerical simulations and comparisons with experimental results

5.1 Parameters setting

We consider the simplified two-dimensional geometry of Fig. 5f, discussed in Sect. 3.1. Matrix and yarn domains are discretized by three-nodes triangular finite elements as shown in Fig. 10a. Young's modulus, Poisson's ratio and tensile strength of the two materials have been assigned as reported in Table 1 and Table 3. Since the aggregates in the cementitious mortar have a size of about 1-2 mm, we assign $B=5$ mm to the thickness of the process zone. Indeed, according to [47, 31], the characteristic thickness of the damage localization zone is typically 2-3 times the size of the constituent grains. Given E , σ_e and B , parameters d and l_m are determined from (5)_{1,2}.

Different constitutive parameters are assigned to the matrix-fiber interface to distinguish dry (DRY) and coated with sand (HS) carbon fabrics at different temperature exposure. These parameters have been assigned following an inverse approach, starting from global double shear bond curves (Fig. 8) and deriving the interface constitutive parameters. For sake of simplicity, we assume $k=k_x=k_y$ in the elastic tensor $\mathbf{k}$ in (6). Since experiments exhibit temperature-dependent mechanical responses, the interface constitutive parameters vary with temperature T , that is, $k=k(T)$, $\tau_e=\tau_e(T)$ and $q=q(T)$. Parameters k and τ_e define slope and extension of the d - τ_e elastic branch, while q describes the shape of the post-elastic branch. We recall that a in (6) is determined from k and τ_e by formula (9). A schematic description of the procedure followed to fix the interface material parameters is proposed in the Appendix.

Interface parameters - DRY carbon fabrics. To reproduce the brittle behavior observed in experiments (see Fig. 8a), we assign $q=-2$, whatever the temperature T . In this way, the interface brutally breaks when the limit elastic shear stress τ_e is reached (see Fig. 6). For k and τ_e , we fix $k(20)=1.6$ N/mm³, $k(120)=1.2$ N/mm³, and $\tau_e(20)=\tau_e(120)=1.7$ MPa (see Fig. 10b). For increasing T , k reduces, while τ_e maintains fixed.

Interface parameters - HS carbon fabrics. Temperature considerably affects the parameter values in the case of coated fabric, since the mechanical characteristics of the epoxy coating highly depends on thermal conditions. We assume $k(20)=1.0$ N/mm³, $\tau_e(20)=1.9$ MPa, and $k(120)=0.4$ N/mm³, $\tau_e(20)=0.75$ MPa (see Fig. 10b). Thus, temperature considerably reduces both the elastic coefficient and the shear strength. Since the experimental curves of Fig. 8b exhibit a pronounced post-elastic softening phase, curves of Fig. 6 suggest of choosing values of q within the range $(-2, 2)$. At $T=20^\circ\text{C}$, we set $q=0.3$, which accounts for a residual shear strength

$\tau_r = 0.68$ MPa at the shear displacement $\delta_r = 4\delta_e = 7.6$ mm (black dot in Fig. 10b). At $T = 120^\circ\text{C}$, we set $q = 0.7$. In such a way, at the shear displacement $\delta_r = 4\delta_e = 7.5$ mm, the residual shear strength is $\tau_r = 0.39$ MPa (red dot in Fig. 10b).

For both the HS and DRY samples, we assume $l_s = 1$ mm.

5.2 Results and comparisons

Simulations are conducted by increasing the vertical displacement δ , and computing the corresponding vertical normal stress σ_y on the yarn upper side. These quantities are related to the overall displacement s and force f (see Fig. 8), measured in the experiments and reported in the curves of Fig. 8, by means of the relations

$$s = \delta + \frac{h_y}{E_f} \sigma_y, \quad f = 3\sigma_y A, \quad (17)$$

where $h_y = 310$ mm is the length of the fabric part which connects the sample to the experimental pulling device, E_f is the yarn Young's modulus, and A is the yarn cross-section area. In (17)₁, the second term in the right-hand side is the displacement due to the elastic deformation of the fabric, and, in (17)₂, the factor 3 accounts for the number of yarns in a fabric.

The force-displacement curves given by the numerical simulations are drawn in Fig. 8 (solid line) and compared with the experimental curves (dotted line).

Results - DRY carbon fabrics. As expected, DRY_20C and DRY_120C samples exhibit a brittle behavior. The matrix-yarn interface experiences debonding when the limit shear stress τ_e is attained, while the cementitious matrix never damages. The evolution of the damage α and shear stress τ_y for increasing δ is described in Fig. 11. The δ - f curves plotted in Fig. 11a exhibit steep and short softening branches, concluding with drops. Profiles of α and τ_e on the interface of the DRY_20C sample are plotted in Figs. 11b and 11c for different values of δ within the softening phase (dotted points in the enlargement of Fig. 11a). Damage forms in the upper part of the interface, when the limit shear stress τ_e is reached. Then it evolves downward, for almost a half of the interface. Finally, a brutal failure occurs, producing the total detachment of the yarn from the matrix. Fig. 11c shows that τ_y is equal to τ_e at the tip of the damaged zone, and it decreases within the damaged zone as α increases, being null there where $\alpha = 0$.

Results - HS carbon fabrics. Even in HS samples (with coated carbon fabrics), damage concentrates at the matrix-fiber interface, and the cementitious matrix maintains undamaged. Both at $T = 20^\circ\text{C}$ and 120°C , the s - f curves of Fig. 8 present softening branches which accurately fit the experimental curves. Damage evolution at the interface is described in Fig. 12 where snapshots of α and τ_y are represented at different values of s corresponding to the softening regime. In the two simulations, damage forms in the upper side of the interface when τ_y reaches the maximum value τ_e , and rapidly spreads all over the interface. Increasing s , damage almost homogeneously increases all over the interface, and, at $s = 0.7$ mm, the final damage values $\alpha_f = 0.64$ and 0.60 are reached at the interface of the HS_20C and HS_120C samples, respectively. The interface at the end of the experiments is not completely damaged, being α_f quite smaller than 1, and this provides residual strength sources to the system. A residual strength is also observed in the experiments. Indeed the curves of Fig. 8b present non-null values of f at their end. This strengthening at large displacement may be due to the augmented frictional effect produced by the coating.

Figure 10. (a) Mesh. (b) δ_y - τ curves for the calibration of the interface damage parameters.

Figure 11. (a) Displacement δ – force f curves for the DRY_20C and DRY_120C samples. Profiles of damage α (b) and shear stress τ (c) at the interface of the DRY_20C sample for different values of δ .

Figure 12. Profiles of damage α and shear stress τ at the interface of the HS_20C (a,b) and HS_120C (c,d) samples for different values of s [mm].

6. Conclusions

Based on the experimental results for specific materials presented herein, the following is concluded:

- FRCM systems can provide high temperature compatibility retaining mechanical performance when exposed to 120 °C depending on the type of fabric reinforcement used.
- FRCM reinforced with dry (uncoated) fabric seemed not to be influenced by the temperature conditions, maintaining an adequate resistance and bond to the substrate even when exposed to 120 °C for 100 minutes, when the temperature at the fabric to mortar interface was between 90 and 110 °C.
- FRCM reinforced with coated fabric showed drastic differences depending on the temperature of testing. The reduction in the FRCM ultimate tensile capacity was of 70% when tested at 80 °C. Same reduction was observed at 120 °C. Double shear bond tests showed a reduction in the ultimate peak load of 61% at 120 °C.
- FRCM with coated fabrics preheated to 120 °C for 60 minutes and tested at room temperature showed smaller differences in terms of mechanical performances. The decrease of the peak load was of 7% and no differences were detected in the ultimate slip. These results showed that the coating is able to maintain a good adhesion with the mortar when cooled down after being exposed to 120 °C for 60 minutes. Therefore, FRCM reinforced with coated carbon fabric can still maintain its structural function after the exposure to high temperatures, upon to 120 °C.
- Numerical simulations confirmed that for any temperature and fabric type, the main failure mechanism is by fabric slippage within the cementitious matrix.
- Double shear simulations on FRCM reinforced with DRY fabrics exhibit a top-down detachment at the matrix-fibers interface after reaching the maximum peak load. The

damage development occurs in the first 50mm of the bonded area and quickly evolves along the entire bond length up to failure.

- In presence of coated fabrics, the detaching mechanism is different from that observed in DRY fabrics. Indeed, damage almost homogeneously starts and slowly develops at the whole fabric-matrix interface. At the end of the softening phase, the interface is only partially damaged, and it is still able of bearing some shear stresses. This final residual strength accounts for material frictional sources.
- Although there are few results in literature regarding the FRCM behavior when exposed to high temperature conditions, some qualitative comparisons can be made. As experienced by Trapko, FRCMs have proven to behave better than FRP when exposed to high temperatures, maintaining an adequate load bearing capacity up to 80 °C [17]. The use of coated fabrics improved the FRCM mechanical performances but can be a limitation if the temperature within the FRCM exceeds the coating T_g . However, coated fabrics are able to recover the load bearing capacity when cooled down after being exposed to high temperatures (at least up to 120 °C for 60 minutes of exposure) and this result is in line with the experiments conducted by Silva and co-workers [22].

We conclude that the phase-field variational approach has revealed a promising approach for the study of the failure mechanisms in FRCM systems. Indeed, the proposed model, despite its geometrical simplicity, has shown great predictive capabilities, accurately reproducing the experimental results. A further advantage of the model is that it only depends on few parameters directly related to specific materials properties, which are easily measurable from experiments. Here they are determined following an inverse procedure, i.e., assigning those values that allow for a better fitting of the experimental response curves.

The use of FRCM as externally bonded reinforcement could be a valid solution to be adopted in case of applications where high temperature service conditions is a possible scenario. However, further tests on the mechanical behavior and durability of FRCM systems when exposed to these particular environmental conditions are necessary to better understand the phenomenon and provide guidelines for a proper design approach.

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APPENDIX

The procedure used to fix the model parameters is schematically drawn, and some examples are presented.

Parameters setting procedure. Assume that:

- (i) the experimental force-displacement curve is given. Here, as an example, the curve of Fig. 13 is considered, which is an HS_20 curve among the three HS_20 curves of Fig. 8b;
- (ii) the 2D geometry is defined according to the criteria given in Sect. 3.1;
- (iii) Young's modulus and Poisson's ratio of matrix and yarn E_m , ν_m , E_f , ν_f are given;
- (iv) splitting tensile strength σ_e of the matrix is known;
- (v) size B of the process zone in the mortar is assigned (typically 2-3 times the size of the cementitious aggregates);
- (vi) the internal length l_s in (6) is assumed equal to 1 mm; being related to the sliding process zone, its value is quite uncertain and thus it is fixed arbitrary. However, not-reported simulations have shown that different values do not modify the results.

The remaining constitutive parameters are deduced as follows:

1. the coefficients d and l_m in the matrix damage energy are determined from formulas (5)_{1,2};
2. the maximum elastic shear stress τ_e of the interface (see Fig. 6) is estimated from the maximum elastic force f_e of Fig. 13 by the formula

$$\tau_e = \frac{1}{3hb_3} \frac{\beta}{(\beta+1)} f_e, \quad (1A)$$

obtained from (1) and (17)₂, where h and b_3 are the geometrical lengths of Fig. 5;

3. the elastic coefficient of the interface springs is $k = \tau_e / \delta_e$ (see Fig. 6), which, use (17)₁, rewrites

$$k = \tau_e / \left(s_e - \frac{h_y}{3A} \frac{f_e}{E_f} \right), \quad (2A)$$

where quantities on the right-hand side are known (τ_e is determined at point 1, f_e and s_e are deduced from the experimental response curve (point i), E_f is known (point iii), and h_y and A are assigned geometrical quantities (point ii)). Formula (2A) is used to set k ;

4. once τ_e and k are estimated, coefficient a in (6) is determined from (9);
5. finally, the exponent q in (6), which controls the slope of the softening branch, is chosen via a fitting procedure, aimed at reproducing the experimental softening branch (Fig. 13).

Examples. Some examples are proposed, where the above procedure of parameters setting is followed.

We assume the experimental curve of Fig. 13 (point i), the geometry defined in Sect. 3.1 (point ii), the constitutive parameters of Tables 1 and 3 (points iii and iv), and $B=5$ mm (point v).

Following prescriptions given at points 1-4, we obtain: $d=0.0011$ MPa, $l_m=1.77$ mm (point 1); $\tau_e=1.9$ MPa (point 2); $k=1$ MPa/mm (point 3); $a=3.61$ MPa mm (point 4). For the softening exponent q of point 5, different values are considered in order to show the parameter influence on the post-elastic stress-softening behaviour. Numerical response curves corresponding to different q are drawn in Fig. 13. The slope of the softening branch reduces as q increases. In this case, the curve for $q=0.3$ allows for the best matching the experimental softening branch.

Figure 13. Force-displacement curves for different values of q .

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