Strain relaxation in epitaxial Ge crystals grown on patterned Si(001) substrates

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Abstract

In this paper we report on the defects formed in Ge crystals grown on Si(001) pillars upon strain relaxation. The analysis is performed by high-angle annular dark-field scanning transmission electron microscopy. The strain relaxation happens by means of 60° and 90° misfit dislocations with Burgers vectors $\vec{b}=\frac{1}{2} < 110 >$. Misfit dislocations may split forming partial dislocations with Burgers vectors $\vec{b}=\frac{1}{6} < 112 >$, and are separated by a stacking fault. Besides, intrinsic stacking faults in different {111} planes interact and annihilate each other forming stair rod dislocations. Coherent and incoherent twin boundaries of the $\Sigma 3\{111\}$ and $\Sigma 3\{112\}$ types are also found at the Ge.

Keywords: Dislocations; Stacking Faults; Twins; HAADFSTEM; Ge

When Ge layers epitaxially grown on Si substrates reach a critical thickness, the misfit strain is accommodated by misfit dislocations (MDs) at the interface with their half planes in the Si-substrate. The MDs are of 60° and 90° types with Burgers vectors $\vec{b}=\frac{1}{2} < 110 >$ lying in {111} planes and line direction along
5 [110]. The MDs are always accompanied by threading dislocations[1] (TDs)

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which cross the layers and end at the Ge surface. The TDs are of 60° -type lying in $\{111\}$ planes. Besides the TDs, planar defects have also been observed in Ge layers such as stacking faults (SFs) and twin boundaries (TBs) especially for low growth temperatures[2, 3, 4]. They are for example created at the interface
10 during the recrystallization of Ge [2] or during the coalescence of islands during the growth[4, 3].

As the performance of semiconductor devices is largely affected by dislocations, much effort is devoted to develop new methods for strain relief and to reduce the MD and TD densities. The approach pursued here is to grow three-dimensional
15 (3D) Ge crystals on Si substrates patterned at a micrometer scale (i.e. Si pillars). The crystals are grown by low-energy plasma enhanced chemical vapor deposition (LEPECVD) far from equilibrium at high rates of around $15 \mu\text{m/h}$ and substrate temperatures of about 500°C [5, 6]. At substrate dimensions in the micrometer range the misfit strain is not reduced much in comparison to planar substrates,
20 and MDs are still formed at the interface. However, the 60° TDs are eliminated because they end at the sidewalls of the Ge crystals[7]. Thus, the 60° TD density is reduced or even eliminated, depending on the height of the Ge crystals. Instead, new TDs are formed in the Ge which are identified as edge and screw dislocations with Burgers vectors $\vec{b}=\frac{1}{2} < 110 >$ and $\vec{b} = [001]$, respectively[11, 6, 12]. So far,
25 planar defects have not been reported in Ge crystals grown on Si pillars.

Based on transmission electron microscopy (TEM) and high-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM), the present work provides a detailed analysis of the defects formed to relax the misfit strain in Ge crystals grown on Si(001) pillars.

30 The Ge crystals were grown on Si(001)-pillars with dimensions $5 \times 5 \mu\text{m}^2$ and $8 \mu\text{m}$ in height[5]. TEM cross sectional samples were prepared by mechanical polishing, dimple grinding, and ion milling using a Fischione ion miller model 1050 with 3 and 2 kV Ar ions to achieve electron transparency. TEM observations were carried out using a JEOL 2200FS TEM/STEM microscope operated at
35 200 kV, and a double spherical aberration-corrected JEOL JEM-ARM200F microscope operated at 200 kV for the HAADF-STEM analysis. The latter

microscope was set up in STEM mode with a probe semi-convergence angle of 25.3 mrad and an annular semi-detection range of the annular dark-field detector of 90-370 mrad.

40 Figure 1(a) shows a HAADF-STEM image of the Ge/Si interface. It can be seen that the 4% lattice mismatch between the two materials is accommodated by the formation of MDs (white lines). The MDs are identified as pairs of perfect glissile 60° dislocations and perfect sessile 90° dislocations. The interface around the pairs is not smooth and steps of 2-3 atomic layers are observed. These steps
 45 are formed by the creation of the MDs at the interface that initially is flat[8]. In the pair of 60° , one of the 60° MD lies at the interface whereas the other is located in the Ge layer a few atomic layers above the interface; this is typical for films grown far from equilibrium[9]. The Burgers circuits of a pair of 60° MDs are shown in Figure 1(b), using the (finish-start right-handed) FS/RH
 50 convention[10]. The Burgers vectors, indicated by green arrows, are $\vec{b}=\frac{1}{2}[\bar{1}0\bar{1}]$ and $\vec{b}=\frac{1}{2}[011]$. Figure 1(c) shows the Burgers circuit and vector of a 90° MD; it is a Lomer dislocation lying in the (001) planes with $\vec{b}=\frac{1}{2}[\bar{1}10]$. The 90° MDs are formed by the interaction of two 60° MDs with Burgers vectors in different glide planes $\frac{1}{2}[\bar{1}0\bar{1}] + \frac{1}{2}[011] \rightarrow \frac{1}{2}[\bar{1}10]$. This reaction results in a reduction of the
 55 core and elastic energies ($a^2 > \frac{a^2}{2}$, where a is the lattice parameter). The 60° MDs are therefore strongly attracted to each other forming the 90° Lomer MD.

Besides MDs, a high density of planar defects was observed in the Ge crystals. Figure 2(a) shows a HRTEM image of the Ge/Si interface with planar defects with a density of up to $1 \times 10^6 \text{ cm}^{-1}$. They are located on $(1\bar{1}1)$ and $(1\bar{1}\bar{1})$
 60 planes and some of them look like pyramids with angles of 70.5° between them. These defects propagate along the $\{111\}$ planes with extensions between 3 to 40 nm. HAADF-STEM observations show that they are coherent twin boundaries (CTBs) of the $\Sigma 3\{111\}$ -type, as well as extrinsic and intrinsic stacking faults (ESFs and ISFs). The formation of these types of defects can be explained by
 65 island growth, impurities on the Si surface[13] or by splitting of 60° dislocations[9]. Figure 2(b) shows CTBs in a Ge crystal formed at the interface with an extension of 40 nm. The TBs are pointed by red arrows and the $\{111\}$ plane orientations

Figure 1: HAADF-STEM images of the Ge/Si interface: a) Ge/Si interface showing the position of the 60° and 90° MDs with white lines, b) Burgers circuits of the 60° MDs (in red and yellow arrows) and Burgers vectors (green arrows) and c) Burgers circuit of the 90° MDs at the interface.

are shown by the green and yellow lines, passing from grain A (GA) to grain B (GB) and then again to GA. The area between the two CTBs corresponds to 9 atomic layers of $\{111\}$ planes (2.94 nm, assuming $a=0.5676$ nm). The inset of Figure 2(b) shows the Fourier transform of the image. Here, the TB plane is $(1\bar{1}\bar{1})_{GA}=(1\bar{1}1)_{GB}$ (red circle), and the planes corresponding to the GA and GB are $(1\bar{1}1)$ and $(1\bar{1}\bar{1})$, respectively (green and yellow circles). The CTB ends inside the crystal (Figure 2(c)), forming an incoherent twin boundary (ITB) of the $\Sigma 3\{112\}$ -type which is perpendicular to the $\Sigma 3\{111\}$ -CTB. The planes forming the ITB are $(1\bar{1}1)$ and $(1\bar{1}\bar{1})$ forming 7, 5 and 6 rings along the boundary. It is not possible to observe the whole length of the ITB in this figure due to the overlap of grains A and B. Figure 3(d) shows an image of the CTB at the Ge/Si interface. Because this area is highly stressed, a clear observation of the atomic positions is not possible. Nevertheless, where visible, dumbbells are marked by red circles, single atomic columns with blue circles corresponding to partial dislocations (PDs) marked by yellow arrows, and continuous $(1\bar{1}1)$ planes are denoted by red lines. A twin is formed by the gliding of a group of Shockley PDs along parallel $\{111\}$ planes. The group of Shockley PDs are 30°

85 type since the Ge grows initially compressed[14]. The Ge and Si planes at the interface in the twin seem to form a TB along the Ge/Si interface. According to our observations the CTBs are created at the Si surface due to the small steps around the pairs of MDs or during the coalescence of islands during the growth of the buffer layer at low temperature. This shows that for growth by LEPECVD
 90 at 500°C, preferentially islands nucleate rather than a two-dimensional layer.

Figure 2: High resolution images of a Ge crystal: a) HRTEM overview image of the Ge/Si interface with planar defects, b) HAADF-STEM image of two CTBs and its FFT, c) ITB closing the CTBs, and f) Ge/Si interface at the CTB. Dumbbells are denoted by red dots and partial misfit dislocations (PMDs) with yellow arrows.

Figure 3(a) shows a HAADF-STEM image of the Ge/Si interface with a SF wherein the half planes of the of 60° MDs in the substrate are marked with white arrows. A PMD is marked by red line limiting a SF. The stacking sequence of the SF (Figure 3(b)) changes from AaBbCcAaBbCc... to AaBbCc**Bb**AaBbCc...,
 95 where the bold Bb is an extra plane. Therefore, SF is of extrinsic type because there is an extra plane. Since Ge is compressively strained on the (001)-Si pillars, the dissociation of a 60° MD at the interface into two PMDs and an ESF leads to a 90° PMD at the interface and a 30° PMD in the Ge crystal in the vicinity of

an additional perfect 60° MD[15, 16, 9]. The 60° MD is attracting the 90° PMD
 100 at the interface and repulsing the 30° PMD to the film[9]. Figure 3(a) shows
 the position of the Shockley 90° PMD (red lines) at the interface, and nearby
 there is a 60° MD. A 90° MD with an ESF is equivalent to a pair of 30° MDs
 with an ISF on the adjacent glide planes[16]. The reaction of the splitting of
 the MD is $\frac{1}{2}[101] \rightarrow \frac{1}{6}[1\bar{1}2] + \frac{1}{6}[211]$ which is favorable since there is a reduction
 105 of energy ($\frac{a^2}{2} > \frac{a^2}{3}$), where the first and the second terms are the 90° and 30°
 PMDs, respectively.

Figure 3: HAADF-STEM images of the Ge crystal: a) PMD and ESF created at the Ge/Si interface, b) stacking sequence of the ESF, c) SFs interaction, d) image of the vertex of the SFs, e) a SF bounded by two SPDs, and f) magnified image showing the stacking sequence of the ISF. PD cores are magnified in the insets in Figure 3(e), the colored dots are the atomic positions, the Burgers circuits and vectors are indicated by yellow and green arrows respectively.

We also observed interactions between SFs near the Ge/Si Interface. When
 two SF extend along the $\{111\}$ planes with an acute angle of 70.5° in between,
 they annihilate each other in vertices forming stair rod dislocations (SRDs)
 110 (Figure 4(c)) [10]. The SF1 and SF2 are created by the coalescence of islands

around MD pairs or, by the dissociation of a 60° or screw dislocations. The SFs are identified as intrinsic type (Figure 3(d)). The stacking sequence changes from AaBbCcAaBbCc... to AaBbCcBbCcAaBbCc... where an Aa plane is missing in both SFs. For the SRD identification, the Burgers vector is obtained
115 by the method described by Cottrell [17] for a dislocation at the boundary of two faults. It consists of two Burgers circuits, one constructed around the SF1 starting and finishing at the SF1, and the other one around the SF1 and SRD starting and finishing at the SF2 (dashed blue line). The Burgers vector of the SRD is the difference between them. The Burgers circuits and vectors of
120 both faults are depicted by yellow lines and by green arrows. The step of the Burgers circuit in the faulted area is like the one in the good material. The Burgers vectors are found to be in $\{111\}$ planes, the magnitude of the Burgers vectors is $\frac{1}{3}$ the distance of the projected lattice points along the $\langle 112 \rangle$ direction which correspond to 30° PDs[18]. They are Shockley PDs (SPDs) type with
125 $\vec{b}=\frac{1}{6}[211]$ and $\vec{b}=\frac{1}{6}[\bar{1}2\bar{1}]$, therefore the Burgers vector of the SRD is given by $\frac{1}{6}[211] + \frac{1}{6}[\bar{1}2\bar{1}] \rightarrow \frac{1}{6}[1\bar{1}0]$ which implies an energy reduction $\frac{a^2}{3} > \frac{a^2}{18}$.

The configuration of the Shockley PDs with an intrinsic SF present in compressively strained materials is 30° PD at the interface and 90° PD in the compressed film having small separations[16, 19]. Since the PDs forming the
130 SRD are two 30° , they are not formed by the splitting of a 60° MD. In order to have 30° PDs in the Ge, a screw MD splits into two 30° MPDs[18, 20]. Possible reactions of the splitting of the screw MDs[18] in the $\{111\}$ planes are $\frac{1}{2}[110] \rightarrow \frac{1}{6}[211] + \frac{1}{6}[12\bar{1}]$ and $\frac{1}{2}[110] \rightarrow \frac{1}{6}[211] + \frac{1}{6}[\bar{1}2\bar{1}]$, ($\frac{a^2}{2} > \frac{a^2}{3}$).

SFs inside the Ge crystals are also found but they are rarer than at the
135 interface. They are located above the interface ($\approx 20\text{nm}$) and bounded by two PDs. Figure 3(e) shows a HAADF-STEM image of a SF bounded by two PDs pointed by red arrows and separated by 2.63 nm. The general Burgers circuit (orange arrows) around the two PDs is a closed loop. This implies that Burgers vector is equal to zero along this projection indicating a null edge component.
140 The Burgers circuit for each PD is depicted by yellow arrows. The projection of the Burgers vectors closing the circuits are $\vec{b}=\frac{1}{6}\langle 112 \rangle$ (green arrows)

which correspond to SPDs. The core structures of the SPDs are shown in the insets of Figure 3(e) where a half plane is pointed by green arrow and a single atomic column is depicted by a red circle. The two cores are similar and
145 correspond to 30° type[21]. The magnitude of the Burgers vector of both PDs is $\frac{1}{3}$ the distance of the projected lattice points along the $\langle 112 \rangle$ direction which correspond to 30° PDs[18]. Since the general Burgers vector is zero, the splitting dislocation into SPDs is a screw dislocation. The Burgers vectors of the 30° SPDs correspond to $\vec{b}=\frac{1}{6}[211]$ and $\vec{b}=\frac{1}{6}[2\bar{1}\bar{1}]$. The splitting reaction is given by
150 $\frac{1}{2}[110] \rightarrow \frac{1}{6}[211] + \frac{1}{6}[12\bar{1}]$ [18, 22] implying again a reduction of energy $\frac{a^2}{2} > \frac{a^2}{3}$.

A magnified image of the stacking sequence is shown in Figure 3(f). The sequence of the atomic positions are shown by colored circles, where the normal stacking sequence AaBbCcAaBbCc... changes to AaBbCcAaCcAaBbCc... (Bb plane is missing), therefore, this fault is an ISF.

155 During the growth of the Ge crystals, Ge is also deposited on the sidewalls of the Si pillars producing an overgrowth area between the Ge in the sidewalls and the Ge crystal. CTBs are also found in this area with longer extension than those found at the interface (Figure 4). They are located at the edge of the Si pillars and glide along $\{111\}$ planes across the overgrowth area. They end
160 at the sidewalls or inside of the Ge crystals with an ITB of the $\Sigma 3\{112\}$ -type similar to Fig. 2(c)[23, 24, 25]. In Figure 4(a), the CTBs, marked by red arrows, correspond to $(1\bar{1}\bar{1})_{\text{GA}}=(1\bar{1}\bar{1})_{\text{GB}}$ planes. The plane orientation in the GA $(1\bar{1}\bar{1})$ and in the GB $(1\bar{1}\bar{1})$ is marked by green and yellow lines, respectively. The area between the two CTBs contain 48 $\{111\}$ -planes (15.68 nm). Figure 4(b) shows
165 the Fourier transform of the image in Figure 4(a), the TB planes correspond to $(1\bar{1}\bar{1})_{\text{GA}}=(1\bar{1}\bar{1})_{\text{GB}}$ (red circle), and the planes in GA and GB are $(1\bar{1}\bar{1})$ and $(1\bar{1}\bar{1})$, respectively (green and yellow circles). This image shows a periodicity of extra spots between the reflections (blue area). These extra spots are due to dynamical diffraction caused by the overlapping of the GA and GB grains. A
170 simulated diffraction pattern calculated by JEMS[26] is shown in Figure 4(c) for an epitaxial material (GA+GB) including double diffraction effects. This simulated diffraction pattern shows a good match with the image in Figure

4(b). The CTBs end inside the crystal by closing with an ITB (Figure 4(d)). The CTBs are marked by red arrows and the ITB by a blue arrow. The ITB plane corresponds to $(\bar{2}\bar{2}4)_{GA}=(\bar{2}\bar{2}4)_{GB}$ shown in the Fourier transform (FFT) with a blue circle, the red circle corresponds to the $(1\bar{1}\bar{1})_{GA}$ and $(1\bar{1}\bar{1})_{GB}$ planes crossing the ITB. The green and yellow circles are $(1\bar{1}\bar{1})$ in GA and $(1\bar{1}\bar{1})$ in GB forming the ITB. Figure 4(e) shows the ITB structure which is periodic and formed by one 5 ring, one 7 ring and one distorted 6 ring[23]. The single atomic columns are pointed by red circles and are located at the corners of the 6 and 7 ring (yellow rings) in agreement with the model proposed by Sawada for Si[23].

Figure 4: Images of the Ge deposited on the sidewalls on the Si pillars: a) HAADF-STEM image of two CTBs, b) Fourier transform of the image in panel (a), c) Simulation of the diffraction pattern of GA and GB in an epitaxial material, d) HAADF-STEM image of an ITB $\Sigma 3\{112\}$ and its FFT, e) Magnified image from the ITB of panel (d) showing 5, 7 and 6 rings at the boundary. Red circles show the position in the rings of the single atomic columns.

In conclusion, defects at the Ge/ Si interface were identified using HAADF-STEM analysis. The misfit strain in Ge crystals grown on (001)-Si patterned substrates is accommodated by MDs of 60° and 90° types lying on $\{111\}$ and $\{001\}$ planes. MDs split into SPDs bounding intrinsic or extrinsic SFs. The SFs annihilate when they meet each other different $\{111\}$ planes forming a SRD. $\{111\}$ -CTBs are also found in the Ge crystals. They are created at the interface

and end inside of the crystal with a $\{112\}$ -ITB.

Overall it can be concluded that the variety of 1D and 2D crystal defects
190 in Ge crystals epitaxially grown far from equilibrium is greater than previously
documented. The presence of these defects and the variety makes it difficult to
estimate their impact on the physical properties of the Ge crystals.

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