Noble Metal High Entropy Alloys

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Abstract

A series of noble metal high entropy alloys with up to six constituent elements has been produced by casting. PtPdRhIrCuNi forms single-phase face-centered cubic solid solution, and its stability is confirmed by annealing experiments. This alloy deforms homogeneously to ~30% to a high ultimate compression strength of 1839 MPa. We discuss rules for the formation of single-phase solid solution.

Keywords : High entropy alloys; FCC structure; solid solution; Compressive property; Phase Stability

In contrast to conventional alloys, which are typically composed of only one or two principal elements, high entropy alloys (HEAs), consist of five or more elements with (near) equiatomic concentration, which form single-phase solid solution (SPSS) [1-5]. This design strategy greatly increases the number of potential technologically relevant alloys [6, 7]. The mere combination of practical elements suggests vast numbers of potential HEAs. However, prediction of HEAs out of such vast numbers of potential alloys has been proven to be difficult [6, 7]. Predicting stable phases require the knowledge and comparison of the Gibbs free energy of all possible phases [8]. However, this is beyond today's computing power and hence assumptions for ΔH_{mix} , and ΔS_{mix} have been suggested [9-12] based on regular mixing behavior [9, 10, 13-16]. The entropy term has been estimated assuming random configuration contribution at equiatomic composition to $S_c = k \ln n$ (n : number of components) [1]. In the attempt to estimate the enthalpic contribution, pairwise ΔH_{mix} were considered [9, 10, 14, 16, 17]. The effect of mixing many elements is estimated through $\Delta H_{\text{mix}} = \sum_{i=1, j>i}^n 4\Delta H c_i c_j$ which is the weighted average of all ΔH , the pairwise enthalpy of mixing. For SPSS to form, it has been suggested from empirical considerations [9, 10] that this averaged ΔH_{mix} should be in the range from -11.6 to 3.2 kJ/mol [9]. However, deviation from this rule has been reported [9, 11, 15, 17], suggesting oversimplifications in the estimation of the enthalpic contribution. In addition to thermodynamics, geometric consideration similar to Hume-Rothery has been identified to be crucial in phase formation of HEAs [18, 19]. For the formation of solid solutions, it was suggested that the atomic size difference, δ , ($\delta = \sqrt{\sum_i^n c_i (1 - r_i / \sum_i^n c_i r_i)^2} \times 100$, where r_i is the atomic radius of the i^{th} atom) should be smaller than 6.6% [9].

Considering both thermodynamic and geometrical factors affecting phase formation, we report new HEA systems consisting of noble metals. We found for the noble metals HEAs that,

in addition to the weighted average ΔH_{mix} , enthalpy of mixing for individual pairs plays a vital role in phase formation.

We considered Au, Pd, Ag, Pt, Rh, Ir, Cu and Ni for potential alloy constituents. All of the elements are faced-centered cubic (FCC) forming elements as listed in Table 1. Binary (AuPd), ternary (AuPdAg), quaternary (AuPdAgPt), quinary (AuPdAgPtCu), and senary (AuPdAgPtCuNi and PdPtRhIrCuNi) alloys at equiatomic composition of approximately 10 g were produced by arc melting of high purity metals. The crystal structure and microstructure of the alloys were studied using X-ray diffraction (XRD) (Rigaku, SmartLab) and scanning electron microscopy (SEM) (Zeiss, Sigma VP) with backscatter electron (BSE). Chemical analysis was performed by using energy-dispersive X-ray spectrum (EDS) attached to SEM. Specimens of dimension of 2 x 2 x 4 mm for compression tests were electric-discharged machined from 3 mm cast samples. Compression tests were conducted using an Instron mechanical testing machine at a constant strain rate of 10^{-4} s^{-1} .

XRD patterns of the as-cast AuPd, AuPdAg, AuPdAgPt, AuPdAgPtCu, AuPdAgPtCuNi, and PdPtRhIrCuNi alloys are shown in Fig. 1. All peaks have been identified to be solid solutions of FCC structure (space group: Fm-3m). Formation of FCC phases can be expected because all constituent elements are FCC structures, corresponding solid solutions in every possible binary combination appear to form FCC structures upon solidification at equiatomic composition, and most of the constituent elements have similar physicochemical and thermodynamic parameters (Table 1 and Table S1), such as atomic radii (1.25~1.39 Å), Pauling electronegativity values (1.90~2.54) and valence electron numbers (9~11). Furthermore, for all considered alloys, δ is smaller than 6.6% and ΔH_{mix} is within the range of -11.6~3.2 kJ/mol (Table 1).

The XRD patterns exhibit, only one set of FCC diffraction peaks for AuPd, AuPdAg, and AuPdAgPt, suggesting that these alloys form SPSS. However, a second phase of FCC structure forms when Cu is added into AuPdAgPt as demonstrated by the additional set of FCC diffraction peaks in AuPdAgPtCu. Although both δ and ΔH_{mix} remain in the solid solution forming range after Cu addition, pairs of Pt-Cu and Pd-Cu have higher negative enthalpy of mixing compared to the other pairs (Table 2). This indicates that a significant deviation of individual pairs from the average can promote formation of secondary phases. In the attempt to cancel the effect of large negative ΔH from the Pt-Cu and Pd-Cu pairs, we added Ni which has a positive ΔH with Ag and Au (Table 2). This approach however is not successful, a two phase microstructure remains in AuPdAgPtCuNi (Fig. 1). This suggest that a mere consideration of average ΔH_{mix} may be insufficient in predicting SPSS, Instead we considered introducing pairs of moderately positive ΔH by substituting Au and Ag with Rh and Ir (Table 2). As can be seen in Fig. 1, only one FCC phase is present in PdPtRhIrCuNi.

Microstructures observed by SEM-BSE from the central parts of the as-cast samples are shown in Fig. 2(a) and (b) for AuPdAgPtCuNi and PdPtRhIrCuNi, respectively. The AuPdAgPtCuNi alloy shows a microstructure consisting of primary dendrite phases embedded in matrix phases of darker contrast. With length scale ranging from 5 to 10 μm , the dendritic phase is estimated to have a volume fraction about 10 to 20 %. These two phases correspond to the two FCC phases in XRD patterns. On the other hand, the single solid solution forming PdPtRhIrCuNi exhibits a completely dendritic microstructure, as shown in Fig. 2(b). The average size of primary arm is about 5 μm . Chemical analyses indicate that the dendrite is Rh and Ir rich, e.g. $\text{Pd}_8\text{Pt}_{13}\text{Rh}_{26}\text{Ir}_{34}\text{Cu}_6\text{Ni}_{13}$. The interdendritic region exhibit a varying composition with up to $\text{Pd}_{20}\text{Pt}_{21}\text{Rh}_{13}\text{Ir}_7\text{Cu}_{18}\text{Ni}_{21}$.

In general, there are two possible origins of the compositional variations in the microstructure; non-equilibrium solidification [2] and phase separation [20]. Under a higher diffusive condition, composition gradient should decrease to form a homogeneous SPSS for non-equilibrium solidification and increase for phase separation due to difference in thermodynamic driving force, as schematically illustrated in Fig. 3(a). In order to determine which scenario is present in PdPtRhIrCuNi, we conducted annealing experiments both below and above T_m of the alloy, with the evolution of the element distribution revealed by EDS mapping (Fig. 3(b)-(e)). In the as-cast state (Fig. 3(b)), the distribution of the elements is non-uniform with the dendritic region rich in Rh and Ir and poor in Pd and Cu. When being annealing at 1000 °C (Fig. 3(d)), element distribution becomes more uniform. Further increasing annealing temperature to 1200 °C results in further reduction of composition variations. However, increasing annealing temperature to 1400 °C (Fig. 3(e)) which is above T_s of the alloy, composition variation increases rapidly. To quantify the compositional difference between dendritic and interdendritic regions, we use $\Delta C_{\text{sum}} = \sum |C_{i,\text{bright}} - C_{i,\text{dark}}|$ as an indicator, where i represent the constituent elements so that less difference leads to smaller value of ΔC_{sum} . Fig. 3(f) shows the change of ΔC_{sum} with annealing temperature. The concentration changes for each element can be found in Supplementary Materials. As shown in Fig. 3(b), ΔC_{sum} decreases with increasing annealing temperature from 1000 °C to 1200 °C. At 1400 °C $> T_s$, ΔC_{sum} increases. The changes of ΔC_{sum} with annealing temperature suggest that the compositional variations in as-cast PdPtRhIrCuNi originate from non-equilibrium solidification and the alloy evolves into a homogenous in composition SPSS phase. To confirm if the alloy indeed develops towards a uniform composition FCC SPSS phase, we conducted another set of annealing experiments at constant temperature (1200 °C) for various annealing conditions from 2 hrs to 200 hrs, which can be

shown in Supplementary Materials. We found that the volume fraction of the bright phase gradually decreases as a function of time [21]. Our results indicate that the microstructure develops towards a homogeneous FCC SPSS phase when approaching equilibrium.

HEAs have been reported to possess a combination of high strength and ductility [4, 22]. To evaluate the mechanical property of the PdPtRhIrCuNi, we performed compression tests. As shown in Fig. 4(a), the yield strength, σ_y , of PdPtRhIrCuNi is 527 MPa, while the maximum strength, σ_m , is 1839 MPa. In comparison with previously reported HEAs that form FCC SPSS, the strength of PdPtRhIrCuNi is higher because of the “Cocktail effect” [3], originating especially from the high strength of Rh and Ir. According the stress-strain curve shown in Fig. 4(a), the strain to failure is 32.4 %, a value typical for FCC structured HEAs [23]. Fracture appears to occur along the maximum shear stress (Fig. 4(b)). As marked by arrows, numerous slip bands can be observed on sample surface, indicating the homogeneous deformation upon loading. In addition, the data show a dramatic solid-solution-like strengthening mechanism for the single-phase FCC alloy (PdPtRhIrCuNi) which is not present in the two phases alloy (AuPdAgPtCuNi).

In summary, we designed a noble metal HEA, PdPtRhIrCuNi. Annealing experiments reveal that the stability of a single-phase FCC solid solution. Mechanical characterization revealed a high ultimate compression strength of 1839 MPa and large ductility in excess of 30 %, suggesting the operation of a solid-solution-like strengthening mechanism. Comparisons of similar senary alloys revealed that average values for heat of mixing are insufficient in indicating the formation of single-phase solid solutions. By comparing two senary alloys that follow the phase selection criteria currently used for the design of HEAs, PtPdRhIrCuNi which forms a SPSS and AuPdAgPtCuNi which exhibits a two phase mixture, we found that the phase selection

is not fully predictable. We attribute the formation of dual phases in AuPdAgPtCuNi to the large pairwise heat of mixing.

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Figure 1. X-ray diffraction patterns of (a) AuPd, (b) AuPdAg, (c) AuPdAgPt, (d) AuPdAgPtCu, (e) AuPdAgPtCuNi, and (f) PdPtRhIrCuNi.

Figure 2. SEM-BSE morphologies at the central regions of the as-cast samples. (a)AuPdAgPtCuNi, and (b)PdPtRhIrCuNi.

Figure 3. (a) Situations that can result into compositional variations within the microstructure of alloys that are fabricated by non-equilibrium cooling. Decrease in total compositional difference within the microstructure upon subsequent annealing temperature below the solidus temperature, e.g., T_3 , suggest a stable single solid solution region. . Increasing ΔC with annealing is indicative of a spinodal in the system, e.g., at T_1 equilibrium situation comprises of two-phase mixture. (b)-(e) Elemental distributions obtained by EDS mapping for PdPtRhIrCuNi alloy: (b) as-cast, (c)-(e) annealed at 1000 °C, 1200 °C, and 1400 °C for 2 hrs. (f) $\Delta C_{\text{sum}} = \sum |C_{i,\text{bright}} - C_{i,\text{dark}}|$, an indicator of compositional difference between dendritic and interdendritic regions, as function of annealing temperature for of PdPtRhIrCuNi alloy. Detailed compositions of the two regions after each annealing can be found in Table S4.

Figure 4. (a) Compressive stress-strain curves for the PdPtRhIrCuNi alloy (red) and AuPdAgPtCuNi alloy (blue). (b)-(c) SEM images of the sample surface after compression test.

Table 1. Crystal structure, lattice parameter, a , atomic radius, r , and melting temperature, T_m , for considered elements.

	Au	Pd	Ag	Pt	Rh	Ir	Cu	Ni
structure	FCC	FCC	FCC	FCC	FCC	FCC	FCC	FCC
a , Å	4.078	3.891	4.085	3.924	3.803	3.839	3.615	3.524
r , Å	1.39	1.34	1.37	1.35	1.33	1.35	1.25	1.25
T_m , °C	1064	1555	962	1768	1964	2466	1085	1455

Table 2. List of atomic-size difference, δ , enthalpy of mixing, ΔH_{mix} , highest positive enthalpy of mixing ΔH_{max} , and highest negative ΔH_{min} .

alloys	δ [%]	ΔH_{mix} [kJ/mol]	ΔH_{max} [kJ/mol]	ΔH_{min} [kJ/mol]
AuPd	2.49	0	0	0
AuPdAg	2.33	-5.78	0	-7
AuPdAgPt	2.19	-2.00	4	-7
AuPdAgPtCu	4.25	-6.56	4	-14
AuPdAgPtCuNi	5.39	-2.22	15	-14
PdPtRhIrCuNi	3.71	-2.56	6	-14

PdIrCu
HEA
RhPtNi

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Graphical abstract