2D

3D

$(\theta_w, \varphi_w, \zeta_w)$	$(r_{wobj}, \theta_{wobj}, \varphi_{wobj})$
$(42^\circ, 50^\circ, 60^\circ)$	$(15 \text{ mm}, 18^\circ, 0^\circ)$
$(55^\circ, 19^\circ, 22^\circ)$	$(11 \text{ mm}, 14^\circ, 0^\circ)$
$(62^\circ, -28^\circ, -8^\circ)$	$(14 \text{ mm}, 17^\circ, 0^\circ)$
$(r_{hobj}, \theta_{hobj}, \varphi_{hobj})$	
$(23 \text{ mm}, 51^\circ, 28^\circ)$	
$(21 \text{ mm}, 51^\circ, 3^\circ)$	
$(24 \text{ mm}, 51^\circ, -32^\circ)$

Whisking mechanics and active sensing

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Abstract:

We describe recent advances in quantifying the three-dimensional (3D) geometry and mechanics of whisking. Careful delineation of relevant 3D reference frames reveals important geometric and mechanical distinctions between the localization problem (“where” is an object) and the feature extraction problem (“what” is an object). *Head-centered* and *resting-whisker* reference frames lend themselves to quantifying temporal and kinematic cues used for object localization. The *whisking-centered* reference frame lends itself to quantifying the contact mechanics likely associated with feature extraction. We offer the “windowed sampling” hypothesis for active sensing: that rats can estimate an object’s spatial features by integrating mechanical information across whiskers during brief (25 – 60 ms) windows of “haptic enclosure” with the whiskers, a motion that resembles a hand grasp.

1. Introduction

The rodent vibrissal-trigeminal system is one of the oldest models for the study of active sensing in the field of neuroscience [1,2,3,4,5]. The past five years have seen several breakthroughs in the field of vibrissal research, including the discovery of the central pattern generating circuits responsible for rhythmic whisking [6] and their close association with sniffing behavior [6,7], as well as the elucidation of differential processing along parallel thalamocortical pathways [8,9]. However, we still do not fully understand how to interpret the signals in these central structures, in part because we do not yet fully understand the inputs: the tactile signals that drive the responses of primary sensory neurons in the trigeminal ganglion.

Recent advances in three-dimensional (3D) whisker mechanics [10,11**,12,13*] offer the opportunity to compute the complete set of tactile inputs transmitted by the vibrissae during active tactile exploration. The goal of the present paper is to review recent literature so as to establish a unified framework for describing the geometric and mechanical variables relevant to whisking behavior. Specifically, we develop formalisms for head-centered and whisker-centered reference frames and compare them with the more traditional resting-whisker reference frame. The whisker-centered reference-frame is well suited to describe mechanical information about the external world transmitted by the whisker, but it is geometrically unintuitive. The resting-whisker reference frame is well suited to describe the location of an object relative to a particular whisker, but is ill suited to describing mechanical variables and mechanoreceptor deformation.

By carefully distinguishing between these reference frames, we argue that a whisking rodent will face two separate problems during tactile exploration. The first is how to localize an object in head-centered coordinates based on tactile information that originates in whisker-centered coordinates (“where” is the object). The second is how to integrate information across multiple whiskers to estimate the object’s contour, independent of its location in head-centered coordinates (“what” is the object). In this review we focus on the rat whisker system, but the framework also applies to mice and other rodents.

2. The geometry of whisking

Whiskers are arranged in a regular array (rows and columns) on the rat’s face, and decrease in length from caudal to rostral (Fig 1AB). Each whisker has an intrinsic curvature that follows from approximating its proximal shape by a parabola [12,14]. Intrinsic curvature varies systematically across the array (Fig 1B); shorter whiskers tend to have larger curvature than longer whiskers and also a more variable curvature across whiskers [15].

Each whisker is held tightly within a follicle at its base [16,17]. Each follicle is packed with mechanoreceptors, and is actuated by both intrinsic and extrinsic muscles [18,19,20,21,22,23]. Whisking behavior allows rodents to move their whiskers independently of the head, and it is therefore important to distinguish between head-centered and whisker-centered reference frames.

Because each whisker is held tightly by its follicle [16], and because the base of a whisker is relatively stiff [15,24,25,26,27,28], the follicle and the proximal segment of the whisker move approximately as a single unit (a

rigid body) relative to the head. Figure 1C describes the time-dependent position and orientation of this unit in a head-centered reference frame.

The two-step process depicted in Figure 1C – namely, a translation of the head-centered reference frame to the location of the whisker basepoint and a rotation that aligns the translated reference frame to the proximal segment of the whisker – describes the location and orientation of the whisker with respect to a head-centered reference frame. This process results in the two new reference frames shown in Figure 1D: a resting-whisker reference frame and a whisker-centered reference frame.

For the resting-whisker reference frame, the rotation considers the whisker at biomechanical rest and aligns the x'' -axis with the proximal segment of the whisker as it emerges from the mystacial pad. The y'' -axis is perpendicular to the x'' -axis, with positive defined as the direction in which the tip curves concave forward. This reference frame is now fixed. In contrast, the whisker-centered reference frame moves with the whisker. In this frame, the whisker always lies in the x'' - y'' plane and is tangent to the x'' -axis at its base.

This approach can be extended to the full three-dimensional (3D) case. In 3D, the base point coordinates (r_{bp} , θ_{bp} , ϕ_{bp}) for the translation include an additional angle, the elevation angle ϕ_{bp} . In 3D, three angles (θ_w , ϕ_w , ζ_w) are needed to characterize the rotation, where θ_w is the horizontal angle, ϕ_w is the elevation angle, and ζ_w is the roll of the whisker around its own tangent at the base [12,14,29].

The angle θ_w is measured in a horizontal plane and the angle ϕ_w in an elevation plane, both oriented relative to the plane that defines the pitch of the rat's head. In physiological experiments, zero head pitch is defined by aligning bregma with lambda. An alternative, appropriate in the context of some biomechanical and behavioral experiments, is to define zero pitch such that the basepoints of the whiskers lie in horizontal rows [14], or such that the two eyes and the nose lie in the horizontal plane [12]. Each choice offers distinct advantages and disadvantages, depending on the experimental questions asked. Once the zero head pitch plane, and thus the horizontal plane, has been identified, the elevation plane can be computed from projecting the whisker onto the horizontal plane: the tangent to the real whisker at its base and the tangent to the projected whisker at its base define the elevation plane.

Finally, it is important to recall that all of these coordinates, (r_{bp} , θ_{bp} , ϕ_{bp}) and (θ_w , ϕ_w , ζ_w), are functions of time, as they describe the position and orientation of the whisker's base in the head-centered reference frame.

The position of an object relative to the rat can be described in any of the three coordinate systems of Fig 1CD: the head-centered, the resting-whisker, or the whisker-centered reference frame. Throughout the present work, we assume the object to be a vertical peg, as is often used in behavioral experiments [30,31,32,33]. For simplicity, the peg is assumed to have infinitesimally small radius, as if it were a line segment.

Object coordinates in each of these three reference frames are illustrated in Fig 2. Object location in the head-centered reference frame is self-explanatory; the position of the object in this frame does not depend on how the whisker moves. The other two reference frames require a few additional notes.

First, if the basepoint location (r_{bp} , θ_{bp} , ϕ_{bp}) changed with time, the origin of these two reference frames and the object coordinates in these two reference frames would translate accordingly. For the pure rotational motion illustrated in the examples of Fig 2, basepoint translation can be neglected; 2D object coordinates in the resting-whisker reference frame (r_{rwobj} , θ_{rwobj}) thus remain constant during the whisk. In contrast, while r_{wobj} also remains constant in the whisker-centered reference frame, θ_{wobj} changes continuously and becomes negative after significant deflection against an object. Note also that as the whisker makes contact with and deflects against the object, its 2D rotation from the onset of contact is measured by a new angle, θ_{push} . If the whisker were perfectly straight, θ_{push} would be equal and opposite to θ_{wobj} , but because the whisker has intrinsic curvature, their relationship is more complicated and depends on the radial distance r_{wobj} .

Finally, we note that the characterization of object location from any of the three reference frames is easily extended to the 3D case; this simply requires an additional angle for elevation relative to the corresponding horizontal plane, namely $(r_{hobj}, \theta_{hobj}, \phi_{hobj})$, $(r_{wobj}, \theta_{wobj}, \phi_{wobj})$, or $(r_{obj}, \theta_{obj}, \phi_{obj})$. See Section 4 for a more detailed analysis of the unexpected subtleties of 3D object location.

3. The mechanics of quasi-static contact

When the whisker makes contact with an object, a mechanical transient is generated (a dynamic effect), and the whisker begins to bend. The quasistatic forces associated with bending are slower, but generally larger in magnitude than the transient forces associated with the collision [34,35,36]. Fig 3AB provide 2D and 3D illustrations, respectively, of the mechanical signals at the base of the whisker generated by contact [11,24,33,37,38,39,40,41].

Mechanical signals at the whisker base cannot be directly measured, because placing a sensor at the whisker base would interfere with its mechanics. Quantifying these contact variables requires either mechanical modeling [10,15,28,33,37,38,39,42,43,44**] or the use of geometric proxies. For example, change in curvature near the whisker base during contact is sometimes an appropriate proxy for change in bending moment at the whisker base [45*,46]. The quality of the proxy will depend on the exact method by which changes in curvature are computed (e.g., computing a spline vs. fitting a circle near the whisker base). Moreover, whenever the curvature is not computed precisely at the base, its actual value will depend on the somewhat subjective choice of a point “near the base” at which the curvature is computed.

As noted, the diagrams in Fig 3AB use the whisker-centered reference frame; it is in this coordinate system that mechanical signals are transmitted to the follicle. To clarify this point, consider the whisker’s location relative to mechanoreceptor endings within the follicle (Fig 3C). Mechanoreceptors respond to deformations caused by the motion of the whisker within the follicle. These deformations activate Vg neurons, the “gatekeepers” of all vibrissal-related information to the trigeminal pathway [44,45,47,48,49,50,51,52,53,54,55,56**]. A meaningful physical description of how mechanoreceptors will deform, and thus how Vg neurons will respond, requires a reference frame in which the location of the mechanoreceptor relative to the whisker does not change as the whisker moves. Vg response to mechanical stimuli thus requires that these stimuli be characterized in the whisker-centered reference frame.

4. The location of whisker-object contact points from different reference frames

How might the rat localize an object in the context of reference frames and variables described above?

Consider a rat whisking against a peg situated at two different horizontal angles ($\theta_{hobj} = 51^\circ$ and $\theta_{hobj} = 79^\circ$) relative to its snout (Fig 4A and 4B, at time of initial contact). A 2D view from the top, further simplified by neglecting whisker curvature (see insets at top left), correctly indicates that all whiskers caudal to the peg will make contact with the peg at a single horizontal angular location in the head-centered reference frame (θ_{hobj}). However, the 2D view gives the misleading impression that there is a simple relationship between the angular location θ_{hobj} of the object in the head-centered reference frame and the angle θ_w through which the whisker must rotate in order to make contact with the object.

The 3D views reveal considerable more complexity. All three whiskers make initial contact with the object at different values of θ_w , ϕ_w , and ζ_w , because the orientations of each of the whiskers are different in the head-centered reference frame. Note that although θ_{hobj} differs by exactly 28° between Figs 4A and 4B, the θ_w values for the whiskers do not shift by 28° . The complex relationship between θ_w and θ_{hobj} is due to the intrinsic curvature of the whiskers.

In whisker-centered coordinates, all whiskers have different values of r_{wobj} and θ_{wobj} at the time of initial contact, while ϕ_{wobj} is identically zero because the whiskers have not deflected out of their individual x-y planes. Also note that in head-centered coordinates, the coordinates of the whisker-object contact point r_{hobj} and ϕ_{hobj} are different

for each whisker, while θ_{hobj} stays constant because the peg is assumed to have infinitesimally small radius. If the peg had finite radius, then θ_{hobj} would change as the whisker slips along its length; this type of motion is termed “longitudinal slip” [22,37,38,39,41,42].

Fig 4C and 4D depict the geometry of contact after all whiskers have protracted against the peg until θ_w has increased by 10° . Roll (ζ_w) and elevation (φ_w) change with θ_w according to the kinematic equations for whisking motions developed by Knutsen et al., 2008 [12]. After this protraction, the coordinates ($\theta_w, \varphi_w, \zeta_w$) of whisker orientation relative to the head have changed, as have the coordinates ($r_{\text{wobj}}, \theta_{\text{wobj}}, \varphi_{\text{wobj}}$) of the object in the whisker-centered reference frame. The value of φ_{wobj} is no longer zero, because the whiskers have now deflected out of their initial planes.

It is interesting to note that the location of the whisker-peg contact points have also changed in the head-centered reference frame, both from whisker to whisker and during the protraction. These changes may seem unintuitive, because the location of the peg does not change relative to the head. Nevertheless, the location of the whisker-peg contact points have changed because the whiskers slip against the peg, both vertically and along their length. In this example, the peg is assumed to have vanishingly small radius, and the value of θ_{hobj} changes with protraction but not from whisker to whisker. In contrast, both r_{hobj} and φ_{hobj} change considerably from whisker to whisker but less so as a given whisker protracts against the peg. If the peg had finite radius, θ_{hobj} would also vary considerably from whisker to whisker.

The panels of Fig 4 summarize the significant challenges of the 3D object localization problem for the rodent, and also implicitly reveal an important “where/what” distinction in the vibrissal system. In panels 4A and 4B, the animal must localize the peg at two different angular positions. In panels 4C and 4D, as the whiskers deflect against the object the animal should have the same perception of the contour of the peg, regardless of whether the whiskers made contact with the peg at 51° or 79° .

Our approach to this problem is based on the observation that object location (“where” is the object) is most easily expressed in the head-centered or resting-whisker reference frames. In contrast, it is the whisker-centered reference frame that provides an optimal and most natural frame for the calculation of the contact forces and moments that lend themselves to a description of object contour (“what” is the object). In the next section, we examine the sources of information available to the animal for determining object location as well as object contour.

5. Where vs. what: determining object location and contour

Consider first the problem of localizing the peg at either 51° or 79° (Fig 4AB). Both the resting-whisker and the head-centered reference frames lend themselves to an intuitive description of object location [30,31,32,33,57,58,59]. To localize an object, the rat must detect the mechanical transients generated by collision with an object, determine the location of its whisker at the instant of contact, and determine the location along the whisker at which contact was made.

However, determining the whisker’s location at the instant of object contact is challenging because there are very few proprioceptors in the whisking muscles [9,17]. The rat has thus no direct access to ($\theta_w, \varphi_w, \zeta_w$), though some information may be available through the mesencephalic nuclei [60,61]. Recent studies have suggested that reafferent signals reporting whisking phase could be combined with an efferent copy of whisking midpoint and amplitude to estimate angular whisker position θ_w [62,63,64]. Given that the elevation and roll of the whisker are tied closely to protraction angle [12,29], the full 3D angular position of the whisker ($\theta_w, \varphi_w, \zeta_w$) at the time of contact could in principle be determined.

Several excellent review articles have recently surveyed the neurophysiological basis for the implementation of this type of localization scheme [57,58,65,66]. From a purely mechanical standpoint, this localization approach is plausible because the whisker has very little mass, and its proximal region behaves like a rigid body during

non-contact whisking [12,29]. The rat would thus be able to monitor and control purely kinematic variables (i.e., phase, midpoint, amplitude) to obtain an estimate of whisker position during localization behaviors. However, this localization scheme requires precise timing information to allow the computation of θ_w at time of contact. Moreover, values of θ_w must be monitored separately for each whisker.

A complementary hypothesis emerges from considering 3D geometric and mechanical effects. Because the whisker rolls as it protracts, the orientation of the whisker varies systematically through the whisking cycle [12,29]. In turn, the whisker's orientation at the time of object contact will determine the direction in which it is deflected by the object [10,11,13,41,42]. The direction of whisker bending could thus provide a mechanism for the rat to determine the horizontal angle at which the whisker has made contact with the object [12,13].

Consider next the problem of extracting the contour of the peg. In principle, the rat could determine object contour by computing the location of each whisker-object contact point in head-centered coordinates; this would be done in the manner just described for object location (whisking phase, timing, etc...). The contour of the object could then be determined by comparing these contact point locations – in head centered coordinates – across the array of whiskers. Although this scheme cannot be ruled out, it is computationally expensive and error prone, because the correct computation of object contour would depend on the correct computation of several object locations.

An alternative possibility is suggested by Figure 4CD, which indicates that after object contact, a new source of information becomes available to the animal: the contact forces and moments at the base of each whisker. The signals associated with contact mechanics tend to be much larger than the signals present during non-contact whisking [34,35,45,53,67,68,69]. Given the spatial invariance of a mechanoreceptor with respect to the follicle (Figure 3), the deformation of mechanoreceptors associated with contact is optimally expressed in whisker-centered coordinates. Two recent studies indicate that this mechanical information is indeed encoded by primary sensory neurons of the trigeminal ganglion [44,45].

We therefore propose that – just as during human exploration with fingertips [70] – the rat exploits contact mechanics to determine object features such as contour. Although very few studies have examined whisker-object contact patterns, a few recent experiments provide clues as to how this computation is enabled by whisker motions.

First, several studies have indicated that as rats perform haptic exploration tasks, they gradually increase contact durations with the object [71,72,73]. Mechanically, this would have the effect of damping out vibrations associated with object collision and ensuring that the whisker enters a quasistatic regime in which bending is the dominant effect [28,34,35]. In 2D, the mechanical signals associated with bending have been shown to uniquely represent the whisker centered geometry (r_{wobj} , θ_{wobj}) [43]. Moreover, recent work from our laboratory [13] strongly indicates that a subset of forces and moments at the whisker base will also be sufficient to represent (r_{wobj} , θ_{wobj} , φ_{wobj}).

Second, studies on orienting behavior have shown that rats tend to position their heads so as to maximize the number of whiskers in contact with a surface, given the expected orientation of the surface [74,75]. The tendency to maximize the number of whisker-object contacts suggests that the integration of information across multiple whiskers will play an important role during contour extraction.

Finally, a recent study employed a light sheet to directly visualize whisker-object contact patterns as naïve rats freely explored a flat, vertical surface [76*]. Results showed that every whisk exhibited brief windows during which many whiskers collectively made sustained (25 – 60 ms) contact with the surface. The number of whiskers in contact depended strongly on the pose of the head, but averaged around 15 to 20. Furthermore, during this contact window (termed the “sustained collective contact interval,” or SCCI), all whiskers converged and moved more slowly on the surface.

Taken together, we interpret these studies to suggest that the rat employs a strategy of “windowed sampling” during object exploration. As opposed to relying primarily on inter-vibrissal phase or timing cues to extract object spatial features (e.g., contour), the rat spatially integrates across whiskers the mechanical signals acquired during the SCCI. These mechanical signals can thus provide information about object identity through an integrative computation that does not depend on the object’s location in head-centered coordinates.

6. Conclusions

Three-dimensional investigation of vibrissotactile exploratory behavior is experimentally challenging, and simulations of 3D vibrissal geometry and mechanics are complex. Yet a 3D approach is critical if we are to begin understanding the input signals that drive activity at more central levels of the trigeminal system [10,11,13,51,54]. As the field progresses in its understanding of 3D mechanics, geometry, and vibrissal-object contact patterns, it will be essential to ensure a systematic notation for each of the reference frames relevant to quantifying input variables.

In particular, the head-centered and resting-whisker reference frames naturally lend themselves to a description of object location, while the whisker-centered reference frame provides a natural description of mechanics. We further suggest that by exploiting contact mechanics, the animal could obtain estimates of contact point location within the whisker-centered reference frame; object contours can then be determined by integrating mechanical information across vibrissae during a brief (25 to 60 ms) window of quasi-static deflection that lasts only a fraction of the whisk. We posit that rats perform a “haptic enclosure” [77,78] with their whiskers, similar to a grasping motion of the human hand.

Although this article has implicitly raised a host of interesting questions about the neural representations of these coordinate systems, we can only offer speculative ideas as to how and where those neural representations would emerge. By analogy to reaching and grasping [79], we suggest that rodents may employ a variety of reference frames (head-centered, unilateral-array centered, whisker-centered) depending on their behavioral goals. Some evidence for task-specific coordination of head and whisker movements has recently emerged in freely behaving mice [80**]. We suggest that a careful consideration of whisking motions may make the rodent system an excellent model for the study of neural transformations between reference frames, a choice that would complement work in primates.

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Figure captions

Figure 1. Arrangement of the whiskers on the mystacial pad and reference frames relevant to whisking mechanics. **A)** The whiskers of the rat mystacial pad are organized in rows and columns. **B)** Whisker length and curvature vary systematically across the array. **C)** Panels illustrate a two-step process to transform between head-centered, resting-whisker, and whisker-centered reference frames. The translation moves the origin from the snout to a whisker basepoint with polar coordinates (r_{bp} , θ_{bp}) in the head-centered reference frame; θ_{bp} is measured counterclockwise from the midline. The rotation results in a new reference frame in which the proximal segment of the whisker lies in the x'' - y'' plane and is tangent to the x'' -axis at its base. The y'' -axis is perpendicular to the x'' -axis, with positive defined as the direction in which the tip curves concave forward. **D)** The resting-whisker reference frame does not rotate with the whisker. In contrast, the whisker-centered reference frame rotates with $\theta_w(t)$.

Figure 2. Object coordinates in the head-centered, resting-whisker, and whisker-centered reference frames. Here we drop the double prime notation used in Fig 1 to refer to the axes in the resting-whisker and whisker-centered reference frames. Object location in the *head-centered reference frame* (h) does not depend on the motions of the whisker. The *resting-whisker reference frame* (rw) stays fixed as the whisker rotates; object coordinates do not change during whisker motion. The angle θ_{push} measures the change in θ_w from the onset of contact. The *whisker-centered reference frame* (w) rotates with the whisker; the angular location of the object changes continuously, both before and during contact. As in the resting-whisker reference frame, θ_{push} measures the change in θ_w from the onset of contact. In both resting-whisker and whisker-centered reference frames, whisker position at rest is shown as a thick grey dashed line, whisker position at contact as a thin grey dashed line, and whisker position when protracting against the object as a thin black line.

Figure 3. Mechanical signals in the whisker-centered reference frame. **A)** The 2D applied force $\mathbf{F}$ is decomposed into an axial component F_x along the whisker's axis and a transverse component F_y . The bending moment M_z at the whisker base has magnitude $|M_z| = r_{\text{wobj}} |F_y|$. **B)** The 3D applied force is $\mathbf{F}$ decomposed into an axial component F_x and two transverse components F_y and F_z . The bending moment $\mathbf{M}$ at the whisker base is $\mathbf{M} = \mathbf{r}_{\text{wobj}} \times \mathbf{F}$. Contact point coordinates in the whisker-centered frame are $(r_{\text{wobj}}, \theta_{\text{wobj}}, \phi_{\text{wobj}})$. **C)** During a protraction, the follicle and the whisker base rotate and roll as a single unit. The deformations on a mechanoreceptor (green dot) within the follicle are computed in the reference frame of the whisker. Whisker-centered coordinates maintain the geometric relationship between the whisker base and any given mechanoreceptor within the follicle at all times during a protraction. Resting-whisker coordinates cannot achieve this invariance because they are fixed in a single angular location, corresponding to the start of protraction.

Figure 4. The geometry of contact. **A and B)** The figures depict a rat whisking against a peg situated at two different horizontal angles relative to its snout: $\theta_{\text{hobj}} = 51^\circ$ and $\theta_{\text{hobj}} = 79^\circ$. Whisker angular coordinates in the head-centered reference frame, and contact point coordinates in both whisker-centered and head-centered reference frames, are shown for three different whiskers (red, green, and blue). **C and D)** Whisker angular coordinates and contact point coordinates in the same reference frames and for the same three whiskers, after all three have protracted against the peg until θ_w has increased by 10° . The changes in roll (ζ_w) and elevation (ϕ_w) with θ_w were simulated according to the kinematic equations for whisking motions developed by Knutsen et al., 2008 [12].

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A

B

C

The origin of the (x,y) frame is at the snout. The y -axis is aligned with the rostrocaudal midline.

The origin is translated to the whisker basepoint, resulting in the (x',y') frame.

The (x', y') frame is rotated to align with the proximal segment of the whisker as it emerges from the mystacial pad. In 2D, this rotation involves only θ_w .

D

In the resting-whisker frame, the x'' -axis is tangent to the resting whisker at its base. The proximal segment of the resting whisker lies in the (x'',y'') plane. This reference frame does not move with the whisker.

The whisker-centered frame follows the whisker in its rotation by $\theta_w(t)$. The x'' -axis follows the tangent to the whisker at its base. The proximal segment of the resting whisker lies in the (x'',y'') plane. This reference frame moves with the whisker.

Time 1

Time 2

Time 1

Time 2

Figure 2

Head-centered reference frame

2D object coordinates are $(r_{hobj}, \theta_{hobj})$.

3D object coordinates are $(r_{hobj}, \theta_{hobj}, \phi_{hobj})$. The elevation angle ϕ relative to the (x,y) plane is shown for two different contact points.

Resting-whisker reference frame

2D object coordinates are $(r_{rwobj}, \theta_{rwobj})$.

Radial distance is measured from the whisker basepoint to the location of the object. Angular object location does not change as the whisker rotates through θ_w .

As the whisker protracts against an object, the angle θ_{push} measures the change in θ_w from onset of contact.

Whisker-centered reference frame

2D object coordinates are $(r_{wobj}, \theta_{wobj})$.

Radial distance is measured from the whisker basepoint to the location of the object. Angular object location changes as the whisker rotates.

As the whisker protracts against an object and deforms, the x-axis continues to track the tangent to the proximal segment of the whisker. The angle θ_{push} measures the change in θ_w from onset of contact.

Figure 3

A

B

C

Protraction against an object at $\theta_{obj} = 51^\circ$

At time of contact

After θ_w increases by 10°

Protraction against an object at $\theta_{obj} = 79^\circ$

At time of contact

After θ_w increases by 10°

Figure 4