Semi-supervised Selective Ensemble Learning Based On Distance to Model for Nonlinear Soft Sensor Development

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Abstract: Data-driven soft sensors have been widely used in process systems for delivering online estimations of hard-to-measure yet important quality-related variables. However, in many data-driven soft sensor applications, the process may be strongly nonlinear, and the number of labeled samples is limited, which are two major difficulties in developing high-accuracy soft sensors. To cope with this issue, a novel soft sensing method based on semi-supervised selective ensemble learning strategy is proposed. In the proposed method, the process is initially localized by an adaptive process state partition approach, where the information of unlabeled samples can be incorporated. Subsequently, a new distance to model (DM) criterion is defined for selective ensemble learning, which can overcome the drawback of the k nearest neighbor method. The newly defined DM criterion along with the incorporation of unlabeled samples can help to describe the relationships between query samples and local models more accurately, and therefore is able to provide higher estimation accuracy. The parameters of the proposed method are finalized automatically by the particle swarm optimization technique. The proposed method is investigated using three real-life benchmark datasets, and the simulation results demonstrate the effectiveness of the proposed method in dealing with nonlinear regression problems in the process system and in the urban pollutant monitoring area.

Keywords: nonlinear soft sensor, semi-supervised ensemble learning, selective ensemble learning, distance to model, adaptive process state partition, particle swarm optimization.

1. Introduction

In process industries, a large amount of hardware sensors are installed to provide data for the purpose of monitoring and control^[1]. However, many quality-related key variables can not be measured online by these conventional sensors, such as melt index of polypropylene, concentration of butane, endpoint of crude oil, octane number of diesel oil, biomass concentration, etc. Measurements of those quality variables can be obtained through either online analyzer or offline laboratory analysis. Unfortunately, both of the two ways may result in high cost or hours of measurement delay, making them fail to satisfy modern industrial applications' ever

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increasing demands^[2-3]. The infrequent or inaccurate measurements of those quality variables may lead to poor control performance, huge production losses and even safety hazards^[4].

Soft sensors for prediction purpose have been increasingly adopted to cope with the above mentioned issue in recent years^[1,5-6]. The essence of soft sensor is to construct a predictive mathematical model for describing the functional relationship between primary variables (i.e., those difficult-to-measure variables) and secondary variables (i.e., those easy-to-measure variables). Whenever the measurements of primary variables are in need, such predictive model is invoked to infer or estimate their real values. In other word, the soft sensor is a kind of computer software but possesses the function of hardware sensors. Thereby, in contrast with those online analyzers and laboratory analyses, soft sensors have lower maintenance cost and their measurement delays are negligible.

Due to the advantages of data-driven soft sensors over model-driven soft sensors, and the popularization of the distributed control system, numerous modeling algorithms have been applied to develop data-driven soft sensors in many process industries, such as the distillation column process^[7], the wastewater treatment process^[8], the polymerization process^[9], etc. The most commonly used ones include multivariate statistical regression algorithms such as Principal Component Regression (PCR)^[10-11] and Partial Least Squares (PLS)^[12-13], and machine learning algorithms such as Artificial Neural Networks (ANN)^[14-15], Support Vector Machines^[9,16], Gaussian Process Regression (GPR)^[17-18], etc. Normally the linear soft sensing methods such as the PCR and the PLS have more practical applications due to their simplicity revealed by a recent investigation among chemical processes in Japan^[5,19], however, they can not model the process nonlinearity, while almost all industrial processes exhibit different degrees of nonlinearities. Those nonlinear soft sensors such as the ANN based ones and the SVM based ones can be adopted to alleviate such issue. Nevertheless, the nonlinear modeling algorithms have the risk of over-fitting especially in the scenario of small amount of training samples, and one single global model may not perform well for processes with strong nonlinearities in wide operating ranges. Ensemble learning based soft sensors, which constructs a series of sub-models and then combines them to give the final estimation of the primary variable, has proven to be theoretically and practically helpful to improve the prediction performance by reducing the estimation variance compared with the single-model based soft sensors^[3,20].

Ensemble learning is composed of two steps, namely ensemble members generation and prediction combination^[20]. In the first step, the entire dataset is divided into several sub-datasets, upon which sub-models are

constructed. For the sake of dealing with the process nonlinearity, this paper focuses on the localization strategies that construct local models specialized on specific model regions, where the philosophy of ‘divide and conquer’ is adopted. Clustering-based methods, for example the fuzzy C-means (FCM)^[21-22] and expectation maximization (EM)^[18,23-24] are commonly used approaches to completing this mission. Recently, some adaptive localization schemes based on the moving window technique are reported^[3,25-31]. The advantages of these methods over clustering-based approaches are that the number of local models is not predefined but adaptively determined, and new clusters can be easily identified and added to the local model set at the online operation stage. In addition, the correlation between process variables can be effectively taken into consideration. Therefore, this paper employs one of the moving window-based localization methods, i.e., the one developed in our previous work^[3], as it not only accounts for both first order and second order information of the predicted errors, but also has the functionality of redundancy discrimination.

In the other step of ensemble learning, namely the prediction combination step, the key task is to assign the combination weight to each local model according to some criterion including fuzzy membership^[32-33], Bayesian posterior probability^[23-24, 34], distance to subspaces^[35-36], predicted errors^[3,26,29-30,37], and so forth. Although these ensemble learning methods have been shown effective in developing high-performance soft sensors, they still have limitations. For example, due to the measurement noise, those criteria such as fuzzy membership, Bayesian posterior probability and distance to subspaces using only the query sample to measure the relevance between the query sample and certain local model might be unreliable. Although the k nearest neighbors (k NN) of the query sample are employed in some predicted errors-based criteria, further research indicates that in the case of some process drifts and small amount of labeled samples^[3, 30, 37-38], the selected labeled k NN of the query sample may cover overlarge operating area and the predicted errors may fail to reflect the true relationship between the query sample and local models.

What’s worse, in soft sensor applications, labeling samples is usually expensive and time-consuming, resulting in the fact that the number of labeled samples is limited. As a result, local model regions that rely on labeled sample only may not accurately capture the expertise area of the corresponding local model, which can lead to the problems of inaccurate estimation of the probability density function or the subspace. Making use of both labeled and unlabeled samples, which is termed as ‘semi-supervised learning’ in the machine learning field, is a potential way to deal with the limitation of using labeled samples only. For example, Xiang et al. realized the semi-supervised learning based on local spine regression for classification purpose^[39]. Bao et al. and Ge and

Song developed semi-supervised soft sensors through co-training^[40] and Bayesian method^[41], respectively, where the incorporation of unlabeled samples has been shown effective for accuracy enhancement. However, their works are limited to distance-based learning, not suitable for the moving-window based localization focused in this paper.

Motivated by solving the issue discussed in the above paragraph, this paper proposes a novel ensemble learning method for nonlinear soft sensor development. In the proposed method, the process state is adaptively partitioned into local model regions, and the combination weights of local models are calculated based on a newly defined criterion namely the distance to model (DM). In addition, due to selective ensemble learning has been shown effective to improve the estimation performance compared with making an ensemble of all local models^{[3][42-43]}, an adaptive selective ensemble learning mechanism developed in our previous work^[3] is incorporated. The soft sensing method developed in this paper is referred to as S³EnL-DM, which represents ‘semi-supervised selective ensemble learning based on distance to model’. Our novel contributions in this paper are summarized as follows:

- (1) A DM criterion is proposed to measure the relevance between the query sample and certain local model. This DM criterion utilizes not only the query sample but also its neighbors selected by the time metric instead of the Euclidean distance metric, which can overcome the drawbacks of using only the query sample or selecting the query sample’s neighbors by the k NN.
- (2) We propose to represent local model regions with not only labeled samples but also unlabeled samples. The reason why unlabeled samples are used is that sampling unlabeled samples is much easier and more frequent^[44], and the utilization of unlabeled samples is expected helpful for describing the expertise area of the local model in the input space.
- (3) Based on the DM criterion and the local model region representation strategy, a semi-supervised ensemble learning method is developed, which can be used for soft sensor modeling of nonlinear process systems, or dealing with nonlinear regression problems in other areas.

The remaining of this paper is structured as follows. In Section 2, some preliminaries are presented, followed by the details of the proposed method, including the adaptive process state partition, the distance to model criterion, and the selective ensemble learning strategy in Section 3. In Section 4, case studies are conducted on benchmark datasets gathering from real-life processes, and simulation results and discussions are presented. Finally

conclusions are put forward in Section 5.

2 Preliminaries

2.1 Least squares support vector regression

The least squares support vector regression (LSSVR) is a more computationally efficient nonlinear function estimator modified from the support vector regression (SVR). In this paper the LSSVR is applied to construct local models upon the partitioned local model regions because of its ability of handling process nonlinearity. The LSSVR model can be obtained by solving the following optimization problem^[45]:

$$\begin{cases} \min J(\boldsymbol{\omega}, \mathbf{e}) = \frac{1}{2} \boldsymbol{\omega}^T \boldsymbol{\omega} + \frac{\gamma}{2} \sum_{k=1}^N e_k^2 \\ \text{s.t. } y_k = \boldsymbol{\omega}^T \boldsymbol{\varphi}(\mathbf{x}_k) + b + e_k, \quad (k=1, 2, \dots, N) \end{cases} \quad (1)$$

where $\{\mathbf{x}_k, y_k\}$ is the k -th training sample, $\boldsymbol{\varphi}(\cdot)$ is the nonlinear mapping function, $\boldsymbol{\omega}$ and b are the model coefficients in feature space, γ is the regularization parameter, $\mathbf{e} = \{e_1, e_2, \dots, e_N\}^T$ is the training error vector, and N is the number of training samples. The solution to Eq. (1) is obtained by constructing the Lagrangian as

$$L(\boldsymbol{\omega}, b, \mathbf{e}; \boldsymbol{\alpha}) = J(\boldsymbol{\omega}, \mathbf{e}) - \sum_{k=1}^N \alpha_k \{ \boldsymbol{\omega}^T \boldsymbol{\varphi}(\mathbf{x}_k) + b + e_k - y_k \} \quad (2)$$

where $\boldsymbol{\alpha} = \{\alpha_1, \alpha_2, \dots, \alpha_N\}^T$ are Lagrange multiplier vector. Setting the derivatives of $L(\boldsymbol{\omega}, b, \mathbf{e}; \boldsymbol{\alpha})$ with respect to $\boldsymbol{\omega}$, b , $\mathbf{e}$ and $\boldsymbol{\alpha}$ to zeros leads to

$$\begin{cases} \frac{\partial L(\boldsymbol{\omega}, b, \mathbf{e}; \boldsymbol{\alpha})}{\partial \boldsymbol{\omega}} = 0 \Rightarrow \boldsymbol{\omega} = \sum_{k=1}^N \alpha_k \boldsymbol{\varphi}(\mathbf{x}_k) \\ \frac{\partial L(\boldsymbol{\omega}, b, \mathbf{e}; \boldsymbol{\alpha})}{\partial b} = 0 \Rightarrow \sum_{k=1}^N \alpha_k = 0 \\ \frac{\partial L(\boldsymbol{\omega}, b, \mathbf{e}; \boldsymbol{\alpha})}{\partial e_k} = 0 \Rightarrow \alpha_k = \gamma e_k, \quad k=1, 2, \dots, N \\ \frac{\partial L(\boldsymbol{\omega}, b, \mathbf{e}; \boldsymbol{\alpha})}{\partial \alpha_k} = 0 \Rightarrow \boldsymbol{\omega}^T \boldsymbol{\varphi}(\mathbf{x}_k) + b + e_k - y_k = 0, \quad k=1, 2, \dots, N \end{cases} \quad (3)$$

After eliminating $\boldsymbol{\omega}$ and $\mathbf{e}$ one can get $\boldsymbol{\alpha}$ and b through solving the following system of linear equations:

$$\begin{bmatrix} \mathbf{K} + \frac{1}{\gamma} \mathbf{I} & \mathbf{I}_N \\ \mathbf{I}_N^T & 0 \end{bmatrix} \begin{bmatrix} \boldsymbol{\alpha} \\ b \end{bmatrix} = \begin{bmatrix} \mathbf{Y} \\ 0 \end{bmatrix} \quad (4)$$

where $\mathbf{I}$ represents unit matrix, $\mathbf{I}_N$ is a column vector with all elements as 1, $\mathbf{K} \in R^{N \times N}$ and $\mathbf{K}(i, j) = K(\mathbf{x}_i, \mathbf{x}_j)$. Here $K(\cdot, \cdot)$ is called kernel function, and Gaussian kernel function is employed in this paper, which is defined as

$$K(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma^2}\right) \quad (5)$$

where $\sigma > 0$ determines the kernel width. Finally the prediction of the LSSVR model, $\hat{y}_t$, given a query sample $\mathbf{x}_t$ becomes

$$\hat{y}_t = \sum_{k=1}^N \alpha_k K(\mathbf{x}_t, \mathbf{x}_k) + b \quad (6)$$

2.2 Particle swarm optimization

The particle swarm optimization (PSO) technique seeks the solution to an optimization problem by mimicking birds' hunting behaviors. In this paper, it is employed to finalize model parameters for the proposed method due to its powerful search ability and easy implementation. In the PSO, each bird is named as a 'particle', and the solution to an optimization problem corresponds to the position of one bird in the search space. Each particle has its position, speed and fitness value, and tracks the best particle to seek the solution. The PSO starts to work by randomizing a group of particles, and ends the search procedure after several times of iterations. At each iteration, one particle updates its position according to two best values. The first one is called 'personally best value (*pbest*)' which is the best position for a particle itself, and the other one is called 'globally best value (*gbest*)' which is the best position for all particles. Formulas for calculating the position and the speed of one particle in the standard PSO are given as^[46]:

$$\begin{cases} \mathbf{v}_i(k+1) = w \cdot \mathbf{v}_i(k) + c_1 \cdot rand \cdot (\mathbf{pbest}_i - \mathbf{p}_i(k)) + c_2 \cdot rand \cdot (\mathbf{gbest} - \mathbf{p}_i(k)) \\ \mathbf{p}_i(k+1) = \mathbf{p}_i(k) + \mathbf{v}_i(k) \end{cases} \quad (7)$$

where $\mathbf{v}_i(k)$, $\mathbf{p}_i(k)$ and $\mathbf{pbest}_i$ represent the speed, position and personally best position of the i -th particle at the k -th iteration, *rand* means random value between 0 and 1, c_1 and c_2 are accelerating constants, and w is called inertial weight, which is an important parameter for the PSO. Here a linearly decreasing inertial weight which has both good global and local search ability is adopted to calculate w ^[46]:

$$w = w_{\max} - \frac{w_{\max} - w_{\min}}{K} \cdot k \quad (8)$$

where $w_{\max}$, $w_{\min}$, K , k represent the maximum weight, the minimum weight, the maximum iteration number and the iteration index, respectively.

3 Selective Semi-supervised Ensemble Learning Based on Distance to Model

The proposed soft sensing method, i.e., the S³EnL-DM, is composed of the offline operation stage and the online operation stage. At the offline stage, the process state is divided into local model regions adaptively, upon which independent local models are constructed. The parameter selection for S³EnL-DM is also completed at this stage with the aid of PSO. At the online operation stage, whenever the estimation need for a query sample arises, the relationship between the query sample and each local model will be quantified using the DM based criterion. Only those local models which are expected to have higher accuracy for the query sample are selected and combined via the Bayesian inference to give the final estimation for the query sample. The mechanisms in both of the two stages are detailed in this section.

3.1 Adaptive process state partition

The adaptive way for process state partition proposed in Ref. [3] is used to prepare concise local model set, which is illustrated in Fig. 1.

Fig. 1 Adaptive process state partition way using a moving window

Initially, a data window $W_{\text{ini}} = [X_{\text{ini}}, Y_{\text{ini}}]$ with W consecutive-time samples is set, upon which a local model f_{ini} is constructed. Subsequently the window is moved one sample step ahead, and a shifted window $W_{\text{sft}} = [X_{\text{sft}}, Y_{\text{sft}}]$ can be obtained. Then the predicted errors for Y_{ini} and Y_{sft} based on f_{ini} , denoted as R_{ini} and R_{sft} , respectively, are calculated. If R_{ini} and R_{sft} are not significantly different, the performance of f_{ini} is considered not deteriorated on W_{sft} , then W_{sft} doesn't represent a new local model region different from that represented by W_{ini} . Therefore, the model region represented by W_{sft} will not be stored, and the window continues to move and new R_{sft} will be calculated by f_{ini} . Once R_{sft} significantly deviates from R_{ini} , it indicates a new local model region is identified, upon which a new local model f_{new} is built. Assume at this point L ($L \geq 1$) local models $\{f_l\}_{l=1}^L$ have been constructed and stored. Even though f_{new} differs from f_{ini} , whether it is independent of other stored local models $\{f_l\}_{l=1}^{L-1}$ has not been examined. If there exists one local model f_l ($1 \leq l \leq L-1$) similar to f_{new} , then f_{new} will not be preserved. That is, redundancy check needs to be performed. The tasks of both new local process state identification and redundant local model detection are completed through the t -test and χ^2 -test, which accounts

for the mean and variance information, respectively. Finally, such localization method generates a group of local model regions $\{W_l = [X_l, Y_l]\}_{l=1}^L$ and the corresponding local models $\{f_l\}_{l=1}^L$.

The detailed procedures for implementing such adaptive process state partition are given in Ref. [3]. In this paper, the local experts are constructed by the LSSVR on the identified local model regions $\{W_l = [X_l, Y_l]\}_{l=1}^L$, and a group of local LSSVR models are obtained, which are denoted as $\{f_l^{LSSVR}\}_{l=1}^L$. However, it needs to be pointed out that in some applications, due to the window size is too small required for handling the process nonlinearity, the initial model f_{ini} constructed by LSSVR may over-fit the training samples, making the variance of R_{ini} quite smaller, which will generate unnecessarily large amount of local models. In this scenario, the f_{ini} can be constructed by linear modeling algorithms such as PLS, which can also generate a group of local model regions $\{W_l = [X_l, Y_l]\}_{l=1}^L$. Then local LSSVR models $\{f_l^{LSSVR}\}_{l=1}^L$ are constructed upon the corresponding local model regions and stored.

In addition, within each local model region, not only labeled samples but also unlabeled samples are contained, which is illustrated in Fig. 2.

Fig. 2 Illustration of samples within the l -th local model region

Normally the unlabeled samples consisting of X -Variable (i.e., those process variables) are sampled much faster than the labeled samples consisting of both X -Variable and Y -Variable (i.e., those quality variables), however, in most cases, those unlabeled samples are discarded. In this paper, unlabeled samples are utilized for more accurately describing the receptive fields of local models, which is expected to more reasonably assign combination weights to local models given the query sample. Let X_l^u ($1 \leq l \leq L$) represent the unlabeled samples within the l -th local model region, and all samples of process variables within the l -th local model region can be denoted as

$$\tilde{X}_l = \begin{bmatrix} X_l^u \\ X_l \end{bmatrix} \quad (9)$$

Therefore, the local model regions can be represented in terms of only process variables as $\{\tilde{W}_l = \tilde{X}_l\}_{l=1}^L$.

3.2 Distance to model

It has been shown that the DM criterion can reflect the estimation accuracy of a soft sensor model^[47], which defines two ways of calculating DM, i.e., the distance to the average of training data and the distance to the nearest neighbor in the training data. In general, the smaller the DMs between the query sample and the soft sensor model are, the higher the estimation accuracy of the soft sensor model for the query sample is. According to the distance to the nearest neighbor, given a query sample $\mathbf{x}_t$ at time instant t and the l -th local model region represented by $\tilde{\mathbf{X}}_l$ ($1 \leq l \leq L$), the DM between $\mathbf{x}_t$ and the l -th local model, $DM_l(\mathbf{x}_t, \tilde{\mathbf{X}}_l)$ ($1 \leq l \leq L$), is defined as

$$DM_l(\mathbf{x}_t, \tilde{\mathbf{X}}_l) = \min \{ \|\mathbf{x}_t - \tilde{\mathbf{X}}_l(n_i)\|, n_i = 1, 2, \dots, N_l \} \quad (10)$$

where $\tilde{\mathbf{X}}_l(n_i)$ represents the n_i -th sample within $\tilde{\mathbf{W}}_l$ and N_l is the number of samples within $\tilde{\mathbf{W}}_l$. Note that using only $\mathbf{x}_t$ may not suffice to measure the true DM, therefore, we augment $\mathbf{x}_t$ with its neighbors defined as $2T$ consecutive -time samples before and after time instant t , which forms $\mathbf{X}_t$ as

$$\mathbf{X}_t = [\mathbf{x}_{t-T}, \mathbf{x}_{t-T+1}, \dots, \mathbf{x}_{t-1}, \mathbf{x}_t, \mathbf{x}_{t+1}, \dots, \mathbf{x}_{t+T-1}, \mathbf{x}_{t+T}] \quad (11)$$

And the DM between $\mathbf{X}_t$ and the l -th local model represented by $\tilde{\mathbf{X}}_l$, $DM_l^*(\mathbf{X}_t, \tilde{\mathbf{X}}_l)$ ($1 \leq l \leq L$), is defined as

$$DM_l^*(\mathbf{X}_t, \tilde{\mathbf{X}}_l) = \sum_{j=-T}^T s_j DM_l(\mathbf{x}_{t+j}, \tilde{\mathbf{X}}_l) / \sum_{j=-T}^T s_j \quad (12)$$

where s_j ($j = -T, -T+1, \dots, T$) representing the similarity between $\mathbf{x}_{t+j}$ and $\mathbf{x}_t$, which is calculated as

$$s_j = \exp \left(- \frac{\|\mathbf{x}_t - \mathbf{x}_{t+j}\|}{\text{std}_x} \right) \quad (13)$$

where std_x is standard deviation of the distances calculated in input space among both labeled and unlabeled samples. When T is set to 0, $DM_l^*(\mathbf{X}_t, \tilde{\mathbf{X}}_l)$ is identical to $DM_l(\mathbf{x}_t, \tilde{\mathbf{X}}_l)$, and the proposed DM criterion would degenerate to the second DM definition used in Ref. [47].

It should be pointed out that it is $\tilde{\mathbf{X}}_l$ including the unlabeled samples that being employed to calculate the DM rather than $\mathbf{X}_l$ so as to better reflect the true DM. In addition, $\mathbf{x}_t$ is augmented by samples selected according to the time sequence instead of the Euclidean distance, such that the correlation among process variables can be taken into account. Meanwhile, the proposed DM according to Eq. (12) can not be calculated immediately when

$\mathbf{x}_t$ is measured, while requires to wait for T sampling instants in order to obtain the subsequent T samples. This is a drawback of the proposed DM criterion, however, since the sampling rate for the unlabeled samples is usually very fast, the waiting time is very small (usually only a few seconds) and can be negligible compared with the sampling interval of labeled samples which may take hours. Consequently, using the proposed DM criterion at the online operation stage is not a problem.

3.3 Selective ensemble learning

In the ensemble learning, the estimated y -value, $\hat{y}_t$, for a query sample $\mathbf{x}_t$ is obtained as the combination of the estimations of the off-line prepared local LSSVR models. According to the Bayesian inference framework^[23], $\hat{y}_t$ can be calculated as

$$\hat{y}_t = \sum_{l=1}^L P(f_l^{LSSVR} | \mathbf{x}_t) f_l^{LSSVR}(\mathbf{x}_t) \quad (14)$$

where $P(f_l^{LSSVR} | \mathbf{x}_t)$ ($1 \leq l \leq L$) and $f_l^{LSSVR}(\mathbf{x}_t)$ ($1 \leq l \leq L$) are the posterior probability and the prediction of the l -th local LSSVR model given $\mathbf{x}_t$, respectively. Based on the formulas for conditional probability and total probability, $P(f_l^{LSSVR} | \mathbf{x}_t)$ is computed as

$$P(f_l^{LSSVR} | \mathbf{x}_t) = \frac{P(f_l^{LSSVR})P(\mathbf{x}_t | f_l^{LSSVR})}{\sum_{l=1}^L P(f_l^{LSSVR})P(\mathbf{x}_t | f_l^{LSSVR})} \quad (15)$$

where $P(f_l^{LSSVR})$ ($1 \leq l \leq L$) represents the prior probability of f_l^{LSSVR} that the current process property can be described by f_l^{LSSVR} and $P(\mathbf{x}_t | f_l^{LSSVR})$ ($1 \leq l \leq L$) means the likelihood that $\mathbf{x}_t$ comes from the l -th local model region. Since the DM can reflect the prediction accuracy as demonstrated in Ref. [47], the likelihood of the l -th local model is computed based on $DM_l^*(\mathbf{X}_t, \tilde{\mathbf{X}}_t)$. In what follows, without causing any confusion, $DM_l^*(\mathbf{X}_t, \tilde{\mathbf{X}}_t)$ is simplified as DM_l^* for simplicity. In this paper, the Bayesian assumption is adopted, meaning that all local models have the same prior probability, that is, $P(f_l^{LSSVR}) = 1/L$.

Because smaller DM^* implies higher estimation accuracy and the corresponding local model should be assigned to larger combination weight, $P(\mathbf{x}_t | f_l^{LSSVR})$ is defined as

$$P(\mathbf{x}_t | f_t^{LSSVR}) = J_l^* / \sum_{l=1}^L J_l^* \quad (16)$$

where

$$J_l^* = \frac{1}{DM_l^*} / \max\{\frac{1}{DM_1^*}, \frac{1}{DM_2^*}, \dots, \frac{1}{DM_L^*}\} \quad (17)$$

In Eq. (17), larger J_l^* ($l = 1, 2, \dots, L$) represents higher estimation accuracy, and the normalization term in the denominator will not influence the combination results but it can scale J_l^* into the range of (0,1], which can facilitate the implementation of selective ensemble learning. Up to now, the posterior probability of the l -th local model can be obtained and $\hat{y}_t$ can be computed through making ensemble of all local models' predictions with Eq. (14). However, the selective ensemble learning which combines part of local models can achieve better generation performance, as it can reach a good equilibrium between the prediction bias and variance^[3]. In order to perform the selective ensemble learning, which models should be selected at each prediction round must be determined. Intuitively, only those ensemble members whose estimation accuracies given $\mathbf{x}_t$ are higher than a certain satisfaction degree are fused and the rest ones will not be involved. In this paper, such satisfaction degree is determined by setting a pre-defined threshold value J_{thr} on J_l^* . Since $J_l^* \in (0,1]$, the range of J_{thr} is limited to (0,1]. Thereby the index set of the selected local models, which is denoted as $L_S = \{l_1, l_2, \dots, l_S\}$, can be determined as

$$L_S = \{l | J_l^* \geq J_{thr}\} \quad (18)$$

where S represents the number of selected local models. Note that L_S is usually not fixed but adaptively determined depending on the query sample $\mathbf{x}_t$ at each prediction round, and L_S will never be empty, that is, at least one local model will be selected due to the normalization operation in Eq. (17). Subsequently, $\hat{y}_t$ is computed by building an ensemble of the selected local models, which is shown as

$$\hat{y}_t = \sum_{j=1}^S P(f_{l_j}^{LSSVR} | \mathbf{x}_t) f_{l_j}^{LSSVR}(\mathbf{x}_t) \quad (19)$$

and

$$P(f_{l_j}^{LSSVR} | \mathbf{x}_t) = \frac{P(f_{l_j}^{LSSVR})P(\mathbf{x}_t | f_{l_j}^{LSSVR})}{\sum_{j=1}^S P(f_{l_j}^{LSSVR})P(\mathbf{x}_t | f_{l_j}^{LSSVR})} \quad (20)$$

where $j = 1, 2, \dots, S$. Since the Bayesian assumption is adopted, the prior probability $P(f_{l_j}^{LSSVR}) = 1/S$, and according to Eq. (16) the likelihood $P(\mathbf{x}_t | f_{l_j}^{LSSVR}) = J_{l_j}^* / \sum_{j=1}^S J_{l_j}^*$. Finally, we can get the formula of computing $\hat{y}_t$ with those selected local models as

$$\hat{y}_t = \sum_{j=1}^S J_{l_j}^* f_{l_j}^{LSSVR}(\mathbf{x}_t) / \sum_{j=1}^S J_{l_j}^* \quad (21)$$

Detailed procedures for implementing the above selective ensemble learning for estimating the y -value given a query sample $\mathbf{x}_t$ are presented as follows.

Step (1): Collect $2T$ consecutive-time samples before and after $\mathbf{x}_t$ to form $\mathbf{X}_t$ according to Eq. (11).

Step (2): Calculate similarities s_j ($j = -T, -T+1, \dots, T$) between $\mathbf{x}_t$ and $\mathbf{x}_{t+j}$ using Eq. (13).

Step (3): Get DM_l ($l = 1, 2, \dots, L$) with Eq. (10) and get DM_l^* ($l = 1, 2, \dots, L$) with Eq.(12).

Step (4): Compute J_l^* ($l = 1, 2, \dots, L$) via Eq. (17).

Step (5): Obtain the index set of the selected local models, L_S , through Eq. (18).

Step (6): Estimate the real y -value for $\mathbf{x}_t$ based on Eq. (21).

3.4 PSO aided model parameter determination

The proposed soft sensing method involves several parameters that need to be determined, namely the window size W , the kernel parameter σ and the regularization parameter γ in the LSSVR algorithm, the time span T and the threshold value J_{thr} for selective ensemble learning. The significance levels for hypothesis testing can be pre-defined as small positive values such as 0.05 according to Refs. [3, 26]. In general, smaller W can divide the process state more detailedly, and hence is able to enhance the ability of handing the process nonlinearity. Nevertheless, too small window size has the risk of causing model instability and un-reliable estimations of the predicted residuals' mean and variance^[3]. The threshold value J_{thr} is an important value for the proposed method, as it decides the degree of selective ensemble learning. Specifically, $J_{thr} = 0$ means all local models are involved

for ensemble learning, while when J_{thr} is set to 1, only one local model with the smallest DM is chosen to predict the y -value for the query sample. Improper selection of J_{thr} could not obtain a satisfactory equilibrium between the prediction variance and bias, which may result in unacceptable estimation performance. It can also be expected that the time span T should be neither too small nor too large. In addition, two parameters involved in the LSSVR algorithm are set identical among local LSSVR models, although they can be automatically determined through the leave-one-out cross-validation in some applications^[48].

Generally, multi-tuning of these parameters may be intractable, which takes too much effort and time if it is done manually. In this paper, the parameter tuning is completed by the PSO automatically. The fitness function in the PSO is set as the predicted root mean squares error on the validation dataset ($RMSE^{val}$) that reflects the estimation accuracy. The $RMSE^{val}$ is defined as

$$RMSE^{val} = \sqrt{\sum_{t=1}^{N_{val}} (\hat{y}_t^{val} - y_t^{val})^2 / N_{val}} \quad (22)$$

where y_t^{val} and $\hat{y}_t^{val}$ represents the real y -value and its estimation for the t -th sample in the validation dataset, respectively, and N_{val} is the number of samples in the validation dataset. According to the definition of $RMSE^{val}$, the model parameters of the proposed method is determined as

$$(W^*, \sigma^*, \gamma^*, T^*, J_{thr}^*) = \min_{W, \sigma, \gamma, T, J_{thr}} RMSE^{val}(W, \sigma, \gamma, T, J_{thr}) \quad (23)$$

In the PSO, the iteration procedure can be terminated by either limiting the maximum iteration number, or setting a threshold value for **gbest** differential between two iteration rounds. Here we adopt the former one, and the maximum iteration number is set as 50. In addition, the number of particles is set as ten times the number of parameters that need to be determined.

4. Case Studies

In this section, the performance of our proposed soft sensing method, i.e., the S³EnL-DM, is first tested on two benchmark datasets, which are obtained from the industrial debutanizer column process (DCP) and the sulfur recover unit (SRU). These datasets can be publicly downloaded from the website provided by Ref. [49], and have been widely employed for evaluating the performance of various soft sensors^[3,34,44,49-51]. Subsequently, the application of the S³EnL-DM in the urban pollutant monitoring field for developing calibration model for the electronic nose is reported. The performance of some benchmark soft sensing methods is also presented for

comparison purpose. These benchmark methods include the PLS^[52], the LSSVR^[45], the just-in-time learning LSSVR (JITL-LSSVR)^[53], the ensemble of LSSVR (EnLSSVR)^[37] that employs LSSVR to construct local experts. In addition, in order to verify the effectiveness of those unlabeled samples employed by the S³EnL-DM, one more soft sensor model is developed denoted as SEnL-DM. The only difference between the SEnL-DM and the S³EnL-DM is that in the SEnL-DM, the unlabeled samples in the training dataset are discarded. In other word, in the SEnL-DM, the stored local model regions are represented by labeled samples only instead of by both labeled and unlabeled sample. The performance of those soft sensors is quantified using the RMSE index on the testing dataset which is denoted as RMSE^{1st}.

4.1 Application to the debutanizer column process

The debutanizer column process (DCP) is one part of the naphtha splitter plant, and is mainly used to remove butane and propane as overheads from the naphtha stream^[49], which is shown in Fig. 3. At the bottom of DCP, the content of butane is required to be minimized. To realize this objective, the measurement of butane content should be obtained in real-time. However, the butane content is usually analyzed by a gas chromatograph installed at the top of the DCP, which introduces a large measurement delay. Therefore, it is desirable to deliver real-time estimation of the butane content through developing a soft sensor. Seven hardware sensors which are marked with yellow circles in Fig. 3, are installed to obtain secondary variables, the explanations of which are presented in Table 1.

Fig. 3 Block diagram of the DCP

Table 1 Descriptions of secondary variables for developing soft sensor for the DCP

The DCP dataset contains 2394 samples, and the time alignment matching has been completed. They are evenly divided into three groups: the first one containing half of the dataset serves as the training dataset, and both of the rest two contain a quarter of the dataset which serves as the validation dataset and the testing dataset, respectively. In the training dataset, we assume only a part of samples are labeled and the rest ones are unlabeled. The proportion of the labeled samples in the training dataset is denoted as p , and the performance of all mentioned soft sensors are tested under different proportions of labeled samples. In this case study, the proposed S³EnL-DM based soft sensor employs the PLS to assist process state partition due to the reason explained in Section 3.1, and the latent variable number of PLS is determined by 5-fold cross validation (CV), such that the model complexity of the S³EnL-DM can be reduced, the computational burden of the PSO can be decreased and

the difficulty of the optimization can be lowered. Note that the 5-fold CV is implemented on the W samples within each local model region which is a part of the training dataset. In the 5-fold CV, the W samples are first divided into five disjoint subsets. In each iteration a temporary PLS model is trained on a different combination of four subsets, and the unused one is used to calculate the estimation errors based on the temporary PLS model. After five iterations, the latent variable number which can minimize the total estimation errors is selected to construct the final local PLS model using all the W samples. The significance levels for t -test and χ^2 -test are both set as 0.05, the scaling parameter std_x is calculated as 0.218 according to its definition, and window size W is fixed as 10 in advance for simplicity. The remaining parameters are optimized by the PSO, and the candidate set for each parameter are determined by either its physical meaning or trial-and-error^[3], which are summarized in Table 2. The optimized values of the parameters of the $S^3\text{EnL-DM}$ are tabulated in Table 3.

Table 2 Candidate sets for parameters of the $S^3\text{EnL-DM}$ that need to be optimized in the case of the DCP

Table 3 Optimized parameters of the $S^3\text{EnL-DM}$ based soft sensor under different proportions of labeled samples in the training dataset

The time trend plot comparisons of the prediction results of those soft sensors under the condition that 20% samples in the training set are labeled are illustrated in Fig. 4(a-f), and the prediction accuracies of those soft sensors under different sizes of labeled dataset are quantified in Table 4 in terms of RMSE^{tst} . Here the latent variable number of the PLS model is selected on the validation dataset, and the LSSVR model with Gaussian kernel is realized by using the LSSVM toolbox downloaded from <http://www.esat.kuleuven.be/sista/lssvmlab/>. In addition, the EnLSSVR, the SENL-DM and the $S^3\text{EnL-DM}$ share the same local model set, which are identified in the $S^3\text{EnL-DM}$, but other parameters required by the EnLSSVR and the SENL-DM are optimized by the PSO.

Fig. 4 Time trend plot comparisons of predicted butane content between various soft sensors with $p = \frac{1}{5}$: (a) predictions of PLS, (b) predictions of LSSVR, (c) predictions of JITL-LSSVR, (d) predictions of EnLSSVR, and (e) predictions of SENL-DM; and (f) predictions of $S^3\text{EnL-DM}$.

Table 4 Predicted RMSE^{tst} of various soft sensors under different proportions of labeled samples

It is observed from Fig. 4(a) that the performance of the PLS based soft sensor fail to model this process especially in predicting the peak values of the butane concentration, due to its limitation in handling nonlinear

process. Meanwhile, Fig. 4(b) shows the LSSVR outperforms the PLS to some extent, however, its estimation performance is still disappointing, indicating that a single nonlinear function estimator may have difficulty in modeling the process with strong nonlinearity. In contrast, the rest four soft sensors which employ the ‘divide and conquer’ strategy could achieve much better estimation performance as shown in Fig. 4(c-f). In particular, the proposed two methods, i.e., the SEnL-DM and S³EnL-DM, can further enhance the estimation accuracy compared with the JITL-LSSVR and the EnLSSVR, demonstrating the effectiveness of the proposed ensemble learning strategies. The quantified prediction accuracy listed in Table 4 confirms the above analyses. In addition, the predicted RMSE^{1st} tabulated in last two rows of Table 4 demonstrate that the S³EnL-DM outperforms the SEnL-DM, which can not be distinguished clearly in Fig. 4(e-f).

It should be pointed out that satisfactory performance of the S³EnL-DM demonstrated in Fig. 4 and Table 4 relies on properly tuning model parameters, which is realized through proper selection of validation samples. If we randomly allocate samples to the validation dataset and the testing dataset, where the training dataset keeps invariant required by the localization method, the average predicted RMSE^{1st} and the corresponding standard deviation under different proportions of validation samples would be as presented in **Table 5**. Here ζ represents the proportion of validation samples, and the average performance is obtained via 10 times independent simulations. In each simulation, model parameters are optimized by the PSO on the validation dataset with specific proportion of labeled samples in the training dataset and that of the validation samples.

Table 5 Average predicted RMSE^{1st} of the S³EnL-DM under different proportions of validation samples with random partition

It is indicated by Table 5 that, generally the larger the proportion of validation samples (i.e., ζ) is, the better estimation performance the S³EnL-DM achieves. However, the standard deviation of the average prediction accuracy is likely to increase as ζ becomes bigger. Moreover, comparing the results reported in Table 5, and the predicted RMSE^{1st} of the S³EnL-DM listed in Table 4, one can find that under many values of ‘ p ’ when ζ exceeds 80%, the prediction accuracies of the S³EnL-DM with random selection of validation samples are inferior to that of the S³EnL-DM with deterministic selection of validation samples where the proportion of validation samples are 50%. That is, evenly selecting validation samples can help to enhance the prediction accuracy of the S³EnL-DM. Therefore, we can basically infer that making the validation samples as disperse as possible over the entire operation area, and as many as possible, is beneficial to properly tuning the algorithm parameters of the S³EnL-DM, which is suggested and adopted in the rest two case studies.

With the aid of visualization using the principal component analysis, the mechanisms of the JITL-LSSVR, the EnLSSVR, the SEnL-DM and the S³EnL-DM can be revealed by taking the 110th testing sample as example in the case of $p = \frac{1}{6}$ as shown in Fig. 5, which is helpful for understanding the reason why the proposed methods show superiorities over the other two methods. In Fig. 5(a), the JITL-LSSVR determines the k NN of the query sample according to the Euclidean distance criterion and constructs a local model on those selected neighbors. It ignores the correlation among process variables and the samples that are spatially close in terms of the Euclidean distance criterion may not have the same correlation^[25], which makes the mapping relationship between the secondary variables and the primary variable among those selected neighbors still nonlinear even after the nonlinear mapping.

This issue can be tackled by the adaptive process state partition based on a moving window employed by the EnLSSVR, the SEnL-DM and the S³EnL-DM, which gathers correlation-related samples to form one local model region as embodied in Fig. 5(b-d). However, the EnLSSVR still utilizes the k NN of the query sample to assign weights to local models, and it may suffer from the difficulty of reasonably assigning combination weights to local models due to the above analyzed limitation of the k NN method. For example, in this application with $p = \frac{1}{6}$, for the 110th testing sample, the EnLSSVR assigns five largest combination weights to the 39th, the 16th, the 15th, the 58th and the 30th local model, and the corresponding local model regions are illustrated in Fig. 5(b). As can be seen, the query sample is located beyond the ‘expertise area’ of the 39th local model that has the largest contribution to the final estimation for the query sample. In this scenario, high estimation accuracy can not be guaranteed.

In contrast, in both the SEnL-DM and the S³EnL-DM the neighbors of the query sample are selected according to the time sequence rather than the k NN method, which are marked with blue cycles in Fig. 5(c-d). For the 110th testing sample, the SEnL-DM selects the 11th – 13th local models, while the S³EnL-DM selects the 8th – 15th local models. The 11th and the 13th local model regions are visualized with labeled samples in Fig. 5(c), and the 8th and the 15th local model regions are visualized with both labeled and unlabeled samples in Fig. 5(d). It can be inferred from Fig. 5(c-d) that the query sample is located within the ‘expertise area’ of the selected local models, implying that the proposed DM criterion can effectively select proper local models given a query sample and high estimation accuracy can be expected. It is notable that as the S³EnL-DM employs both labeled and unlabeled samples to describe the ‘expertise area’ of one local model, the DM between the query sample and the

local model can be calculated more accurately. In other word, it is the unlabeled samples in the training dataset that help the $S^3\text{EnL-DM}$ to outperform the SEnL-DM .

Fig. 5 Mechanisms of various soft sensors for the 110th testing sample under the condition that $p = \frac{1}{6}$: (a) JITL-LSSVR, (b) EnLSSVR, (c) SEnL-DM , and (d) $S^3\text{EnL-DM}$.

The influences of model parameters of the proposed $S^3\text{EnL-DM}$ method on the estimation performance under different proportions of labeled samples in the training dataset are demonstrated in Fig. 6(a-c). Such sensitivity analysis of the estimation accuracy with respect to model parameters is helpful to understand the proposed method, and then facilitate the determination of model parameters. As can be seen from Fig.6 (a), smaller window sizes can enhance the estimation accuracy because they are helpful to deal with the process nonlinearity, while larger window size not only increases the prediction error but also causes large fluctuation of the estimation performance. Nevertheless, too small window sizes should be resisted, as they may result in the problem of over-fitting among local models.

Fig. 6 Estimation accuracy as a function of parameters of the proposed soft sensor: (a) W ; (b) J_{thr} ; and (c) T . In each case, the rest parameters remain the same as their values optimized by the PSO on the validation dataset.

Fig.6 (b) proves the functionality of the selective ensemble learning. When $J_{\text{thr}} = 1$, only one local model is selected given a query sample, which is referred to as the ‘best model selection’ strategy; while $J_{\text{thr}} = 0$ meaning all local models are combined. Apparently, neither of the two strategies is the best choice. In particular, when all ensemble members are combined, the estimation error is rather high compared with the ‘best model selection’ strategy. This is due to the bias term in the bias/variance decomposition of the estimation error^[3]. It is worth to point out that the proposed selective ensemble learning strategy has two delightful properties. The first one is that the threshold value J_{thr} is limited to the range of $[0 \ 1]$, and the other one is that there is wide range of J_{thr} for achieving high estimation performance. Such two properties enable us to maximize the benefit of the selective ensemble learning strategy with few difficulties.

It is observed in Fig. 6(c) that augmenting the query sample with its time sequence neighbors is necessary, since setting T to zero always generates larger RMSE^{tst} than setting T properly. Note that there is also wide space of T of getting low estimation error. In addition, it is interesting to notice that in the case of small proportion of labeled samples such as $p = \frac{1}{10}$, increasing T has little influence on the estimation accuracy, however, when the

proportion of labeled samples is large, for example $p = \frac{1}{2}$, increasing T from 10 to 20 can remarkably deteriorate the estimation performance. Actually, as the size of the labeled samples increases, the coverage area of one local model becomes narrower, since the window size under each value of p is set to the same value, i.e., 10. Consequently, when $p = \frac{1}{10}$, increasing T in small range will not significantly change the DM between the query sample and one local model because the local model region is very ‘wide’. While in the case that $p = \frac{1}{2}$, when $T > 10$, the coverage area of the neighbors of the query sample may be wider than that of one local model region. As a result, the DM between the query sample and the local model may be changed improperly.

4.2 Application to the sulfur recovery unit

In this subsection, the performance of those soft sensing methods conducted on the debutanizer column process are further tested on a sulfur recovery unit (SRU), whose flowchart is depicted in Fig. 7^[49]. The SRU process is utilized to recycle the pure sulfur and remove the pollutant that is harmful to human body and atmosphere. The inputs of the SRU process are the monoethanolamine (MEA) gas that is abundant with hydrogen sulfide (H_2S) and the sour water stripper (SWS) gas abounding with H_2S and ammonia (NH_3). The H_2S is transformed into pure sulfur with sulfur dioxide (SO_2) generated. Those unconverted residual gas is the feed of a downstream process, i.e., the Maxisulfur plant for completing the final transformation. The concentrations of H_2S and SO_2 contained in the exhaust gas should be monitored. In this case study, soft sensors are developed to estimate the concentrations of H_2S and SO_2 , where the secondary and primary variables are presented in Table 6.

Fig. 7 Flowchart of the SRU

Table 6 Secondary and primary variables of soft sensors for SRU

There are 10081 samples in the SRU dataset, which are also partitioned evenly into three groups, namely the training dataset, the validation data and the testing dataset. The training dataset contains half of the available samples, while both the validation dataset and the testing dataset contain a quarter of all samples. Meanwhile, in the training dataset, only 20% samples are regarded as labeled, and the rest ones are treated as unlabeled samples. The required model parameters of those employed soft sensing methods are finalized in the same ways as those used in the debutanizer column process. In the S^3EnL -DM, the window size is chosen as 20, and the confidence levels are set as 0.05. The rest parameters, namely J_{thr} , σ , γ , and T , are optimized by the PSO on the validation dataset. The candidate sets for J_{thr} , σ , γ , and T are again determined by their physical interpretation or

trial-and-error, and they are presented in Table 7, where the optimized values of those parameters are included.

Table 7 Candidate sets and optimized values for parameters of the S³EnL-DM in the case of SRU

Estimation accuracies of various soft sensing methods in terms of RMSE^{tst} are presented in Table 8. Note that in this case study, the process state partition is completed by LSSVR, requiring no assistance of PLS. Through Table 8, the advantage of the proposed methods over the other four can be confirmed, and the functionality of the utilization of unlabeled samples can be demonstrated by comparing the performance of the SEnL-DM and that of the S³EnL-DM.

Table 8 Predicted RMSE^{tst} of various soft sensors for estimating concentrations of H₂S and SO₂

Scatter plot comparisons between the S³EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR are provided in Fig. 8 and Fig. 9, respectively, where the predictions of the PLS based soft sensor for the concentrations of both H₂S and SO₂ stay around the mean of the target variable because of the strong nonlinearity in this SRU process. In addition, the scatters obtained by the proposed S³EnL-DM method are clustered more tightly along the diagonal line for the concentrations of both H₂S and SO₂, showing that the S³EnL-DM has better ability in dealing with this nonlinear process. In particular, large values of the concentrations of both H₂S and SO₂, for example the peak value, should be paid more attention to, as they may result in dangerous situations. In this respect, the S³EnL-DM is more preferable, because its predictions for large values of the primary variables are more accurate compared with those of other soft sensors.

Fig. 8 Scatter plot comparisons for estimating the concentration of H₂S between the S³EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR

Fig. 9 Scatter plot comparisons for estimating the concentration of SO₂ between the S³EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR

4.3 Application to the urban pollution monitoring

In addition to being used for developing soft sensors in process systems, the proposed S³EnL-DM is applicable to dealing with other nonlinear regression problems, such as the calibration of the electronic nose in the urban pollution monitoring scenario. As is known to all, pollutants in urban atmosphere could cause severe damages, and some of them such as the benzene may induce cancers when human body is exposed in it for long time. Therefore, the concentrations of these urban atmospheric pollutants need to be precisely measured. Currently,

this task is primarily completed by industrial spectrometers, which are installed in spatially distributed stations^[54]. Due to some reasons such as the sizes and the costs, these equipments are distributed very sparsely, preventing accurate evaluation of the distribution of gases and particles concentrations in a city. Using gas multi-sensor devices, which is referred to as ‘electronic nose’, is an effective and economic way to densify the monitoring network. However, without accurate calibration, the electronic nose usually fails to provide satisfactory estimation ability.

The calibration problem is in essence a regression problem, and the most frequently used approaches for developing the calibration model include PLS, ANN, SVR, etc. In this case study, we employ the S³EnL-DM to construct a calibration model to perform calibration of the electronic nose for the dangerous pollutant benzene. In the calibration model, six variables, namely CO concentration, NO_x concentration, NO₂ concentration, O₃ concentration, temperature and humidity are selected as the input variables. Note that the concentration of non-metanic hydrocarbons (NMHC) is not included, since its analyzer failed to work 8 days after the measurement campaign started^[55]. The reference data were collected at one main street located in the center of an Italian city, and is available at <http://archive.ics.uci.edu/ml/datasets.html>. The collected data covered 13 months, lasting from March 2004 to April 2005, and samples are stored hourly. After removing some missing data, 8991 samples are available.

Besides the S³EnL-DM, the PLS, the LSSVR, the JITL-LSSVR, and the EnLSSVR are also employed to develop calibration models for comparison purpose. The entire samples are divided into training dataset, validation dataset and testing dataset in the same way as those used in the previous two case studies. The parameters of the five calibration models for estimating the concentration of benzene studied in this section are again optimized by the PSO on the validation dataset. In the S³EnL-DM, before optimization, the significance levels are set as 0.05, the std_x is calculated as 0.242, and the remaining model parameters are optimized as follows: $W = 50$, $\gamma = 10617$, $\sigma = 1.517$, $J_{\text{thr}} = 0.678$, and $T = 94$. The search candidates for those parameters that need to be manually selected are also determined by their physical meanings or the trial-and-error manner.

The estimated RMSE of various calibration models on the testing dataset are tabulated in Table 9, and the estimation performance comparisons between the S³EnL-DM and other methods in terms of scatter plot are presented as Fig. 10. By comparing the estimation errors for the benzene concentration achieved by the conventional linear and nonlinear calibration models constructed by the PLS and the LSSVR, respectively, one can find that the performance of the PLS-based model is much worse than that of the LSSVR based model,

indicating the strong nonlinear mathematical relationship between the input variables and the benzene concentration. In addition, Table 9 demonstrates that the calibration models constructed by those local learning based methods, namely the JITL-LSSVR, the EnLSSVR, and the S^3 EnL-DM could further improve the estimation accuracy compared with the LSSVR. Furthermore, it can be seen that the predicted $RMSE^{1st}$ obtained by the S^3 EnL-DM is much smaller than those obtained by the JITL-LSSVR and the EnLSSVR, and Fig. 10 demonstrates the prediction scatters of the S^3 EnL-DM are distributed much tightly and evenly along the diagonal line. These facts and comparisons show that the accuracy improvement achieved by the S^3 EnL-DM based calibration model for estimating the benzene concentration is significant, which verifies the effectiveness of the S^3 EnL-DM in dealing with nonlinear regression problems.

Table 9 Predicted $RMSE^{1st}$ of various calibration models for estimating the concentration of benzene

Fig. 10 Scatter plot comparisons for estimating the concentration of benzene between the S^3 EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR

5. Conclusion

In this paper, a soft sensing method is proposed for nonlinear processes with limited labeled samples, which is referred to as the S^3 EnL-DM. The novel contributions of this paper can be twofold. On the one hand, the unlabeled samples collected in the training dataset are incorporated, which can better describe the expertise area of the local model. On the other hand, a novel DM criterion is proposed for implementing the selective ensemble learning. These two contributions have been proven helpful to improve the performance of soft sensor using datasets coming from two real-life industrial processes. Moreover, the mechanism why the proposed soft sensor can work better is revealed and parameter sensitivity analysis of the proposed method is conducted. In addition to the process system, the proposed method is demonstrated to have effectiveness in dealing with nonlinear regression problems in the urban pollutant monitoring scenario, which constructs calibration model for the electronic nose.

It should be pointed out that although the proposed method outperforms some methods such as the PLS and the LSSVR, the improved performance is achieved at the cost of higher model complexity and more optimization time. Fortunately, the parameter determination of the proposed method can be automatically completed by the PSO, and the optimization time is consumed at the offline stage which would not impose computational burden at the online stage.

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Figure captions

Fig. 1 Adaptive process state partition way using a moving window

Fig. 2 Illustration of samples within the l -th local model region

Fig. 3 Block diagram of the DCP

Fig. 4 Time trend plot comparisons of predicted butane content between various soft sensors with $p = \frac{1}{5}$: (a) predictions of PLS, (b) predictions of LSSVR, (c) predictions of JITL-LSSVR, (d) predictions of EnLSSVR, and (e) predictions of SEnL-DM; and (f) predictions of S³EnL-DM.

Fig. 5 Mechanisms of various soft sensors for the 110th test sample under the condition that $p = \frac{1}{6}$: (a) JITL-LSSVR, (b) EnLSSVR, (c) SEnL-DM, and (d) S³EnL-DM.

Fig. 6 Estimation accuracy as a function of parameters of the proposed soft sensor: (a) W ; (b) J_{thr} ; and (c) T . In each case, the rest parameters remain the same as their values optimized by the PSO on the validation dataset.

Fig. 7 Flowchart of the SRU

Fig. 8 Scatter plot comparisons for estimating the concentration of H₂S between the S³EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR

Fig. 9 Scatter plot comparisons for estimating the concentration of SO₂ between the S³EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR

Fig. 10 Scatter plot comparisons for estimating the concentration of benzene between the S³EnL-DM and the PLS, the LSSVR, the JITL-LSSVR and the EnLSSVR

samples within l -th local model region

● labeled samples

● unlabeled samples

X -Variable

Y -Variable

Table titles

Table 1 Descriptions of secondary variables for developing soft sensor for the DCP

Table 2 Candidate sets for parameters of the $S^3\text{EnL-DM}$ that need to be optimized in the case of the DCP

Table 3 Optimized parameters of the $S^3\text{EnL-DM}$ based soft sensor under different proportions of labeled samples in the training data set.

Table 4 Predicted RMSE^{tst} of various soft sensors under different proportion of labeled samples

Table 5 Average predicted RMSE^{tst} of the $S^3\text{EnL-DM}$ under different proportion of validation samples with randomly partition

Table 6 Secondary and primary variables of the soft sensors for SRU

Table 7 Candidate sets and optimized values for parameters of the $S^3\text{EnL-DM}$ in the case of SRU

Table 8 Predicted RMSE^{tst} of various soft sensors for estimating concentrations of H_2S and SO_2

Table 9 Predicted RMSE^{tst} of various calibration models for estimating the concentration of benzene

Table 1 Descriptions of secondary variables for developing soft sensor for the DCP

Secondary variable	Explanation
u_1	Top temperature
u_2	Top pressure
u_3	Reflux flow
u_4	Flow to next process
u_5	6 th tray temperature
u_6	Bottom temperature
u_7	Bottom temperature

Table 2 Candidate sets for parameters of the $S^3\text{EnL-DM}$ that need to be optimized in the case of the DCP

Ratio of labeled samples	γ	σ	J_{thr}	T
$\frac{1}{10} \leq p \leq \frac{1}{4}$	[1, 50]			
$p = \frac{1}{3}$	[1, 100]	[0.05, 0.5]	[0, 1]	[0, 15]
$p = \frac{1}{2}$	[1, 200]			

Table 3 Optimized parameters of the S³EnL-DM based soft sensor under different proportions of labeled samples in the training data set.

Parameter	$p = \frac{1}{10}$	$p = \frac{1}{9}$	$p = \frac{1}{8}$	$p = \frac{1}{7}$	$p = \frac{1}{6}$	$p = \frac{1}{5}$	$p = \frac{1}{4}$	$p = \frac{1}{3}$	$p = \frac{1}{2}$
γ	10.37	14.71	15.95	27.05	26.23	25.35	22.28	73.14	100.00
σ	0.175	0.187	0.245	0.219	0.284	0.331	0.343	0.228	0.327
J_{thr}	0.706	0.729	0.772	0.645	0.735	0.823	0.799	0.745	0.853
T	9	7	7	9	5	6	6	7	5

Table 4 Predicted RMSE^{1st} of various soft sensors under different proportion of labeled samples

Soft sensing method	$p = \frac{1}{10}$	$p = \frac{1}{9}$	$p = \frac{1}{8}$	$p = \frac{1}{7}$	$p = \frac{1}{6}$	$p = \frac{1}{5}$	$p = \frac{1}{4}$	$p = \frac{1}{3}$	$p = \frac{1}{2}$
PLS	0.1416	0.1410	0.1405	0.1409	0.1408	0.1405	0.1403	0.1404	0.1404
LSSVR	0.1243	0.1234	0.1221	0.1218	0.1130	0.1099	0.0958	0.0931	0.0747
JITL-LSSVR	0.1154	0.1082	0.1093	0.1093	0.1006	0.0927	0.0906	0.0822	0.0666
EnLSSVR	0.1127	0.1063	0.1042	0.1122	0.0999	0.0862	0.0828	0.0785	0.0589
SEnL-DM	0.0993	0.0925	0.0913	0.0872	0.0765	0.0717	0.0644	0.0467	0.0322
S ³ EnL-DM	0.0952	0.0892	0.0870	0.0801	0.0711	0.0685	0.0596	0.0439	0.0311

Table 5 Average predicted RMSE^{lst} of the $\text{S}^3\text{EnL-DM}$ under different proportion of validation samples with randomly partition

	$\zeta = 20\%$	$\zeta = 40\%$	$\zeta = 60\%$	$\zeta = 80\%$
$p = \frac{1}{10}$	0.0985 ± 0.0017	0.0960 ± 0.0039	0.0957 ± 0.0037	0.0928 ± 0.0062
$p = \frac{1}{9}$	0.0920 ± 0.0022	0.0908 ± 0.0030	0.0901 ± 0.0031	0.0876 ± 0.0044
$p = \frac{1}{8}$	0.0884 ± 0.0026	0.0873 ± 0.0031	0.0857 ± 0.0034	0.0838 ± 0.0041
$p = \frac{1}{7}$	0.0833 ± 0.0031	0.0817 ± 0.0032	0.0812 ± 0.0031	0.0793 ± 0.0052
$p = \frac{1}{6}$	0.0754 ± 0.0023	0.0733 ± 0.0024	0.0718 ± 0.0027	0.0706 ± 0.0032
$p = \frac{1}{5}$	0.0732 ± 0.0018	0.0715 ± 0.0020	0.0712 ± 0.0031	0.0698 ± 0.0019
$p = \frac{1}{4}$	0.0611 ± 0.0011	0.0599 ± 0.0013	0.0597 ± 0.0022	0.0570 ± 0.0033
$p = \frac{1}{3}$	0.0455 ± 0.0013	0.0450 ± 0.0013	0.0446 ± 0.0019	0.0440 ± 0.0051
$p = \frac{1}{2}$	0.0342 ± 0.0029	0.0337 ± 0.0024	0.0323 ± 0.0031	0.0311 ± 0.0025

Table 6 Secondary and primary variables of the soft sensors for SRU

Variable	Explanation
Secondary variable	MEA gas flow
	First air flow
	Second air flow
	Gas flow in SWS zone
	Air flow in SWS zone
Primary variable	Concentration of H ₂ S
	Concentration of SO ₂

Table 7 Candidate sets and optimized values for parameters of the $S^3\text{EnL-DM}$ in the case of SRU

		γ	σ	J_{thr}	T
Candidate set		[1, 50]	[0.01, 0.5]	[0, 1]	[0, 15]
Optimized value	for H_2S	11.57	0.100	0.806	3
	for SO_2	14.74	0.097	0.708	5

Table 8 Predicted RMSE^{1st} of various soft sensors for estimating concentrations of H₂S and SO₂

Concentration	PLS	LSSVR	JITL-LSSVR	EnLSSVR	SEnL-DM	S ³ EnL-DM
H ₂ S	0.0519	0.0415	0.0401	0.0382	0.0376	0.0367
SO ₂	0.0573	0.0517	0.0475	0.0477	0.0421	0.0408

Table 9 Predicted RMSE^{1st} of various calibration models for estimating the concentration of benzene

PLS	LSSVR	JITL-LSSVR	EnLSSVR	S ³ EnL-DM
2.3782	1.3919	1.3656	1.3436	0.7947

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