Unconventional Superconductivity in Heavy-Fermion Compounds

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Abstract

Over the past 35 years, research on unconventional superconductivity in heavy-fermion systems has evolved from the surprising observations of unprecedented superconducting properties in compounds that convention dictated should not superconduct at all to performing explorations of rich phase spaces in which the delicate interplay between competing ground states appears to support emergent superconducting states. In this article, we review the current understanding of superconductivity in heavy-fermion compounds and identify a set of characteristics that is common to their unconventional superconducting states. These core properties are compared with those of other classes of unconventional superconductors such as the cuprates and iron-based superconductors. We conclude by speculating on the prospects for future research in this field and how new advances might contribute towards resolving the long-standing mystery of how unconventional superconductivity works.

Keywords:

unconventional superconductivity, heavy-fermion behavior, quantum critical point, non-Fermi liquid behavior, magnetic fluctuations, Kondo lattice

1. Introduction

In the two decades prior to the 1979 discovery of unconventional superconductivity in CeCu₂Si₂ [1], the properties of superconductors were typically studied within the context of the Bardeen-Cooper-Schrieffer (BCS) theory of superconductivity [2, 3, 4]. The BCS theory describes pairing between conduction electrons as being mediated by phonons so that the characteristic Debye temperature, Θ_D , plays an important role as an energy scale. However, the unexpected discovery of superconductivity in CeCu₂Si₂ turned this paradigm on its head. The superconducting Cooper pairs in CeCu₂Si₂ are not formed from ordinary conduction electrons, but are rather composed of quasiparticles with enhanced effective masses [1]. Furthermore, the hierarchy of energy scales departs significantly from what is assumed in the BCS theory, indicating that pairing of the quasiparticles cannot be phonon-mediated. These observations made it clear that CeCu₂Si₂ was no ordinary superconductor, and heralded a new era of research on unconventional superconductivity. The course of this research has evolved into current explorations of rich phase spaces wherein new and exciting physics has emerged from tuning the delicate interplay between competing ground states. Before discussing the unconventional superconducting states in these fascinating materials, which is the subject of this review, we first briefly introduce the characteristics and origin of heavy-fermion compounds.

1.1. Heavy-Fermion Compounds

The physical properties of simple metals such as the elements sodium or copper can be understood well by models that neglect the many-body interactions that occur between electrons. In even slightly more complex materials, this unrealistic assumption fails dramatically, but the itinerant electron states and their interactions with other electrons can be transformed into non-interacting quasiparticles with enhanced effective masses by invoking the Fermi liquid theory [5, 6, 7]. A Fermi liquid state, which is populated by these independent quasiparticles, is characterized by properties that include a quadratic temperature dependence of the electrical resistivity, $\rho(T) \sim (T/T_F)^2$ for $T \ll T_F$, where $T_F = \epsilon_F/k_B$ is the Fermi temperature and ϵ_F is the Fermi energy [8]. Such a quadratic temperature dependence was first experimentally resolved in 1975 by Andres *et al.* in measurements on the compound CeAl₃ [9]. While T_F values for simple metals such as copper are of order 10^4 K [10] and a $(T/T_F)^2$ temperature dependence of ρ is very difficult to resolve experimentally, analysis of $\rho(T)$ and other physical properties indicated that T_F was three orders of magnitude lower (*i.e.*, 15–25 K) in CeAl₃ [9]! Furthermore, T_F is inversely proportional to the coefficient of the electronic contribution to specific heat, γ , which is proportional to the electronic density of states at ϵ_F , $N(\epsilon_F)$, and is roughly $0.7 \text{ mJ mol}^{-1} \text{ K}^{-2}$ for copper [10] compared to $\gamma \simeq 1600 \text{ mJ mol}^{-1} \text{ K}^{-2}$ for CeAl₃ [9]. Instead of observing magnetic order within the lattice of localized magnetic moments associated with trivalent Ce ions separated by $\sim 4 \text{ \AA}$, a nonmagnetic Fermi-liquid ground state, populated by quasiparticles of order 1000 times heavier than free electrons, was observed in CeAl₃. These astounding results hinted at an

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enormous increase in $N(\epsilon_F)$ as well as the emergence of a new characteristic energy scale in CeAl_3 that acts as an effective T_F .

To understand how these remarkable properties are possible, it is instructive to first consider what happens when a single impurity bearing a localized magnetic moment is dissolved into a non-magnetic metallic host. The Friedel-Anderson model was developed principally to explain magnetic moment formation in metals, but it also describes such a single-ion impurity scenario [11]. In this model, quantum mechanical admixing or hybridization between the localized electron states of the impurity ion and the itinerant electron states from the host, characterized by hybridization matrix element $\mathcal{V}$, produces a virtual bound state or resonance in the density of electronic states with width $\Gamma \propto \mathcal{V}^2$ [11]. When the energy associated with this resonance (the maximum) is within Γ of ϵ_F , $N(\epsilon_F)$ is enhanced.

Addressing a different problem (at least superficially), Jun Kondo proposed a simple Hamiltonian to explain the logarithmic divergence with decreasing temperature observed since the 1930's [12] in measurements of $\rho(T)$ on systems containing dilute magnetic impurities. The essential physics of the Kondo Hamiltonian is embodied in a magnetic exchange coupling $\mathcal{J}$ between the spin $\vec{S}$ of a magnetic impurity with the local spin density of the surrounding conduction electrons $\vec{s}_0$. Using this model and the second Born approximation [13], Kondo was able to derive the long sought after $\rho(T) \sim -\log(T)$ behavior. More importantly for our discussion, a new energy scale, designated the Kondo temperature T_K , also emerged from these calculations [13], which separates the temperature region over which the calculations are valid ($T > T_K$) from $T < T_K$ where perturbation theory breaks down. The Friedel-Anderson and Kondo models, which contribute an enhancement of $N(\epsilon_F)$ and a new energy scale T_K , respectively, are equivalent descriptions of a magnetic impurity in a metallic host as shown by Schrieffer and Wolff [14]. The antiferromagnetic exchange interaction of the Kondo model $\mathcal{J}$ is calculable in terms of $\mathcal{V}$ from the Friedel-Anderson Hamiltonian,

$$\mathcal{J} = 2\mathcal{V}^2(1/|\epsilon_f| + 1/(\epsilon_f + U)), \quad (1)$$

where $\epsilon_f = \epsilon_i - \epsilon_F$ and ϵ_i is the energy of the localized electrons in the unfilled shell of the magnetic impurity ion [14].

A physical picture of how a magnetic impurity interacts with its surroundings emerges from these theoretical developments. At temperatures comparable to but greater than $T_K \propto \exp[-1/(N(\epsilon_F)\mathcal{J})]$ [15], the antiferromagnetic exchange interaction, characterized by $\mathcal{J}$, between $\vec{S}$ and $\vec{s}_0$ promotes polarizing $\vec{s}_0$ antiparallel to the direction of $\vec{S}$. This tendency causes the localized magnetic moment of the impurity ion to become dynamically screened or compensated, and the exchange interaction leads to strong local spin-flip or incoherent Kondo scattering of charge carriers (*i.e.*, a $\rho(T) \propto -\log(T)$ term is obtained in this temperature regime). At temperatures less than T_K , the screening of the impurity ion's magnetic moment becomes complete as the surrounding conduction electrons form a bound state with the impurity, producing a single non-magnetic quasiparticle with an enhanced effective mass. This many-body singlet state behaves like a local Fermi liquid [16], emphasizing that T_K is a suitable effective T_F .

The physics of a single magnetic impurity embedded in a metallic host, which is treated in great detail elsewhere [17, 18, 19, 15], provides a mechanism for an enhanced $N(\epsilon_F)$ via the emergence of a quasiparticle resonance and leads to a new energy scale T_K , below which, a local Fermi-liquid state exists. However, heavy-fermion materials like CeAl_3 do not contain dilute concentrations of magnetic *impurities*, but are rather composed of a *lattice* of localized magnetic moments coupled to the Fermi sea [19]. These compounds share other common traits including a crossover from Curie-Weiss behavior at high temperature to enhanced Pauli magnetic susceptibility at low temperature and a broad peak-like feature in the electrical resistivity. These and other characteristics of heavy-fermion compounds can be understood within the context of a generalization of the Friedel-Anderson model called the periodic Anderson model. In an overly simplistic picture, the periodic Anderson model assumes that the Kondo effect occurs at every site bearing a localized magnetic moment. In principle, this leads to the formation, below an energy scale T^* , of 10^{23} quasiparticles per mole localized magnetic moments. Characteristic Kadowaki-Woods [20, 21] and Wilson-Sommerfeld [17] ratio values, calculated using quantities obtained from experimental data below T^* , are used to confirm Fermi-liquid ground states. T^* , sometimes referred to as the Kondo lattice coherence temperature, is typically identified with the temperature of the maximum of the peak-like feature in $\rho(T)$ and is distinct from T_K . The crossover from localized to delocalized magnetic-moment behavior in the magnetic susceptibility also occurs near T^* . In many cases, $T^* < T_K$ such that screening of the localized magnetic moments begins near T_K , but is incomplete until T^* when the Kondo lattice becomes coherent. However, under certain filling conditions [22] or when mutual screening of local magnetic moments enhances T^* relative to T_K [23, 24, 25], cases where $T^* > T_K$ have been reported and discussed.

The periodic Anderson model is particularly well suited to describing the properties of metallic compounds containing sublattices of Ce, Sm, Yb, U, and Pu ions. This is largely a consequence of these ion's tendency towards valence instabilities in metals [26] that allows for a finite T_K and T^* (*i.e.*, ϵ_f is small enough so that $\mathcal{J} \propto \mathcal{V}^2/|\epsilon_f|$ is finite for reasonable values of $\mathcal{V}$). It is natural then that the majority of known heavy-fermion compounds are composed of one of these lanthanide or actinide elements, with Ce- and U-based compounds being particularly well represented. There are also a more limited number of Pr-based heavy-fermion compounds that are known, and these sometimes involve the quadrupolar Kondo effect that was originally proposed for compounds containing U^{4+} ions with cubic point group symmetry [27, 28, 29]. The electric quadrupole moment, associated with a non-magnetic Γ_3 doublet ground state of Pr^{3+} , can be screened just like a magnetic moment in the conventional Kondo effect, leading to a heavy-fermion state [30, 31]; however, we note that the heavy-fermion superconductor $\text{PrOs}_4\text{Sb}_{12}$ serves as a counter-example with its nonmagnetic singlet Γ_1 ground state [32, 33].

With the exception of Sm, the total angular momentum J ground states for these lanthanide and actinide ions are generally not significantly admixed with excited states [34], but

the $2J + 1$ -fold degeneracy associated with J is usually at least partially lifted by the crystalline electric field (CEF). Since the unfilled $4f$ or $5f$ electron shells of these ions are so well screened by the surrounding filled electron shells, the energy splitting δ between the ground and first excited states of the multiplet can be comparable to energy scales such as T_K , T^* , or the superconducting critical temperature T_c . Furthermore, the hybridization between itinerant and localized electron states, characterized by $\mathcal{J}$, also facilitates the indirect Ruderman-Kittel-Kasuya-Yosida (RKKY) magnetic exchange interaction [35, 36, 37] that couples the localized magnetic moments [15]. In the context of the simple and intuitive Doniach phase diagram [38], $\mathcal{J}$ is the parameter that determines whether the heavy Fermi liquid or the magnetically-ordered (usually antiferromagnetic) ground state overcomes the other. Therefore, the physical properties of these materials are governed by the delicate interplay of comparable energy scales and competition, or sometimes coexistence, between distinct ground states. A rich phase space emerges from this environment, containing numerous ground states often with quantum critical points residing at their zero-temperature boundaries and with nearby quantum criticality at finite temperatures [38, 8, 39]. Looking beyond f -electron systems, we note that there are reports of at least two d -electron transition-metal oxides, LiV_2O_4 [40] and $\text{CaCu}_3\text{Ru}_4\text{O}_{12}$ [41], that exhibit characteristics consistent with a heavy-fermion state. Neither of these compounds is superconducting, but transition-metal oxide-based heavy-fermion compounds may present an unexplored frontier of heavy-fermion research.

Though we have only skimmed the surface of this fascinating subject, it is beyond our scope to provide further depth. We refer the interested reader to numerous review articles dedicated to covering heavy-fermion physics [42, 43, 44, 45, 46, 47, 19, 48, 49]. Having briefly introduced the fundamentals of heavy-fermion physics, we are prepared to consider the basic characteristics of superconductivity in these systems.

1.2. Superconductivity in Heavy-Fermion Compounds

Chronologically speaking, the first observation of superconductivity in a heavy-fermion compound occurred in measurements by Bucher *et al.* on UPt_3 [50]; however, the ground state of UPt_3 was not considered to be a heavy Fermi liquid at the time and the observed superconductivity, after extensive experiments exercising due diligence, was dismissed by the authors as extrinsic [50]. The observed superconducting transition temperature of $T_c = 0.97$ K was only reduced by about 0.3 K in a 6 T magnetic field [50] (meaning that the initial slope of the upper critical field, $(dH_{c2}/dT)_{T_c} \simeq -20$ T/K, was improbably large). Even though a diamagnetic signal was obtained from a powdered sample of UPt_3 , the authors interpreted their results as indicating that superconductivity must arise from precipitated filaments of U [50].

Four years later, Steglich *et al.* reported superconductivity in CeCu_2Si_2 at $T_c \simeq 0.51(4)$ K [1]. It was recognized at that time that CeCu_2Si_2 was a heavy-fermion compound, and significant effort was invested on trying to convince the scientific community that the observed superconductivity in CeCu_2Si_2 was

intrinsic [1]. Early on, two important observations were made that became hallmark characteristics of heavy-fermion superconductors. First, the size of the jump at T_c in specific heat data, ΔC , is comparable to γT_c , indicating that the Cooper pairs are formed from heavy quasiparticles rather than bare conduction electrons. Second, as was the case with CeAl_3 , the effective T_F energy scale is anomalously low; for CeCu_2Si_2 , the spin-fluctuation temperature of order 10 K serves as T_F . The resulting hierarchy of energy scales $T_c < T_F < \Theta_D$ is drastically different from that assumed in the BCS theory of superconductivity [2, 3, 4] wherein characteristic frequencies obey $k_B\Theta_D/h \ll k_BT_F/h$. This observation indicates that superconductivity in CeCu_2Si_2 cannot be conventional (*i.e.* similar to the superfluid state of ^3He [51], this was a second example of a system in which pairing cannot be phonon-mediated).

The results for CeCu_2Si_2 were initially controversial, and as in most burgeoning subjects in materials physics, it took time to sort out questions of sample quality and other details [42]. However, the results stood the test of time and heavy-fermion superconductors such as UPt_3 (the previously-observed superconductivity was demonstrated to be intrinsic) [52], UPt_3 [53], and URu_2Si_2 [54, 55, 56] were subsequently discovered and studied. Many of the early discoveries involved a superconducting state that emerged from a non-magnetic heavy Fermi liquid. However, a new era of research was heralded by the discovery of superconductivity in CePd_2Si_2 and CeIn_3 that appeared only after an antiferromagnetic phase was suppressed by applied pressure [57, 58]. It is widely believed that fluctuations associated with a magnetic quantum critical point play a role in facilitating the observed non-Fermi liquid behavior in the normal states of these compounds and also serve as the pairing mechanism supporting superconductivity [58]. This picture is expected to apply more broadly to all heavy-fermion superconductors; even the compounds for which superconductivity is observed at ambient pressure generally reside in close proximity to a nearby magnetic or quadrupolar ordered phase that nature has already suppressed.

The superconducting states of heavy-fermion compounds are generally characterized by: (1) T_c values usually of order 1 K or lower, (2) Cooper pairs formed from heavy quasiparticles as inferred from large jumps of order γT_c in specific heat at T_c ; (3) Large orbital upper critical fields at 0 K, $H_{c2}^*(0)$, that can be calculated using Werthamer-Helfand-Hohenberg (WHH) theory [59] from the very large initial slopes, $(dH_{c2}/dT)_{T_c}$, near T_c ; (4) Short superconducting coherence lengths ξ relative to the London magnetic penetration depth λ such that the Ginzburg-Landau parameter $\lambda/\xi \gg 1/\sqrt{2}$ (*i.e.*, these are extreme type-II superconductors); (5) Line or point nodes in the superconducting energy gap $\Delta(\vec{k})$; (6) Nearby ordered state in phase space such as magnetic or quadrupolar order. In addition to these ubiquitous characteristics, some of the heavy-fermion superconductors such as UPt_3 and $\text{PrOs}_4\text{Sb}_{12}$ exhibit evidence for multiple superconducting energy gaps [49].

There are many review articles that cover superconductivity in heavy-fermion compounds [42, 43, 60, 44, 45, 61, 46, 47, 19, 48, 49]. This review is organized by lanthanide or ac-

tinide element. Each section focuses primarily on the seminal experimental discoveries, but our narrative is “dressed” by theoretical developments and concepts when appropriate. Additional emphasis is placed on more recently discovered heavy-fermion superconductors that have not been covered in earlier review articles including in new Pr- [31, 62] and Yb-based [63] compounds. The family of “115” heavy-fermion superconductors is also discussed with extra emphasis due to the many ground-breaking discoveries made in the course of studies on these and related materials over the last roughly 13 years. A core set of empirically-observed characteristics associated with heavy-fermion superconductors are then identified and compared with properties of related “cousins” including unconventional superconductivity in the cuprates and the iron pnictides/calchogenides. We conclude with a few thoughts concerning the current state of the field of heavy-fermion superconductivity and provide an outlook for future research and developments.

2. Ce-based heavy-fermion superconductors

2.1. CeM_2X_2 ($M = Ni, Cu, Rh, Pd$; $X = Si, Ge$)

There is a series of isostructural heavy-fermion superconductors that form with the $ThCr_2Si_2$ -type crystal structure with space group $I4/mmm$. Among this series, superconductivity was discovered in the heavy-fermion compound $CeCu_2Si_2$ at ambient pressure [1]; in contrast, superconductivity emerges only after antiferromagnetic order is suppressed by applied pressure in the compounds $CeCu_2Ge_2$ [64], $CePd_2Si_2$ [57], and $CeRh_2Si_2$ [65]. Interestingly, an antiferromagnetic spin-density wave (SDW) order can be stabilized in slightly Cu-deficient samples of $CeCu_2Si_2$ [66]; this observation indicates that stoichiometric $CeCu_2Si_2$ resides on the border of antiferromagnetic order and suggests that the chemical pressure produced by filling Cu vacancies suppresses SDW order and enables superconductivity to emerge [67]. This scenario is supported by the observation that non-stoichiometric $CeCu_2Si_2$ samples exhibiting SDW order also exhibit pressure-induced superconductivity [68]. Therefore, $CeCu_2Si_2$, $CeCu_2Ge_2$, $CePd_2Si_2$, and $CeRh_2Si_2$ share a common predisposition for magnetic order that can be suppressed by applied pressure. The case of superconductivity in the heavy-fermion compound $CeNi_2Ge_2$ [69] does not exactly fit this pattern as we discuss below.

Bulk superconductivity was observed in the heavy-fermion compound $CeCu_2Si_2$ in 1979 at $T_c = 0.6$ K as confirmed by a specific heat jump of $\Delta C/\gamma T_c = 1.4$ at T_c ($\gamma \approx 1000$ mJ mol⁻¹ K⁻²) [1]. The SDW order observed in some samples occurs due to a Fermi-surface instability and is characterized by an incommensurate wave-vector $\vec{Q} = (0.215, 0.215, 0.530)$ with an ordered magnetic moment of $\sim 0.1 \mu_B/Ce$ [70]. In such samples, superconductivity is induced by applying pressure or annealing the samples in Cu vapor. Measurements on single crystals of $CeCu_2Si_2$ reveal a modest anisotropy of the upper critical fields $H_{c2}(T)$ when the magnetic field is aligned parallel and perpendicular to the Ce planes [66]. The initial slopes, $(dH_{c2}/dT)_{T_c} \approx -23$ T/K, are isotropic but $H_{c2}^\perp(0) \approx 2.45$ T

and $H_{c2}^\parallel(0) \approx 2.05$ T values are observed at zero temperature [66]. The Pauli paramagnetic limit for $CeCu_2Si_2$ is estimated [71] $H_{p0} = 1.84T_c \approx 1.2$ T using $T_c = 0.65$ K, and the orbital limiting field is calculated using WHH theory [59] to be $H_{c2}^*(0) = 0.693(-dH_{c2}/dT)_{T_c}T_c \approx 10.4$ T using $(dH_{c2}/dT)_{T_c} \approx -23$ T/K. Given these estimates, it appears that superconductivity in $CeCu_2Si_2$ is paramagnetically-limited [72]; it is likely that $H_{c2}(0) > H_{p0}$ due to strong spin-orbit scattering, which is not accounted for in our estimate of H_{p0} . The quadratic temperature dependence of the specific heat and thermal expansion coefficient [73] and nuclear quadrupole resonance measurements [74] in the superconducting state of $CeCu_2Si_2$ are consistent with the presence of line nodes [60] in the superconducting energy gap $\Delta(\vec{k})$. However, a recent study demonstrated that the specific heat deviates from a quadratic temperature dependence at very low-temperature [75]; this behavior is inconsistent with the presence of line nodes, but the specific heat data within the superconducting state can be accounted for by a scenario involving nodeless multiband superconductivity [75]. Furthermore, the absence of evidence for nodal quasiparticle excitations in the magnetic field dependence of C at 60 mK and the lack of resolvable oscillations of C as a function of angle as the sample is rotated in a field within the ab plane at 0.1 K and 0.2 K both cast doubt on the presence of line nodes in $CeCu_2Si_2$ [75]. These results may require us to reevaluate the conventional understanding about electron pairing in $CeCu_2Si_2$. When samples that exhibit superconductivity at ambient pressure are subjected to applied pressure, T_c increases up to ~ 4 GPa, and then decreases with increasing pressure [76]. Interestingly, a second dome of superconductivity is observed at higher pressure in slightly Ge-doped samples that is associated with a valence transition of the Ce ions (see Fig. 1) [77, 78]; this intriguing result suggests that superconductivity in $CeCu_2Si_2$ can be supported by both a magnetically-mediated pairing mechanism and an interaction based on spatially-extended density fluctuations.

A sinusoidally-modulated antiferromagnetic order below $T_N = 4.15$ K, characterized by incommensurate wave vector $\vec{Q} = (0.284, 0.284, 0.543)$ and an ordered magnetic moment of $0.74 \mu_B/Ce$, is observed at ambient pressure in $CeCu_2Ge_2$ [79]. Following suppression of this antiferromagnetic order by applying pressure, superconductivity was observed in $CeCu_2Ge_2$ with $T_c \approx 0.6$ K near 8 GPa [64]. The upper critical field was measured at an applied pressure of ~ 10.1 GPa and a value of $H_{c2}(0) \sim 2$ T was obtained with an initial slope of $(dH_{c2}/dT)_{T_c} \approx -11$ T/K [64]. The value of $H_{c2}(0)$ is comparable to that of $CeCu_2Si_2$, and is also consistent with paramagnetic limiting ($H_{c2}(0) << H_{c2}^*(0)$). At ambient pressure and ~ 1 GPa, specific heat measurements of $CeCu_2Ge_2$ in the antiferromagnetic state obtain $\gamma \approx 200$ mJ mol⁻¹ K⁻² [80]; however, measurements have not yet been performed in the superconducting state of $CeCu_2Ge_2$ to resolve a jump at T_c . These large values of γ and $(dH_{c2}/dT)_{T_c}$ are consistent with quasiparticles with enhanced masses and heavy-fermion superconductivity in $CeCu_2Ge_2$.

The compound $CePd_2Si_2$ is considered to be an intermedi-

Figure 1: (Color online) Schematic phase diagram of temperature vs. lattice density for a generic Ce-based compound. At low density (lattice density typically tuned by pressure), stable localized magnetic moments participate in long-range antiferromagnetic order below a Néel temperature T_N . The red line represents the $T_N(P)$ phase boundary, which monotonically decreases towards a critical pressure p_{c1} . Unconventional superconductivity, facilitated by magnetically-mediated pairing near p_{c1} , is represented by the red dome, which screens or protects a quantum critical point. With increasing lattice density, the compound crosses over from heavy-fermion behavior to an intermediate valence region. This may proceed through a first-order phase transition (represented by the green dashed line) where a concomitant volume collapse of the unit cell takes place. When the critical end point where the first-order phase transition terminates (green filled circle) is at a sufficiently low temperature, superconductivity may form around the quantum phase transition associated with volume collapse at p_{c2} (the green dome). After Ref. [77].

ate valence system with antiferromagnetic order, characterized by wave vector $\vec{Q} = (0.5, 0.5, 0)$ [81], below $T_N \approx 10$ K. This antiferromagnetic order is suppressed by applied pressure [82], and vanishes near ~ 2.8 GPa [57]. In the vicinity of this critical pressure, strong non-Fermi liquid behavior is observed, manifested by $\rho(T) \sim T^{1.2}$, and superconductivity with $T_c = 0.43$ K emerges (see inset of Fig. 2) [57, 58, 83]. Superconductivity appears as a dome in the temperature-pressure phase diagram centered around 2.8 GPa as is displayed in Fig. 2 [57, 58, 83]. The upper critical fields were measured at 2.67 GPa in a single crystal of CePd_2Si_2 and found to be relatively anisotropic with values of $H_{c2}^a(0) \approx 0.7$ T and $H_{c2}^c(0) \approx 1.3$ T with large initial slopes of $(dH_{c2}^a/dT)_{T_c} \approx -12.7$ T/K and $(dH_{c2}^c/dT)_{T_c} \approx -16$ T/K [83]. The Pauli paramagnetic limiting field can be estimated $H_{p0} \approx 0.8$ T, which is comparable to the observed $H_{c2}(0)$ values; anisotropic paramagnetic limiting is a much more probable scenario [49] than orbital limiting since $H_{c2}^*(0)$ values are estimated $H_{c2}^{*,a}(0) \approx 3.8$ T and $H_{c2}^{*,c}(0) \approx 4.8$ T using the T_c and $(dH_{c2}/dT)_{T_c}$ values. These large $(dH_{c2}/dT)_{T_c}$ values, combined with a relatively large $\gamma = 65(2)$ mJ mol $^{-1}$ K $^{-2}$ value at ambient pressure [84], imply that quasiparticle masses in CePd_2Si_2 are enhanced. This value of γ was obtained by linearly extrapolating specific heat data, measured in the paramagnetic state and plotted as C/T vs. T^2 , to zero temperature [84]. Along with the case of CeIn_3 (see Section 2.2), the heavy-fermion superconductivity exhibited by CePd_2Si_2 was invoked to argue strongly in favor of the existence of magnetically-mediated pairing in the vicinity of a magnetic quantum critical point [58].

The compound CeRh_2Si_2 exhibits antiferromagnetic order at

Figure 2: Temperature-pressure phase diagram determined for CePd_2Si_2 . A dome of superconductivity is observed at low temperature (T_c values scaled by a factor of 3 for clarity) near the critical pressure where antiferromagnetic order, characterized by T_N , extrapolates to 0 K. The inset displays electrical resistivity data $\rho(T)$ vs. $T^{1.2}$ at a pressure of 2.8 GPa; the data obey a non-Fermi liquid $\rho(T) \propto T^{1.2}$ temperature dependence in the normal state. Adapted from Ref. [58].

ambient pressure below $T_{N,1} \approx 36$ K [82]; this magnetic order is characterized by a wave vector $\vec{Q} = (1/2, 1/2, 0)$ and a large ordered magnetic moment of $1.34 - 1.42 \mu_B/\text{Ce}$ [85]. Below $T_{N,2} \approx 24$ K, the magnetic structure changes so that it is described by two distinct wave vectors [85]. The low temperature properties of CeRh_2Si_2 are consistent with a Fermi liquid and the $\gamma \approx 23$ mJ mol $^{-1}$ K $^{-2}$ value, obtained from specific heat measurements within the antiferromagnetic state, is moderately enhanced [86]. Under applied pressure, γ increases rapidly to $\gamma \sim 80$ mJ mol $^{-1}$ K $^{-2}$ near 1.0 GPa, above which, it remains only weakly dependent on pressure [86]. Antiferromagnetic order is also suppressed by applied pressure and $T_{N,1}$ and $T_{N,2}$ vanish near 1.0 GPa and 0.6 GPa, respectively [85]. Near 1.0 GPa, a narrow dome of superconductivity with $T_c \approx 0.42$ K emerges [65]. It is at this pressure that antiferromagnetic order terminates in a first-order phase transition as confirmed by a discontinuous volume change in measurements of thermal expansion under applied pressure [87]. The upper critical field for CeRh_2Si_2 has been measured at ~ 1.1 GPa on a polycrystalline sample to be $H_{c2}(0) \approx 0.28$ T with an initial slope of $(dH_{c2}/dT)_{T_c} \approx -1$ T/K [65]. This value of $H_{c2}(0)$ is very close to the estimated orbital-limiting field $H_{c2}^*(0) \approx 0.29$ T and much smaller than $H_{p0} \approx 0.8$ T. From the upper critical field, it has been estimated that the quasiparticles in CeRh_2Si_2 have enhanced effective masses of $m^*/m_0 \approx 200$ [65]. For addi-

tional information, a description of the properties of the heavy-fermion superconductor CeRh₂Si₂ can be found in Ref. [88].

The 1-2-2 compounds CeCu₂Si₂, CeCu₂Ge₂, CePd₂Si₂, and CeRh₂Si₂ all exhibit antiferromagnetic order that, when suppressed by applied pressure, makes way for heavy-fermion superconductivity to emerge; in contrast to this pattern, the situation for the isostructural compound CeNi₂Ge₂ is more complicated and its superconductivity is less well understood. At ambient pressure, CeNi₂Ge₂ exhibits spin fluctuations with a wave vector $\vec{Q} = (0.23, 0.23, 0.5)$ [89] that is comparable to the SDW order in other 1-2-2 compounds; however, long-range order does not develop in CeNi₂Ge₂ down to the lowest temperatures. The measured $\gamma \approx 350 \text{ mJ mol}^{-1} \text{ K}^{-2}$ [90] definitely suggests that quasiparticles have enhanced effective masses; we note that γ might even be significantly higher depending on how it is defined since CeNi₂Ge₂ exhibits non-Fermi liquid behavior at ambient pressure, manifested by $C/T \approx -\ln(T)$ behavior at low temperature [91]. Traces of superconductivity were observed in CeNi₂Ge₂ below 0.1 K, however, attempts to resolve a diamagnetic Meissner signal were unsuccessful [91]. In CeNi₂Ge₂ samples with extremely low disorder, complete superconducting transitions were observed resistively below $T_c \approx 0.3 \text{ K}$ [69]; however, whether this is bulk superconductivity remains an open question. Traces of superconductivity, presumably distinct from the ambient-pressure superconducting phase, were also observed in measurements of electrical resistivity under applied pressure near 1.5 GPa with $T_c = 0.22 \text{ K}$ [92, 69]. The T_c value associated with this superconducting state increases with increasing pressure up to $T_c \approx 0.4 \text{ K}$ at 2.6 GPa [92]. If this superconductivity is intrinsic, it is possible that it could be related to a Ce valence instability as was observed in slightly Ge-doped CeCu₂Si₂ samples (*i.e.*, the phase diagram is similar to the one displayed in Fig. 1) [77, 78].

2.2. CeIn₃, CeMIn₅ ($M = \text{Co, Rh, Ir}$), and related compounds

2.2.1. Introduction

The discovery [94] of pressure-induced superconductivity in the heavy-fermion antiferromagnet CeRhIn₅ marked the beginning of subsequent discoveries of superconductivity in several related compounds. Each of these superconductors are members of a larger family of layered, tetragonal compounds with compositions Ce_nM_mIn_{3n+2m}, where M is a transition metal such as Co, Rh, Ir, Pd and Pt, with the subset of CeMIn₅ materials being $n = 1, m = 1$ members with $M = \text{Co, Rh, Ir}$. The basic structural building block of the family is the infinite layer, cubic compound CeIn₃, which earlier had been found to become superconducting with applied pressure [58]. Figure 3 compares the pressure-dependent evolution of the Néel temperature (T_N) and T_c in CeRhIn₅ and CeIn₃. In both cases, a dome of superconductivity appears as T_N is tuned toward $T = 0 \text{ K}$, but the maximum T_c of CeRhIn₅ is more than an order of magnitude higher than that of CeIn₃. This comparison suggests two significant conclusions: that fluctuations emerging from the $T = 0 \text{ K}$ magnetic quantum critical point may be responsible for Cooper pairing and that, as theoretically predicted [95], the quasi-two-dimensional crystal structure and associated electronic structure of CeRhIn₅ favors a higher T_c . Exploring the implications

Figure 3: (Color online) Pressure dependence of T_N and T_c in CeRhIn₅ (unfilled and filled circles, respectively) and CeIn₃ (unfilled and filled triangles, respectively). The phase diagrams for CeIn₃ and CeRhIn₅ were determined from electrical resistivity [58] and specific heat [93] measurements, respectively. Note that the T_c values of CeIn₃ are multiplied by a factor of 2 for clarity.

of these conclusions and, in particular, the relationship among magnetism, quantum criticality, and superconductivity has been a theme of subsequent studies of the Ce_nM_mIn_{3n+2m} superconductors.

Soon after the discovery of superconductivity in CeRhIn₅, superconductivity was discovered at atmospheric pressure in CeCoIn₅ and CeIrIn₅ [96, 97]. These two new members were the first Ce-based heavy-fermion superconductors to be found at atmospheric pressure since the original discovery of CeCu₂Si₂ [1], and the T_c of 2.3 K in CeCoIn₅ remains the highest among Ce-based heavy-fermion superconductors at atmospheric pressure. CeRhIn₅, CeCoIn₅, and CeIrIn₅ crystallize in the HoCoGa₅ structure type ($P4/mmm$), reported first by Grin *et al.* [98], and can be viewed as $n = 1$ layers of CeIn₃ separated by $m = 1$ layers of ‘MIn₂’ that are stacked sequentially along the tetragonal c -axis. In addition to the CeMIn₅ materials, superconductivity is also found in compounds with $n = 1, 2$ or 3 and $m = 1$ or 2 and in Pu-based analogs PuMX₅, where $M = \text{Co, Rh}$ and $X = \text{In or Ga}$. Table 1 summarizes the basic properties of superconductors in this broader family, all of which have been prepared in single crystal form and have large Sommerfeld coefficients. Non-magnetic variants of most of the Ce compounds have been prepared with La or Y and none is superconducting, which suggests that magnetism carried by the Ce ion is important for the appearance of superconductivity. Inspection of entries in this table also shows that the more structurally-anisotropic systems ($n = 1$) tend to have higher T_c ’s than those in which there are two ($n = 2$) or three ($n = 3$) adjacent CeIn₃ units. This trend is consistent with the proposal that reduced dimensionality enhances the pairing interaction in spin-mediated superconductivity [95]. Ce₂RhIn₈ and CeIrIn₅ are exceptions to this pattern, however, and we will return to them later. Of these systems, the CeMIn₅ (Ce115) materials

have been studied most and are the primary topic to be discussed. The properties of the Pu-analogs PuMX_5 are reviewed in a companion article in this issue of Physica C and are briefly touched upon in Section 4.3 of this article.

Band-structure calculations, confirmed through quantum-oscillation measurements, find that the Ce115's are nearly compensated metals with a multi-sheeted electronic structure dominated by warped cylinders characteristic of quasi-two-dimensional heavy band states [109, 110]. Though the effective magnetic moment above ~ 200 K is close to the Hund's rule value for Ce^{+3} , indicating that the $4f$ electron of Ce is localized in each of the Ce115's at high temperatures [94, 96, 97], the electronic structure reveals a different perspective. De Haas-van Alphen (dHvA) measurements find a 'small' Fermi volume in CeRhIn_5 , comparable to that of LaRhIn_5 , which does not contain any $4f$ electrons. On the other hand, the Fermi volume of CeCoIn_5 and CeIrIn_5 is 'large', implying that cerium's $4f$ electron has become part of the Fermi sea in these compounds because of relatively stronger $f - p, d$ hybridization at low temperature [109, 110]. Nevertheless, a two-dimensional-like Fermi surface topology is common to the Ce115's and would suggest that their physical properties should be relatively anisotropic. This is not the case. The normal state electrical resistivity ρ and magnetic susceptibility χ of the Ce115's as well as their superconducting properties are only somewhat anisotropic, with c -axis ρ and χ values about twice that of in-plane values [111]. The upper critical magnetic fields are similarly anisotropic [111].

2.2.2. Superconductivity

Because of a relatively high T_c at atmospheric pressure, superconductivity has been characterized most extensively in CeCoIn_5 . There is compelling evidence from several different types of experiments that the superconducting energy gap in CeCoIn_5 has nodes and, more specifically, that the gap symmetry is $d_{x^2-y^2}$. For example, the thermal conductivity [112] and specific heat [113] exhibit a four-fold modulation as magnetic field is rotated in the tetragonal basal plane, consistent with the presence of line nodes in the gap. More direct probes of the superconducting gap by point-contact [114] and tunneling spectroscopies [115, 116] confirm with little doubt a gap with $d_{x^2-y^2}$ symmetry in CeCoIn_5 ; this symmetry is also proven to exist in the high temperature cuprate superconductors from measurements sensitive to the phase of the order parameter [117]. Also like the cuprates [118], nodal superconductivity in CeCoIn_5 develops out of an unusual normal state in which the electronic structure is partially gapped. First implied from electrical resistivity studies [119], this inference has been verified by tunneling spectroscopy [115, 120] in which a signature for a pseudogap-like structure appears at temperatures somewhat higher than T_c . Additionally, the four-fold modulation of thermal conductivity well below T_c persists to temperatures at which the pseudogap emerges [112], suggesting that the pseudogap has the same nodal structure as the superconducting gap.

The presence of line nodes in the superconducting gap is reflected as well in power-law temperature dependencies of thermal conductivity ($\kappa \propto T^3$ [121] or $\kappa \propto T^2$ [122]), spe-

cific heat ($C \propto T^2$ [121]), and the nuclear spin-relaxation rate ($1/T_1 \propto T^{3+\epsilon}$ [123]) below T_c . The slightly greater than T^3 variation in $1/T_1$ and different power laws for κ may be a consequence of the multi-sheeted Fermi-surface topology of the Ce115's or the possibility that a small fraction of electrons at the Fermi surface does not participate in pairing, but these possibilities remain to be determined unambiguously. Nevertheless, in view of conclusions from tunneling spectroscopy, these power laws support the presence of line nodes in CeCoIn_5 and also set a benchmark for interpreting similar power laws in CeIrIn_5 and CeRhIn_5 [124]. As in CeCoIn_5 , there is a four-fold modulation in the specific heat of CeIrIn_5 [125, 126] and CeRhIn_5 [127] in their superconducting states, reinforcing the interpretation of gap nodes implied from power laws behaviors in them.

Table 2 summarizes the primary superconducting parameters of the Ce115's and includes, where available, corresponding properties of other family members based on Ce. A few comments about table entries are in order. The specific heat jump at T_c and ratio of superconducting gap to T_c are large in CeCoIn_5 and in the purely superconducting state of CeRhIn_5 at high pressures; this implies strong electron-boson coupling. In contrast, $\Delta C/\gamma T_c$ is considerably smaller in other examples. At least in Ce_2CoIn_8 , in which there are apparently two unidentified transitions above T_c [128], and in $\text{Ce}_3\text{PdIn}_{11}$ with two magnetic transitions above T_c [104], some entropy potentially available for superconductivity is removed by these transitions, which could be responsible in part for smaller jumps in specific heat. This effect is seen clearly in CeRhIn_5 where the specific heat jump at T_c is small in the pressure range with coexisting antiferromagnetic order and superconductivity but is large once magnetic order is suppressed completely [93]. CeIrIn_5 is a particularly interesting case. Its electrical resistivity drops to zero near 1.3 K with no clearly defined specific heat anomaly and bulk superconductivity only appears at 0.4 K [97]. Careful Hall effect and magnetoresistance measurements find evidence for a precursor state that extrapolates to ~ 2 K in the zero-field limit [129] where there is also a change in slope of C/T [97]. Conceivably, some entropy is associated with the precursor state that otherwise would be available for superconductivity. With applied pressure, the resistive transition to a $\rho = 0 \mu\Omega \text{ cm}$ state in CeIrIn_5 is essentially independent of pressure, but the bulk transition increases and eventually coincides with the resistive transition near 3 GPa, above which T_c decreases with further increasing pressure [130]. This response suggests that some other state is competing with superconductivity as was found in CeRhIn_5 as a function of pressure [131]. In this regard, we also note that no specific heat anomaly associated with bulk superconductivity has been found so far in Ce_2RhIn_8 at pressures up to 1.6 GPa and temperatures above 0.35 K [132] even though T_N extrapolates to 0 K near 2.5 GPa, which is close to where the resistive transition to $\rho = 0 \mu\Omega \text{ cm}$ reaches 2 K [102]. This is unusual and deserves further exploration.

The initial slope of the upper critical magnetic field near T_c , $(dH_{c2}/dT)_{T_c}$, is roughly twice as large for fields applied in the $a - b$ plane than perpendicular to it for CeCoIn_5 and CeIrIn_5 (for both its resistive and bulk transitions) and this is reflected as well in their $T = 0$ K upper critical fields $H_{c2}(0)$. Inter-

Table 1: Basic properties of members of the $\text{Ce}_n\text{M}_m\text{In}_{3n+2m}$ family as well as of the PuMX_5 materials. The tabulated properties are at ambient pressure unless designated by pressure (P) in units of GPa at which T_c is a maximum. We define SC = superconductivity and AFM = antiferromagnetism. The Sommerfeld coefficients are approximate, to order $\pm 10\%$, in some cases because of a relatively strong temperature dependence of C/T above a phase transition or because of a relative high T_c , *e.g.*, in PuMGa_5 materials.

Compound	Ground State	T_N, T_c (K)	γ (mJ mol ⁻¹ K ⁻²)	References
CeCoIn ₅	SC	2.3	250	[96]
CeRhIn ₅	AFM/SC (P)	3.8/2.4 (2.3 GPa)	430	[94]
CeIrIn ₅	SC	0.4	750	[97]
CePt ₂ In ₇	AFM/SC (P)	5.5/2.3 (3.1 GPa)	340	[99]
Ce ₂ CoIn ₈	SC	0.4	500	[100]
Ce ₂ RhIn ₈	AFM/SC (P)	2.8/2.0 (2.3 GPa)	400	[101, 102]
Ce ₂ PdIn ₈	SC	0.7	550	[103]
Ce ₃ PdIn ₁₁	AFM + SC	1.6 + 1.5 + 0.4 (SC)	300	[104]
PuCoIn ₅	SC	2.5	200	[105]
PuRhIn ₅	SC	1.6	200	[106]
PuCoGa ₅	SC	18.5	80	[107]
PuRhGa ₅	SC	8.7	80-150	[108]

Table 2: Superconducting parameters of the Ce115's and related materials. $\Delta C/\gamma T_c$: jump in specific heat at T_c divided by the Sommerfeld coefficient just above T_c ; $2\Delta/k_B T_c$: twice the zero-temperature superconducting energy gap divided by T_c (for CeRhIn₅ at 2.1 GPa, $T_c = 2.2$ K); $(dH_{c2}/dT)_{T_c}$ in units of T/K: slope of the upper critical field near T_c for field applied in the plane (ab) and perpendicular to it (c -axis); $\xi(0)$ in units of Å: Ginzburg-Landau coherence length calculated from the measured zero-temperature upper critical field for field along the c -axis ($\xi_{ab}(0)$) and in the basal plane ($\xi_c(0)$); λ in units of Å: magnetic penetration depth perpendicular (λ_{ab}) and parallel to the c -axis (λ_c). Because of the different T_c 's determined by electrical resistance (~ 1.3 K) and by a bulk measurement (0.4 K) through susceptibility (χ) or specific heat (C), there are associated differences in $(dH_{c2}/dT)_{T_c}$ and $\xi_{ab,c}(0)$ for CeIrIn₅. References for each value are provided in brackets.

Compound	$\Delta/\gamma T_c$	$2\Delta/k_B T_c$	dH_{c2}^{ab}/dT	dH_{c2}^c/dT	$\xi_c(0)$	$\xi_{ab}(0)$	λ_{ab}	λ_c
CeCoIn ₅	4.5 [96]	10 [123]	-24 [133]	-11 [133]	53 [134]	82 [96]	1900 [135]	2700 [135]
	4.7 [133]	6.05 [136]		-8.2 [121]		82 [133, 134]	1900 [137]	2800 [138]
CeRhIn ₅	4.2 [139]	5 [140]	-15.5 [141]	-15.5 [141]	57 [141]	48 [141]		
CeIrIn ₅	0.76 [97]	5.0 [142]	-4.8 [97]	-2.5 [97]	180 [97, 109]	260 [109]	6700 [143]	
		5 [123]	-10 [97]	-5 [97]	71 [97]	115 [109]		
CePt ₂ In ₇	1.5 [99]			-12 [99]				
Ce ₂ CoIn ₈	0.2 [128]				175 [128]	190 [128]		
Ce ₂ RhIn ₈			-9.2 [102]		77 [102]			
Ce ₂ PdIn ₈	1.2 [144]		-14 [145]	-14.3 [144]	130 [144]	120 [144]	1740 [144]	
Ce ₃ PdIn ₁₁	0.6 [104]		-9.6 [104]			120 [104]	9200 [104]

Figure 4: (Color online) Temperature versus pressure phase diagram of CeRhIn_5 determined from specific heat measurements [93]. Regions of antiferromagnetic order and superconductivity are indicated by AFM and SC, respectively.

estingly, even though the Fermi-surface topology appears to be similar in CeCoIn_5 and in CeRhIn_5 at high pressures [146], this anisotropy is reversed in CeRhIn_5 once magnetic order has been suppressed by pressure [141]. The origin of this anisotropy reversal is not currently understood and remains an important issue to be resolved. Below $0.3T_c$, the upper critical field transition in CeCoIn_5 is first order, consistent with strong Pauli limiting [147]. Although there is no clear evidence that the critical field transition becomes first order, it is also Pauli limited in CeRhIn_5 at high pressures [141] and in Ce_2PdIn_8 [144]. It also is noteworthy that $H_{c2}(0)$ is nearly isotropic in the $n = 2$, $m = 1$ compounds Ce_2CoIn_8 and Ce_2PdIn_8 , which might be expected because of their more three-dimensional crystal and, presumably, electronic structures. From this perspective, the upper critical fields of the $n = 3$, $m = 1$ material $\text{Ce}_3\text{PdIn}_{11}$ also should be nearly isotropic, but this remains to be seen.

2.2.3. Magnetism, Quantum Criticality, and Superconductivity

CeRhIn_5 and CeCoIn_5 exemplify the complex interplay among magnetism, quantum criticality, and superconductivity that makes them and other members of the $\text{Ce}_n\text{M}_m\text{In}_{3n+2m}$ family so fascinating. Figure 4 provides a detailed temperature-pressure phase diagram of CeRhIn_5 . Below a critical pressure P_1 , there is a range of pressures where incommensurate antiferromagnetic order coexists microscopically with superconductivity [148]. In this same pressure range, the ordered magnetic moment is only somewhat reduced relative to that expected of Ce^{3+} in a crystal-field doublet ground state [149, 150]. A first-order-like very small change in the c -axis incommensuration of the magnetic order appears where bulk superconductivity sets in at 1.5 GPa, signaling an interplay between the coexisting antiferromagnetic order and superconductivity [150]. Above P_1 , there is no evidence for coexisting antiferromagnetism in zero applied field, but applying a magnetic field induces mag-

Figure 5: (Color online) Magnetic field-temperature phase diagram for CeCoIn_5 determined for $H \parallel a - b$ plane. The Q-phase is bounded by the first-order upper critical field $H_{c2}(T)$ and a line of second-order phase transitions indicated by solid circles. After Ref. [154].

netic order in the superconducting state [93, 151]. The applied magnetic field also allows the Néel boundary to be followed toward its $T = 0$ K quantum critical point (P_2 in Fig. 4) near 2.3 GPa, where there is an abrupt increase in the dHvA frequencies to values that characterize the large-volume quasi-two-dimensional cyclotron orbits of CeCoIn_5 [146]. Above this dome of unconventional superconductivity, the spin-relaxation rate follows a distinctly non-Fermi-liquid temperature dependence ($1/T_1 \propto T^{1/2}$) [152], the resistivity just above T_c increases by over a factor of 20, and the temperature dependence of the electrical resistivity increases as $T^{0.85}$ [153]. Collectively, these responses suggest that the maximum T_c in CeRhIn_5 is associated with an unconventional type of quantum criticality in which magnetic as well as electronic degrees of freedom become critical at P_2 [153].

Unconventional superconductivity in CeCoIn_5 develops from a non-Fermi-liquid normal state at atmospheric pressure [96, 119, 123]. Its dome-shaped $T_c(P)$ [119] suggests, like CeRhIn_5 , that antiferromagnetic order is ‘nearby’. Indeed, replacing about 1% of its In atoms by Cd induces coexisting superconductivity and commensurate antiferromagnetism with a large ordered moment of $\sim 0.7\mu_B$ [155, 156, 157]. Applying a magnetic field to pure CeCoIn_5 , however, reveals evidence for a SDW-like quantum critical point near or just inside its $T = 0$ K upper critical field [158, 159, 160]. The Wiedemann-Franz law is violated near this quantum critical point for transport along the c axis, but is obeyed for in-plane transport [161]. This result points to an anisotropic destruction of the Fermi surface of CeCoIn_5 that is reminiscent of the pseudogap state in the underdoped cuprates and is possibly caused by spin fluctuations with a uniaxial character. Careful specific heat measurements reveal a phase transition just below $H_{c2}(0)$ when the field is applied in the basal plane of CeCoIn_5 . This phase transition, first identified as a possible Fulde-Ferrell-Larkin-Ovchinnikov (FFLO)

state [154], subsequently was shown by nuclear magnetic resonance (NMR) measurements to host antiferromagnetic order [162, 163]. More recent neutron-diffraction experiments confirm field-induced incommensurate magnetic order with a small ordered moment of $0.15\mu_B$ and further show that it is coupled to superconductivity and exists only in the so-called Q-phase illustrated in Fig. 5 [164]. Coupling of the SDW to d -wave superconductivity leads to a highly non-trivial state in which triplet p -wave superconductivity is induced [165]. The resulting spatially-modulated superconducting state is similar to an FFLO phase originally suggested from specific heat studies, but whether antiferromagnetism coexists with an FFLO state in the Q-phase remains to be determined. Applying pressure increases the $H - T$ phase space occupied by the Q-phase [166], which is surprising because pressure typically tends to suppress SDW order in Ce-based systems. In contrast, replacing only 0.05% of the In atoms by Hg wipes out any thermodynamic signature for it [167]. Besides a magnetic field, Nd substitution in CeCoIn₅ induces magnetic order inside the zero-field superconducting state of CeCoIn₅ for Nd concentrations less than 10% [168]. Neutron diffraction measurements find that the Nd-induced antiferromagnetism has the same ordering wavevector and nearly the same small ordered moment as those in the Q-phase [169], raising the possibility that the two phenomena may be related.

Neodymium concentrations greater than 15% suppress superconductivity and, at this concentration, the electrical resistivity reaches $\sim 20 \mu\Omega \text{ cm}$ [168]. Interestingly, it is this value of the low-temperature electrical resistivity and not pair breaking by the magnetic moment of Nd that correlates with the suppression of superconductivity. As found in a systematic study of T_c suppression by chemical substitution of Ce with various trivalent magnetic and non-magnetic lanthanides, T_c reaches zero when the resistivity reaches $\sim 20 \mu\Omega \text{ cm}$, irrespective of the substituent [170, 168]. This correlation suggests [170] an intimate relationship between the quantum criticality of CeCoIn₅ and incoherent scattering produced by the introduction of Ce ‘vacancies’ that manifest themselves as Kondo-impurity scatterers in the superconducting state [171]. Ytterbium substitution for Ce in bulk single crystals of Ce_{1-x}Yb_xCoIn₅ appeared to be a dramatic exception in that T_c extrapolated to 0 K only in the limit $x \rightarrow 1$ [172, 173]; however, a study of Ce_{1-x}Yb_xCoIn₅ thin films revealed a more rapid suppression rate of T_c with x such that superconductivity vanished near $x = 0.4$ [174]. The discrepancy between these results was recently resolved via an unconventional application of Vegard’s law in which it was determined that the actual Yb concentration x_{act} in bulk single crystals is subnominal (*i.e.*, $x_{act} < x$) [175]. Measurements of the Yb and Ce valences in Ce_{1-x}Yb_xCoIn₅ [176, 177] reveal that Ce is nearly trivalent for all x and that the Yb valence decreases rapidly with increasing x from 3+ to a stable intermediate valence of 2.3+ for $x \geq 0.2$ [177]. The measured unit-cell volume [172, 173], $V(x)$, is inconsistent with Vegard’s law; however, the Yb concentration was adjusted in a plot of V vs. x until $V(x_{act})$ was consistent with Vegard’s law [175]. From this analysis, a correction function for the true Yb concentration, $x_{act}(x)$, was obtained that is consistent with independent measurements of the Yb concentration using wave-

length dispersive spectroscopy, energy dispersive spectroscopy, and transmission x-ray absorption spectroscopy measurements [175, 173]. It was found that $x_{act} = x/3$ in bulk single crystals up to $x \sim 0.5$ [175]. The behavior of $T_c(x_{act})$ for the bulk single crystals [175] is consistent with that of thin films of Ce_{1-x}Yb_xCoIn₅ [174], resolving the discrepancy between their respective behaviors. Interestingly, superconductivity still persists to higher concentrations [175, 174] ($x_{act} \simeq 0.4$) than in cases where other rare-earth ions are substituted for Ce ($x_{act} \sim 0.2$) [170, 168, 178].

Motivated by the anomalous physical properties exhibited by Ce_{1-x}Yb_xCoIn₅ [172, 173, 174], numerous studies have been performed to probe this system’s superconducting and normal state properties [179, 180, 181, 182, 183]. Interestingly, near $x = 0.2$ ($x_{act} \simeq 0.067$), an intriguing crossover is observed. A valence transition occurs at this concentration where the Yb valence, which decreases rapidly from nearly 3+ to 2.3+ for $x_{act} < 0.067$, maintains a stable intermediate valence of 2.3+ for $x_{act} \geq 0.067$ [177]. This valence transition is concomitant with a reconstruction of the Fermi-surface topology wherein the heavy α sheets disappear and the Fermi surface resembles that of YbCoIn₅ instead of CeCoIn₅ [184]. Furthermore, from careful measurement of the in-plane magnetoresistivity of Ce_{1-x}Yb_xCoIn₅ in magnetic fields up to 14 T [180], it has been shown that the quantum critical field associated with the field-induced quantum critical point ($H_{QCP} = 5 \text{ T}$ for CeCoIn₅) is suppressed to 0 T near $x = 0.2$; therefore, the quantum critical point is suppressed by Yb substitution and the non-Fermi liquid behavior that persists to much higher Yb concentrations in Ce_{1-x}Yb_xCoIn₅ must be decoupled from its associated quantum criticality [180]. It has also been shown that quantum critical fluctuations near $x = 0.2$ are suppressed with increasing pressure [183]. Despite all of these dramatic transitions and crossovers near $x = 0.2$, there is no apparent feature in $T_c(x)$ at this concentration.

Recent measurements of the London penetration depth Δl have provided compelling evidence that the nodes, presumed to be associated with a $d_{x^2-y^2}$ symmetry of the superconducting energy gap, disappear near $x = 0.2$ in Ce_{1-x}Yb_xCoIn₅ [182]. Whereas substitution with La and Nd for Ce results in a power-law temperature dependence of $\Delta l \sim T^n$ in which the exponent n rapidly approaches $n = 2$, indicating d -wave superconductivity in the dirty limit, Yb substitution for Ce results in an exponent of $n \geq 3$ (see Fig. 6) [182]. This observation implies that there is a topological transition of the superconducting energy gap symmetry in Ce_{1-x}Yb_xCoIn₅ from nodal to nodeless near $x = 0.2$ [182]. This surprising result might be explained by a composite pairing scenario in which a Lifshitz transition of the nodal Fermi surface is driven by Yb substitution, forming a fully-gapped d -wave molecular superfluid of composite pairs [185]. The $\Delta l \sim T^4$ dependence of the penetration depth associated with the sound mode of this condensate agrees with the experimental results reported in Ref. [182].

If the composite pairing scenario for superconductivity in Ce_{1-x}Yb_xCoIn₅ ($x > 0.2$) applies, Ref. [185] predicts that the nodal behavior will return at a second quantum critical point at higher Yb concentration. The higher Yb concentration region

Figure 6: (Color online) Exponents n for power-law behavior of low-temperature London penetration depth $\Delta\lambda(T)$ data (see text) for the compounds $\text{Ce}_{1-x}\text{R}_x\text{CoIn}_5$ ($R = \text{La}, \text{Nd}, \text{Yb}$), plotted as a function of (a) $T_c(x)/T_c(0)$ and (b) x . Filled circles correspond to $R = \text{La}$, filled upward-facing triangles correspond to $R = \text{Nd}$, and filled downward-facing triangles correspond to $R = \text{Yb}$. Dashed lines serve as guides to the eye emphasizing $n = 2$, which is the expected exponent for a d -wave superconductor in the dirty limit. After Ref. [182].

of the phase diagram of $\text{Ce}_{1-x}\text{Yb}_x\text{CoIn}_5$ is, therefore, currently being explored. The evolution of the many-body electronic state from a Kondo lattice consisting of Ce magnetic moments for low Yb concentration to a dilute array of Ce impurities at high x has been studied [181]. A crossover was observed near $x = 0.6$ between a regime characterized by localized Ce magnetic moments and one predominantly consisting of itinerant Yb electronic states [181]. Electronic correlations between the Yb ions can be inferred, and these Yb-Yb correlations appear to be particularly strong for $0.65 \leq x \leq 0.775$ according to measurements of specific heat [181]. The search for a second quantum critical point as well as reconciling the notion of nodeless d -wave superconductivity with our understanding of heavy-fermion superconductivity make the system $\text{Ce}_{1-x}\text{Yb}_x\text{CoIn}_5$ a rich and intriguing playground within which to study the evolution and interplay of unconventional superconductivity, electronic structure, valence fluctuations, and quantum criticality.

The phase diagram in Fig. 7 of temperature versus x in the $\text{Ce}M_xM'_{1-x}\text{In}_5$ series, where $M = \text{Rh}, \text{Ir}, \text{Co}$, provides a broad perspective on the relationship between magnetism and superconductivity in the Ce115's [186]. In this figure, phase boundaries indicated by symbols are determined by specific heat for $\text{CeRh}_x\text{Co}_{1-x}\text{In}_5$ [187] and $\text{CeRh}_{1-x}\text{Ir}_x\text{In}_5$ [188]; whereas, dotted phase boundaries are deduced from neutron diffraction measurements on $\text{CeRh}_x\text{Co}_{1-x}\text{In}_5$ [189] and $\text{CeRh}_{1-x}\text{Ir}_x\text{In}_5$ [190]. With both Co and Ir substitution for Rh, superconductivity appears once the magnetic order is either commensurate (Co doping) or incommensurate coexisting with commensurate antiferromagnetism (Ir doping). In the case of Ir substitutions, nuclear quadrupole resonance experiments show that superconductivity coexists microscopically with magnetic order [191], and this is inferred as well from specific heat studies of Co-substituted crystals [187]. It seems, therefore, that commensurate order

Figure 7: (Color online) Phase transitions in $\text{Ce}M_xM'_{1-x}\text{In}_5$ compounds as $M = \text{Rh}$ is replaced by $M' = \text{Ir}$ and Co . In this figure, we define ICAF = incommensurate antiferromagnetism; CAF = commensurate antiferromagnetism; SC = superconductivity. After Ref. [186].

allows or favors the development of d -wave superconductivity in these systems, which appears as well to be the case in CePt_2In_7 [192]. Though there are important commonalities in the relationship between superconductivity and magnetism across the series, there are also significant differences. With Ir substitution, a dome of superconductivity appears that is centered somewhat below the critical Ir content at which the Néel boundary extrapolates to $T = 0$ K. Near 90% Ir, T_c goes to zero and this notch in $T_c(x)$ widens with applied pressure, while T_c of CeIrIn_5 increases and the T_c of samples with lower Ir content grows toward $T_c \sim 2$ K; this value is comparable to that of pure CeRhIn_5 under pressure [193]. This response to pressure suggests that there may be two superconducting phases in the $\text{CeRh}_{1-x}\text{Ir}_x\text{In}_5$ series. On the other hand, with increasing Co content, superconductivity appears suddenly at a Co concentration of $\sim 40\%$, and again, applied pressure enhances T_c toward 2 K [194]. The rapid onset of superconductivity at ambient pressure appears to be associated with a jump in the cyclotron frequency of at least one heavy-mass sheet of the Fermi surface to a value typical of the large Fermi volume of pure CeCoIn_5 [195]. Though it seems likely that the broad dome of superconductivity in Ir-doped CeRhIn_5 may be associated with a magnetic quantum critical point, this is not the case with Co-doping where dHvA measurements do not find a diverging mass near 40% Co [195].

2.2.4. Superconducting Mechanism and Broader Relationships

Without a phase-sensitive measurement, it is not possible to prove that superconductivity in the Ce115's is unconventional. Nevertheless, all measurements consistently point to the conclusion that it is and that the pairing has a nodal, spin-singlet character. With superconductivity appearing in proximity to antiferromagnetism in these as well as other members of the broader family and the development of superconductivity out of

a non-Fermi-liquid normal state, it is reasonable to expect that fluctuations of a quantum-critical nature play a dominant role in producing Cooper pairing [196]. In CeCoIn₅, this criticality is of the conventional Hertz-Millis-Moriya type that involves only critical fluctuations of a magnetic order parameter [158], which favors pairing in the *d*-wave channel. In contrast, the critical response of CeRhIn₅ under pressure is consistent with criticality of magnetic as well as electronic degrees of freedom [127]. Such an unconventional type of quantum criticality also favors *d*-wave pairing [197]. Though Fig. 7 implies that superconductivity in CeIrIn₅ is separated from magnetism, NMR and specific heat measurements argue that CeIrIn₅ is close to a $T = 0$ K instability of a SDW at ambient pressure [198, 199], which again would favor magnetically-mediated *d*-wave pairing.

A neutron-spin resonance develops in the superconducting state of CeCoIn₅ [200], with the ratio of resonance energy to superconducting gap being the same as in the cuprates [201]. Further searches for a neutron resonance in CeRhIn₅ under pressure and in CeIrIn₅ will be challenging, but worthwhile. Besides the spin resonance, results of scanning tunneling spectroscopy [202, 115] strongly support magnetic pairing in CeCoIn₅. Remarkably, this magnetically-mediated superconductivity persists in thin films that are just a few monolayers thick [203]. Magnetically-mediated *d*-wave superconductivity and the presence of a pseudogap and spin resonance as well as a non-Fermi-liquid normal state above T_c in the Ce115's are strikingly similar to the high- T_c cuprates. Though the absolute value of T_c is much lower in the Ce115's than in the cuprates, relative to the electronic energy/magnetic scale relevant for superconductivity, the T_c 's of the Ce115's are just as high as those in the cuprates [204]. The ease with which superconductivity in the Ce115's can be tuned and with which they can be grown as very high quality crystals, in addition to the perspective provided by dimensional tuning in the broader Ce_{*n*}M_{*m*}In_{3*n*+2*m*} family, make these materials particularly useful for unraveling commonalities in heavy-fermion superconductors and unconventional superconductors more broadly.

2.3. Noncentrosymmetric Ce-based compounds

Superconductivity in Ce-based heavy-fermion compounds with noncentrosymmetric crystal structures is an exciting, relatively new area of research. Much of the interest in this topic is driven by the rather unique possibility of superconductivity exhibiting an unconventional mixture of *s*- and *p*-wave pairing that is allowed when inversion symmetry is absent. This fascinating and rich subject has been reviewed recently by Kimura and Bonalde in Ref. [205] and is also the subject of a review article by F. Kneidinger *et al.* in this special issue of Physica C. Therefore, we will only touch briefly on the properties of four Ce-based heavy-fermion compounds with noncentrosymmetric crystal structures: the compound CePt₃Si exhibits superconductivity at ambient pressure [206] while pressure-induced superconductivity is observed in CeRhSi₃, CeIrSi₃, and CeCoGe₃ [207, 208, 209].

The crystal structure of CePt₃Si is described by tetragonal space group *P4mm* which lacks inversion symmetry [206]. Long-range antiferromagnetic order is observed below $T_N = 2.2$

K with superconductivity emerging near $T_c = 0.75$ K at ambient pressure [206]. As is discussed in Ref. [49], some samples of CePt₃Si exhibit $T_c \approx 0.45$ K with sharper phase transitions. A Sommerfeld coefficient, $\gamma = 390$ mJ mol⁻¹ K⁻², is measured which is consistent with heavy-fermion behavior [206]. Furthermore, a jump in the specific heat of $\Delta C/\gamma T_c \approx 0.25$ is observed at T_c , confirming that superconductivity is bulk in CePt₃Si [206]. The upper critical fields were found to be $H_{c2}(0) \sim 5$ T at zero temperature with an initial slope of $(dH_{c2}/dT)_{T_c} \approx -8.5$ T/K from measurements of polycrystalline samples [206]. This value of $H_{c2}(0)$ is comparable to the estimated [59] orbital limiting field $H_{c2}^*(0) \approx 4.4$ T and significantly exceeds the estimated [71] Pauli limiting field of $H_{p0} \approx 1.4$ T. Since $H_{c2}(0) \gg H_{p0}$, we expect that pairing in CePt₃Si is unconventional and involves spin-triplet pairs. Upper critical field measurements on a single crystal of CePt₃Si with $T_c = 0.63$ K demonstrated very little anisotropy in $H_{c2}(T)$ curves and the extrapolated $H_{c2}(0)$ values also exceeded the Pauli paramagnetic limit [210]. For more information concerning the early work on CePt₃Si, see Ref. [211].

Pressure-induced superconductivity was observed in the compounds CeRhSi₃ [207], CeIrSi₃ [208], and CeCoGe₃ [209] that all form in a noncentrosymmetric crystal structure characterized by the tetragonal space group *I4mm*. In each case, antiferromagnetic order is suppressed by applied pressure, enabling superconductivity to emerge. Enhanced Sommerfeld coefficient values of $\gamma \approx 120$ mJ mol⁻¹ K⁻² [207], 120 mJ mol⁻¹ K⁻² [208], and 32 mJ mol⁻¹ K⁻² [212] for CeRhSi₃, CeIrSi₃, and CeCoGe₃, respectively, are observed at ambient pressure. These values suggest that the effective quasiparticle masses are enhanced in these compounds. At ambient pressure, the magnetic ordering temperatures are $T_N \approx 1.6$ K and $T_N \approx 5$ K for CeRhSi₃ and CeIrSi₃ [207, 208], respectively, while CeCoGe₃ exhibits three successive transitions at $T_{N1} \approx 21$ K, $T_{N2} \approx 12$ K, and $T_{N3} \approx 8$ K [209]. Under applied pressure, antiferromagnetic order is suppressed in each compound and superconductivity emerges. For CeRhSi₃, superconductivity is observed at pressures above ~ 1.2 GPa and exists in a wide dome up to 3 GPa with maximum $T_c \approx 1$ K near 2.3 GPa [207]; the lower-pressure side of the dome appears to coexist with antiferromagnetic order [207]. For CeIrSi₃, antiferromagnetic order vanishes for pressures near 2.25 GPa, and a dome of superconductivity is observed with maximum $T_c \approx 1.65$ K near 2.6 GPa [208]. Finally, applied pressure suppresses antiferromagnetic order in CeCoGe₃ with T_{N1} (the highest magnetic transition temperature) vanishing near 5.5 GPa [209]. Superconductivity is observed in a broad dome centered near 6.5 GPa with maximum $T_c \approx 0.69$ K [209]. The upper critical fields of these compounds are all enormous and significantly exceed their respective Pauli paramagnetic limits. Initial slopes of $(dH_{c2}/dT)_{T_c} \approx -23$ T/K (2.6 GPa) and -20 T/K (at 6.5 GPa) for CeRhSi₃ [213] and CeCoGe₃ [212], respectively, suggest that $H_{c2}(0)$ values may exceed 30 T for these compounds when $H \parallel c$! For CeIrSi₃, the upper critical field values at 2.65 GPa and zero temperature are $H_{c2}^a(0) \approx 9.5$ T and $H_{c2}^c(0) \approx 45$ T with initial slopes of $(dH_{c2}^a/dT)_{T_c} \approx -14.5$ T/K and $(dH_{c2}^c/dT)_{T_c} \approx -17$ T/K (as seen in Fig. 8) [214]. These values of $H_{c2}(0)$ are also consistent with

Figure 8: (Color online) The anisotropic upper critical fields $H_{c2}(T)$ for CeIrSi₃. The magnetic field H is applied along the c -axis under applied pressures of 2.60 GPa (filled circles) and 2.65 GPa (unfilled circles), and along [110] under an applied pressure of 2.65 GPa (unfilled squares). The dramatic anisotropy in $H_{c2}(T)$ is apparent and the $H_{c2}^c(0)$ value appears to be close to 40 T at 2.60 GPa (after Ref. [214]).

spin-triplet pairing and attest to the unconventional nature of pressure-induced superconductivity in these noncentrosymmetric heavy-fermion compounds.

2.4. CeNiGe₃, Ce₂Ni₃Ge₅, and CePd₅Al₂

We conclude our discussion of Ce-based heavy-fermion superconductors by discussing three compounds that do not fall neatly into the categories we have just discussed. This includes CeNiGe₃, Ce₂Ni₃Ge₅, and CePd₅Al₂, and the properties of each compound are briefly addressed below.

Though it has the same 1-1-3 stoichiometry as many of the noncentrosymmetric superconductors discussed in Section 2.3, the compound CeNiGe₃ crystallizes with the centrosymmetric orthorhombic space group $Cmmm$ and exhibits antiferromagnetic order below $T_N \approx 5.5$ K at ambient pressure [215]. In an analysis of specific heat data that includes fitting a Schottky-anomaly feature, the Sommerfeld coefficient was reported to be $\gamma \approx 45$ mJ mol⁻¹ K⁻² [215]. Analysis of Curie-Weiss behavior in the magnetic susceptibility of CeNiGe₃ provides a μ_{eff} value that is very close to the expected value for a localized magnetic moment associated with Ce³⁺ ions [215]. Under applied pressure, T_N initially increases up to about ~ 3 GPa and then rapidly decreases, vanishing near ~ 5.5 GPa [216]; an incomplete superconducting transition was first reported in $\rho(T)$ measurements of CeNiGe₃, and a dome of superconductivity, centered near this critical pressure with maximum $T_c \approx 0.48$ K as defined by the transition's onset, was obtained in the temperature-pressure phase diagram [216]. Measurements of CeNiGe₃ under pressure were later conducted with improved

pressure homogeneity, obtaining qualitatively different results [217]. In the study of Kotegawa *et al.*, superconductivity first emerges near 1.7 GPa (coexisting with the antiferromagnetic phase of CeNiGe₃) and traces out two distinct superconducting domes with maximum T_c values of 0.32 K and 0.43 K near pressures of ~ 3.5 GPa and ~ 6.8 GPa, respectively [217]; this higher pressure coincides with the suppression of T_N to 0 K [217]. The observation of a diamagnetic signal in the magnetic susceptibility suggests that the superconductivity associated with the lower pressure dome could be bulk. In contrast, the superconducting transition within the higher pressure dome becomes incomplete in measurements of electrical resistivity conducted in modest magnetic fields [217]; this observation suggests that the higher pressure phase might not be bulk superconductivity [217]. The upper critical field of CeNiGe₃ at zero temperature was found to increase significantly under applied pressure from $H_{c2}(0) \approx 0.02$ T at 1.9 GPa to $H_{c2}(0) \approx 1.56$ T at 6.8 GPa [217]. The initial slope of the upper critical field experiences a comparable increase from $(dH_{c2}/dT)_{T_c} \approx -0.24$ T/K at 1.9 GPa to $(dH_{c2}/dT)_{T_c} \approx -10.8$ T/K at 6.8 GPa [217]. Below 3.4 GPa, superconductivity is orbitally-limited, but it is probably paramagnetically-limited in the higher pressure dome [217]. Though the question of whether superconductivity at higher pressure is bulk remains an outstanding issue, the large observed value of $(dH_{c2}/dT)_{T_c} \approx -10.8$ T/K at 6.8 GPa and the appearance of superconductivity in the vicinity of a suppressed antiferromagnetic phase are consistent with the usual signatures of heavy-fermion superconductivity.

The compound Ce₂Ni₃Ge₅ crystallizes with orthorhombic space group $Ibam$ [218]. A Sommerfeld coefficient of $\gamma \approx 90$ mJ mol⁻¹ Ce⁻¹ K⁻² is obtained [219], and antiferromagnetic order, characterized by phase transitions at $T_{N,1} = 5.1$ K and $T_{N,2} = 4.5$ K, is exhibited by Ce₂Ni₃Ge₅ [219, 218]. The magnetic entropy recovered at $T_{N,1}$ is $S_{mag} \approx 0.67R \ln 2$, which is reduced slightly from the expected S_{mag} for a doublet ground state because of the Kondo effect [219]. A neutron diffraction study on a polycrystalline sample of Ce₂Ni₃Ge₅ was only able to resolve the transition at $T_{N,1}$ and obtained ordered moments of $0.4(1) \mu_B/\text{Ce}$ at 1.4 K, polarized antiparallel to one another along the a axis [218]. Under applied pressure, $T_{N,1}$ is suppressed, vanishing completely near 3.9 GPa; it was not possible to track $T_{N,2}$ as a function of applied pressure due to broadening of the feature associated with this transition [220]. Near 3.9 GPa, a dome of superconductivity is observed with maximum $T_c \approx 0.26$ K (defined by the onset) [220]. At 3.6 GPa, an upper critical field of $H_{c2}(0) \approx 0.7$ T is measured at 0 K and the initial slope is $(dH_{c2}/dT)_{T_c} \approx -8$ T/K [220]. This value of $H_{c2}(0)$ slightly exceeds the Pauli paramagnetic limiting field, estimated to be $H_{p0} \approx 0.48$ T, but is roughly a factor of 2 smaller than the estimate for $H_{c2}^*(0) \approx 1.4$ T. This result implies that superconductivity in Ce₂Ni₃Ge₅ is paramagnetically-limited, and the enhanced values of γ and $(dH_{c2}/dT)_{T_c}$ suggest that heavy quasiparticles participate.

The final compound we will discuss in this section is CePd₅Al₂. Following the discovery of superconductivity in the isostructural compound NpPd₅Al₂ [221] (see Section 4.3), pressure-induced superconductivity was observed in this heavy-

fermion compound. In CePd_5Al_2 , two distinct antiferromagnetic states are observed at ambient pressure that are characterized by $T_{N,1} = 3.9$ K and $T_{N,2} = 2.9$ K [222]. The Sommerfeld coefficient value for CePd_5Al_2 is $\gamma \approx 56$ mJ mol⁻¹ K⁻² at ambient pressure [222], which is consistent with modestly-enhanced quasiparticle masses. Under applied pressure, $T_{N,1}$ first increases and then decreases with increasing pressure up to ~ 8 -9 GPa [222]; in the vicinity of this critical pressure, a dome of superconductivity is observed. The maximum $T_c \approx 0.57$ K is observed near 10.8 GPa and measurements of the upper critical field values at this pressure with $H \parallel c$ yield $H_{c2}^c(0) \approx 0.25$ T with initial slope $(dH_{c2}^c/dT)_{T_c} \approx -1.04$ T/K [222]. This value of $H_{c2}(0)$ is roughly a factor of 2 smaller than the orbital limit, estimated to be $H_{c2}^{*,c}(0) \approx 0.41$ T using the values of T_c and $(dH_{c2}^c/dT)_{T_c}$. On the other hand, $H_{c2}(0) \ll H_{p0} \approx 1$ T, so further investigations will be necessary to identify the primary pair-breaking mechanism for superconductivity in CePd_5Al_2 in a magnetic field.

3. U-based heavy-fermion superconductors

3.1. Introduction

Following the discovery of heavy-fermion superconductivity in CeCu_2Si_2 in 1979 [1], four superconducting uranium compounds with large γ values were identified in the time frame 1983-84: UBe_{13} ($T_c = 0.9$ K, $\gamma = 1.0$ J mol⁻¹ K⁻²) [52], U_6Fe ($T_c = 4.0$ K, $\gamma = 24$ mJ mol⁻¹ K⁻²) [225], UPt_3 ($T_c = 0.54$ K, $\gamma = 450$ mJ mol⁻¹ K⁻²) [53], and U_2PtC_2 ($T_c = 1.5$ K, $\gamma = 75$ mJ mol⁻¹ K⁻²) [228]. These observations quickly demonstrated that heavy-fermion behavior is a general phenomenon that is not restricted to Ce-based compounds and generated an enormous amount of interest in the physics of heavy-fermion materials. Interestingly, Bucher *et al.* had already reported superconductivity in UBe_{13} [50]; however, the superconductivity was attributed to filaments of uranium since it persisted in high magnetic fields. Specific heat measurements by Ott *et al.* showed that UBe_{13} displayed bulk superconductivity with an enormous value of γ [52] comparable with that of CeCu_2Si_2 . The compound U_6Fe was already known to exhibit superconductivity according to the work of Chandrasekar and Hulm [265]. Magnetoresistance measurements by DeLong *et al.* demonstrated that U_6Fe has a rather large upper critical field $H_{c2}(T)$ whose magnitude is consistent with its value of γ [225]. The bulk superconductivity of UPt_3 observed by Stewart *et al.* [53] had not previously been reported.

The compounds UBe_{13} and UPt_3 both exhibit unconventional superconductivity in which the pairing of electrons is widely believed to be mediated by magnetic interactions rather than the electron-phonon interaction. The observation of superconducting properties with power-law temperature dependencies provides evidence for anisotropic superconductivity in which the electrons are paired in states with angular momentum greater than zero and the energy gap vanishes at points or on lines on the Fermi surface. An example of the extraordinary properties of the superconducting state in these materials is the upper critical field of UBe_{13} . There is also evidence for multiple superconducting phases, presumably with different order parameter

symmetries, in $\text{U}_{1-x}\text{Th}_x\text{Be}_{13}$ and UPt_3 under pressure or in an applied magnetic field [266, 267, 268, 269].

3.2. Superconductivity coexisting with or on the border of antiferromagnetic order

3.2.1. UM_2Al_3 ($M = \text{Ni}, \text{Pd}$)

Coexistence between superconductivity and antiferromagnetic order was discovered in the heavy-fermion compounds UPd_2Al_3 and UNi_2Al_3 in 1991 [236, 241]. The critical temperatures of $T_c = 2$ K and $T_N = 14$ K for UPd_2Al_3 and $T_c = 1.06$ K and $T_N = 4.6$ K for UNi_2Al_3 are well-separated with $T_c < T_N$ [236, 241]. Each compound forms with the same hexagonal crystal structure described by space group $P6/mmm$. The U-U separations of 4.186 Å and 4.018 Å for UPd_2Al_3 and UNi_2Al_3 , respectively, are well above the Hill limit [270] (~ 3.4 Å), indicating that the 5f electron states from U^{4+} ions do not overlap significantly, and are expected to exhibit a strongly-localized character. However, hybridization with itinerant electron states leads to some amount of itineracy of the 5f electrons, the degree of which is still a matter of debate for these compounds [49]. The splitting of the U^{4+} $J = 4$ multiplet by the CEF has been studied using magnetic susceptibility measurements [271, 272]. Though the splitting energies are different, the energy level schemes are identical for both compounds; each has a Γ_4 singlet ground state with excited states, listed in order of increasing energy, of a Γ_1 singlet, Γ_6 doublet, Γ_5 doublet, Γ_3 singlet, and Γ_5 doublet. The splitting between the ground and first excited states is 33 K for UPd_2Ni_3 and 100 K for UNi_2Al_3 , coinciding with local maxima in the magnetic susceptibility data near 35 K and 100 K, respectively [271, 272].

Commensurate antiferromagnetic order at $T_N = 14$ K (in zero magnetic field) is observed in UPd_2Al_3 , characterized by a wave vector $\vec{Q} = (0, 0, 1/2)$ and an ordered magnetic moment of $0.85 \mu_B/\text{U}$ [273]. The magnetic entropy released at T_N is $S_{mag} = 0.65R \ln 2$ [237]. In applied magnetic fields, several distinct magnetic phases emerge that are discussed in detail in Ref. [49]. In contrast, the more itinerant character of the 5f electron states in UNi_2Al_3 results in an incommensurate SDW order at $T_N = 4.6$ K, characterized by a wave vector $\vec{Q} = (1/2 \pm \delta, 0, 1/2)$ where $\delta = 0.110(3)$ and a small ordered magnetic moment of $0.24(10) \mu_B/\text{U}$ [274, 275]. This subtle phase transition produces no feature in the electrical resistivity [276] and was missed entirely in the first neutron-diffraction study of UNi_2Al_3 [273]. An entropy of $S_{mag} = 0.12R \ln 2$ is released at T_N [241, 277] that is consistent with the smaller ordered magnetic moment in UNi_2Al_3 .

At low temperature, strong electronic correlations lead to enhanced values of the Sommerfeld coefficient. For UPd_2Al_3 , $\gamma = 210$ mJ mol⁻¹ K⁻² is measured in the paramagnetic state and $\gamma = 150$ mJ mol⁻¹ K⁻² is obtained in the temperature range $T_c < T < T_N$ [236]. These values are comparable to $\gamma = 120$ mJ mol⁻¹ K⁻² obtained for UNi_2Al_3 in its normal state [241]. Using a simple single-band model and making other approximations, the enhanced masses of the quasiparticles were estimated to be $m^*/m_0 \sim 66$ for UPd_2Al_3 and ~ 70 for UNi_2Al_3 [236, 241].

Table 3: Summary of properties of heavy-fermion superconductors including: space group of crystal structure; superconducting critical temperature T_c (asterisk indicates superconductivity induced by applied pressure); Néel (T_N), Curie (T_C), quadrupolar ordering (T_Q), or hidden ordering temperature at ambient pressure; Sommerfeld coefficient γ (reported in units of $\text{J mol}^{-1} \text{K}^{-2}$); jump in specific heat at T_c , $\Delta C/\gamma T_c$; type of nodes in the superconducting energy gap; upper critical field values at zero temperature $H_{c2}(0)$ (reported in units of T); and references from which tabulated results were obtained. When $H_{c2}(0)$ values were only available from studies on a polycrystalline sample, the value is denoted with $\dagger$.

Compound	Structure	T_c (K)	T_N, T_C, T_Q (K)	γ	$\Delta C/\gamma T_c$	Nodes	$H_{c2}^{ab}(0)$	$H_{c2}^c(0)$	References
CeCu ₂ Si ₂	<i>I4/mmm</i>	0.6-0.7	0.9	1	1.4	Line	2.05	2.45	[1, 66, 73, 74]
CeCu ₂ Ge ₂	<i>I4/mmm</i>	0.64*	4.15	0.2			2 †		[79, 64, 80]
CePd ₂ Si ₂	<i>I4/mmm</i>	0.43*	10	0.065			0.7	1.3	[57, 58, 83, 84]
CeRh ₂ Si ₂	<i>I4/mmm</i>	0.42*	36, 24	0.023			0.28 †		[82, 85, 86, 65]
CeNi ₂ Ge ₂	<i>I4/mmm</i>	0.3		0.35					[90, 69]
CeIn ₃	<i>Pm3m</i>	0.19*	10.2	0.14		Line	0.45	0.45	[58, 223]
CeCoIn ₅	<i>P4/mmm</i>	2.3		0.25	4.5	Line	11.6	4.95	[96, 133]
CeRhIn ₅	<i>P4/mmm</i>	2.4*	3.8	0.43	4.2		9.7	16.9	[94, 139, 141]
CeIrIn ₅	<i>P4/mmm</i>	0.4		0.75	0.76		1.0	0.5	[97]
CePt ₃ Si	<i>P4mm</i>	0.75	2.2	0.39	0.25	Line	2.7	3.2	[206, 210]
CeIrSi ₃	<i>I4mm</i>	1.65*	5	0.12			9.5	45	[208, 214]
CeRhSi ₃	<i>I4mm</i>	1*	1.6	0.12			7	>30	[207, 213]
CeCoGe ₃	<i>I4mm</i>	0.69*	21, 12, 8	0.032				>30	[212, 209]
CeNiGe ₃	<i>Cmmm</i>	0.43*	5.5	0.045			1.56		[215, 216, 217]
Ce ₂ Ni ₃ Ge ₅	<i>Ibam</i>	0.26*	5.1, 4.5	0.09			0.7		[218, 219, 220]
CePd ₅ Al ₂	<i>I4/mmm</i>	0.57*	3.9, 2.9	0.056				0.25	[222]
U ₆ Fe	<i>I4/mcm</i>	3.8		0.157	2.1		10*		[224, 225, 226]
U ₂ PtC ₂	<i>I4/mmm</i>	1.47		0.15			7.8	9.2	[227, 228, 229]
UBe ₁₃	<i>Fm3c</i>	0.95		1	2.5	Line	14		[52, 230]
UPt ₃	<i>P6₃/mmc</i>	0.53, 0.48	5	0.44	0.55, 0.27	Line, Point	2.1	2.8	[53, 231, 232, 233, 234]
URu ₂ Si ₂	<i>I4/mmm</i>	1.53	17.5	0.07	0.93	Line	3	14	[55, 54, 235]
UPd ₂ Al ₃	<i>P6/mmm</i>	2.0	14	0.21	1.48	Line	3.3	3.9	[236, 237, 238, 239, 240]
UNi ₂ Al ₃	<i>P6/mmm</i>	1.06	4.6	0.12	0.4		0.9	0.35	[241, 242]
UGe ₂	<i>Cmmm</i>	0.8*	52	0.110*	0.2-0.3	Line			[243, 244, 245, 246]
URhGe	<i>Pnma</i>	0.25	9.5	0.164	0.45		2, 1.3	0.55	[247, 248]
UCoGe	<i>Pnma</i>	0.6	2.5	0.057	1	Point	5	0.5	[249, 250, 251, 252, 253]
UIr	<i>P2₁</i>	0.15*	46	0.049					[254, 255]
PrOs ₄ Sb ₁₂	<i>Im3</i>	1.85		0.5	3	Point	2.3		[32, 256, 257, 258]
PrTi ₂ Al ₂₀	<i>Fd3m</i>	0.2, 1.1*	2.0	0.1			>3*		[259, 260, 31]
PrV ₂ Al ₂₀	<i>Fd3m</i>	0.05	0.6	0.09	0.3		0.014		[259, 62]
β -YbAlB ₄	<i>Cmmm</i>	0.08		0.15			0.15	0.025	[63, 261]
PuCoGa ₅	<i>P4/mmm</i>	18.5		0.077	1.4	Line			[107, 262, 263]
PuRhGa ₅	<i>P4/mmm</i>	8.7		0.07	0.65	Line	27	15	[108, 262, 264]
NpPd ₅ Al ₂	<i>I4/mmm</i>	4.9		0.2	2.33	Point	3.7	14	[221]

Superconductivity occurs at $T_c = 2$ K and $T_c = 1.06$ K in UPd_2Al_3 and UNi_2Al_3 , respectively, and corresponding jumps in the specific heat $\Delta C/\gamma T_c$ of 1.48 and 0.4 are observed at their respective T_c 's [236, 237, 241]. The response of superconductivity in these compounds to applied pressure differ. In UPd_2Al_3 , T_c remains nearly unchanged for applied pressures up to 6.5 GPa and is suppressed linearly for $P > 6.5$ GPa with a gradual rate of $dT_c/dP \sim -0.05$ K/GPa [278]. In contrast, the superconducting state of UNi_2Al_3 is suppressed at a relatively rapid rate of $dT_c/dP \sim -0.24(3)$ K/GPa under low applied pressures [279]. The upper critical fields $H_{c2}(T)$ have been measured at ambient pressure in experiments on single crystals with the field applied parallel and perpendicular to the basal plane (parallel to a axis). Zero-temperature values for UPd_2Al_3 were determined to be $H_{c2}^a(0) = 3.3$ T and $H_{c2}^c(0) = 3.9$ T with initial slopes of $(dH_{c2}^a/dT)_{T_c} \simeq -4.6$ T/K and $(dH_{c2}^c/dT)_{T_c} \simeq -5.45$ T/K [238, 242]. These H_{c2} values are close to the Pauli paramagnetic limiting field of $H_{p0} = 3.7$ T and much smaller than values for the orbital critical fields, estimated using the WHH theory [59] to be $H_{c2}^{*,a}(0) = 6.4$ T and $H_{c2}^{*,c}(0) = 7.6$ T. Therefore, the relatively isotropic upper critical fields for UPd_2Al_3 are paramagnetically-limited. This result can be contrasted with the observation of significant anisotropy in $H_{c2}(T)$ for UNi_2Al_3 , which exhibits orbital limiting [242]. The upper critical fields were determined to be $H_{c2}^a(0) \approx 0.9$ T and $H_{c2}^c(0) \approx 0.35$ T with initial slopes of $(dH_{c2}^a/dT)_{T_c} \simeq -1.14$ T/K and $(dH_{c2}^c/dT)_{T_c} \simeq -0.42$ T/K [242]. When these are compared with estimated values for the paramagnetic limiting field, $H_{p0} = 0.18$ T, and the orbital critical fields, $H_{c2}^{*,a}(0) = 0.79$ T and $H_{c2}^{*,c}(0) = 0.29$ T, the $H_{c2}(0)$ values for UNi_2Al_3 suggest that orbital limiting is the dominant pair-breaking mechanism in a magnetic field. Since $H_{p0} < H_{c2}(0) \sim H_{c2}^*(0)$, spin-triplet pairing may be present in UNi_2Al_3 . This possibility was also suggested in an early study of $H_{c2}(T)$ curves on polycrystalline samples [276] and ^{27}Al Knight shift measurements provide additional support for spin-triplet pairing in UNi_2Al_3 [280].

Indirect probes of the superconducting energy gap symmetry for UPd_2Al_3 and UNi_2Al_3 have obtained evidence for the presence of nodes where $\Delta(\vec{k}) = 0$. The observed temperature dependence of the specific heat in the superconducting state of UPd_2Al_3 goes as $C = \gamma T + AT^3$ [237], indicating a residual contribution to C/T at 0 K from ungapped states. This finding is consistent with the presence of point nodes in $\Delta(\vec{k})$, inferred from $C \propto T^3$ behavior [60]). On the other hand, angle-resolved magnetothermal transport measurements support the presence of a line node in $\Delta(\vec{k})$ for UPd_2Al_3 [239]. NMR measurements provide additional support for an anisotropic energy gap containing a line node [240].

Tunneling measurements are extremely challenging to make on heavy-fermion superconductors due to their short superconducting coherence lengths, which require extremely clean sample surfaces to resolve a signal; however, tunneling spectroscopy measurements were successfully performed on epitaxial thin films of UPd_2Al_3 [281]. A strong coupling feature between the charge carriers and an antiferromagnetic spin fluctuation was observed in the tunneling conductivity of UPd_2Al_3

[281]; when this result is considered together with results from neutron-spectroscopy measurements, a compelling argument for spin-fluctuation mediated pairing in UPd_2Al_3 can be made [281].

3.2.2. UPt_3

The compound UPt_3 is isostructural with the non-superconducting heavy-fermion compound CeAl_3 [9], forming with the hexagonal space group $P6_3/mmc$. While searching for evidence of strong spin fluctuations, bulk superconductivity was observed in UPt_3 in 1984 at $T_c = 0.54$ K [53]. With a measured γ value of 420-450 mJ mol $^{-1}$ K $^{-2}$ in the normal state [282, 53, 233], UPt_3 was quickly compared to the other known heavy-fermion superconductors at the time (UBe_{13} and CeCu_2Si_2). Effective quasiparticle masses of $m^*/m_0 = 187$ and 240 were estimated from analysis of the upper critical fields [283] and far infrared absorptivity [284], respectively, while analysis of quantum oscillation studies obtained effective masses as high as $m^*/m_0 = 120$ [285, 286]. These enhanced effective quasiparticle masses firmly classify UPt_3 as a heavy-fermion superconductor.

In its normal state, the magnetic susceptibility of UPt_3 is anisotropic, exhibiting Curie-Weiss behavior at high temperatures [282] that is also observed in NMR measurements [287]. Studies conducted using numerous probes were initially unable to detect any evidence for magnetic order in UPt_3 ; however, measurements of μSR [231] and neutron scattering were eventually able to resolve evidence for commensurate antiferromagnetic order with a small ordered magnetic moment of 0.02 μ_B/U [232]. The apparent absence of a feature near $T_N = 5$ K in ^{195}Pt NMR [287] and specific heat [53, 233] measurements has led some to suggest that magnetic order in UPt_3 is relatively dynamic.

Evidence for multiple *intrinsic* superconducting phases in UPt_3 , separated by 50-60 mK, was observed in high-resolution specific heat measurements [233, 288]. Considering the results from numerous studies, Joynt and Taillefer state that the two transitions in UPt_3 occur at $T_c^+ = 0.53$ K with specific heat jump $\Delta C/\gamma T_c^+ \simeq 0.55$ and $T_c^- = 0.48$ K with jump $\Delta C/\gamma T_c^- \simeq 0.27$ [289]. Fisher *et al.* noted that they could obtain roughly universal values $\Delta C/\gamma T_c \simeq 1$ if they normalized the specific-heat jump by the fraction of electrons contributing to the superconducting energy gap $f_s = (\gamma - \gamma_0)/\gamma$ where $\gamma_0 \sim 56$ -265 mJ mol $^{-1}$ K $^{-2}$ (depending on the sample) is a residual electronic contribution to specific heat at 0 K [233]. Studies of the specific heat under applied magnetic field demonstrated that there are actually three distinct superconducting phases in UPt_3 , denoted A, B, and C (see the $H - T$ phase diagram in Fig. 9) [288].

Early studies on UPt_3 , prior to the discovery of distinct superconducting phases, observed significant anisotropy in the upper critical fields $H_{c2}(T)$ [283]. In experiments performed as low as 150 mK, the measured $H_{c2}(0)$ values exceeded the Pauli paramagnetic limiting field, estimated to be $H_{p0} \simeq 0.957$ T, by a factor of nearly 2 and the presence of spin-orbit scattering (not accounted for in the formula $H_{p0} \simeq 1.84T_c$ [71]) was invoked as the explanation [283]. However, using the measured value of $(dH_{c2}/dT)_{T_c} \simeq -6.3$ T/K and T_c , an orbital upper critical

Figure 9: (Color online) The magnetic field-temperature ($H-T$) phase diagram for UPt_3 for $H \parallel c$ is displayed. Three distinct superconducting phases, denoted A, B, and C, are depicted. The theoretical superconducting energy gap symmetry for each phase is shown schematically for the E_{2u} theoretical model, and the surrounding frames define the hexagonal crystal symmetry of UPt_3 . The presence of nodes in the gaps is evident, and is most easily seen in the cut-away schematic of the gap for phase B where the gap intersects the internal sphere representing the Fermi surface (after Ref. [234]).

field of $H_{c2}^*(0) = 2.27$ T is estimated [283], which is not dissimilar to $H_{c2}(0)$ values. Measurements of $H_{c2}(T)$ for UPt_3 to lower temperatures demonstrated that the anisotropy, characterized by $H_{c2}^{\parallel}(T) > H_{c2}^{\perp}(T)$ near T_c (where $\parallel$ and $\perp$ are relative to the crystallographic c axis), reverses below ~ 0.2 K so that $H_{c2}^{\parallel}(0) < H_{c2}^{\perp}(0)$ [290]. With the discovery of multiple superconducting phases in UPt_3 [233, 288], it was realized that each phase has its own characteristic upper critical fields. Therefore, the measured zero-temperature upper critical fields $H_{c2}(0)$ are associated with the C phase, while $H_{c2}(T \approx T_c^+)$ values are characteristic of the A phase [289]. The observed anisotropy of $H_{c2}(T)$ in UPt_3 is related to anisotropic mass enhancements of the quasiparticles as confirmed in quantum oscillation studies [286].

Measurements of the specific heat of UPt_3 under applied pressure demonstrated that the zero-magnetic field superconducting phases (A and B) are suppressed at different rates ($dT_c^+/dP \approx -0.24(5)$ K/GPa and $dT_c^-/dP \approx -0.05(1)$ K/GPa) with the two transitions merging at approximately 0.37 GPa and 419 mK [266]. The ordered magnetic moment from U ions is suppressed by applying pressure, as determined in neutron scattering experiments, vanishing near 0.3-0.4 GPa at 1.8 K [291]. This apparent correlation between the suppression of antiferromagnetic order and the emergence of a single superconducting

state strongly suggests that the subtle and dynamic antiferromagnetic order in UPt_3 plays a role in the emergence of the distinct superconducting states.

The coexistence of spin fluctuations and superconductivity and the upper critical field results, namely $H_{c2}(0) > H_{p0}$, both motivated early discussions of a possible p -wave order-parameter symmetry for UPt_3 [53, 283]. It has also been claimed that the strong sensitivity of the superconducting properties to annealing and other sample synthesis conditions is consistent with this possibility [53, 292]. Nodes in the superconducting energy gap are suggested by the observation of a contribution to the specific heat in the superconducting state with linear temperature dependence (*i.e.*, C/T is non-zero as $T \rightarrow 0$ K) and relatively small $\Delta C/\gamma T_c$ jumps in the specific heat at T_c^+ and T_c^- [233, 292]; both observations are consistent with ungapped electron states. The distinct nodal structures of the three superconducting phases of UPt_3 , proposed based on a study of the flux lattice using neutron scattering measurements, are depicted in Fig. 9 from Ref. [234]. The superconducting order parameter of UPt_3 has been discussed in detail in Refs. [293, 289], but it remains a subject of continued experimental interest and attention. Recently, a complex order parameter for UPt_3 was observed through angle-resolved measurements of the critical currents in Josephson tunnel-junction experiments; the results were consistent with an E_{2u} order-parameter symmetry with an odd-parity triplet representation [294]. More recently, the polar Kerr effect was observed only in the B phase of UPt_3 ($T < T_c^-$ and $H = 0$ T), providing evidence for a complex-two component order parameter and time-reversal symmetry breaking within the B phase [295].

3.2.3. URu_2Si_2

The compound URu_2Si_2 is one of the most intriguing and enigmatic heavy-fermion superconductors known. This compound has the tetragonal ThCr_2Si_2 structure, which is shared by many Ce-based heavy-fermion superconductors and a class of Fe pnictide and chalcogenide high-temperature superconductors with the formula MFe_2X_2 , where M is an alkali metal, alkaline earth, or lanthanide, and X is a pnictogen or chalcogen.

At ambient pressure, URu_2Si_2 exhibits two ordered phases: a so-called “hidden order” (HO) phase below $T_o = 17.5$ K and a superconducting phase below $T_c = 1.5$ K, which coexist with one another [54, 55, 56]. The terminology “hidden order” refers to the fact that the identity of the order parameter (OP) of the HO phase has eluded researchers for nearly three decades. Based on an analysis of the mean-field like anomaly in the specific heat of URu_2Si_2 , two of the authors and their coworkers [55] proposed a partial gapping scenario in which the HO phase, conjectured to be a charge or spin density wave (CDW or SDW), forms a gap of ~ 130 K over $\sim 40\%$ of the Fermi surface, while the remainder of the Fermi surface is gapped by the superconductivity that occurs at lower temperature. Energy gaps with comparable values have been extracted from various physical properties including, for example, electrical resistivity [296], optical conductivity spectra [297], and scanning tunneling microscopy [298, 299]. Neutron scattering experiments on URu_2Si_2 single crystal specimens revealed that

the U ions exhibit antiferromagnetic order in the HO phase in which the U magnetic moments are aligned along the c -axis direction and have magnitudes of only $0.03 \mu_B/U$ [300, 301]. However, the reduction in entropy associated with the HO transition is $\sim 0.2R \ln 2$ [55] is much larger than that which would be expected for the ordering of such small U magnetic moments (hence the terminology “hidden order”). An extensive review of the hidden order, superconductivity, magnetism and other aspects of URu_2Si_2 can be found in a recent review article by Mydosh and Oppeneer [302].

The delicate interplay of competing interactions in URu_2Si_2 can be “tuned” by varying control parameters such as pressure, magnetic field, and composition of elemental substituents, yielding a variety of correlated electron ground states. Upon the application of pressure, URu_2Si_2 undergoes a first order transition [303] from the HO phase to a large moment antiferromagnetic (LMAFM) phase at a critical pressure P_c , reported by various groups to lie in the range (0.5 - 1.5 GPa) [304]. The magnetic structure of the LMAFM phase, in which the magnetic moment is $\sim 0.4 \mu_B/U$, is identical to the magnetic structure of the HO phase [305, 302]. It is widely believed that the small moment antiferromagnetic (SMAFM) order in the HO phase is extrinsic and associated with a small volume fraction of the LMAFM phase that is produced by local strains that increase the c/a ratio over a critical value [306]. However, some researchers believe that the SMAFM order in the HO phase is intrinsic, since the onset of the SMAFM occurs at T_o and it is observed in samples with different residual resistivity values [307].

The application of a large magnetic field H results in a suppression of the HO phase at $H \approx 35$ T and the emergence of several novel quantum phases that exhibit non-Fermi liquid behavior [308]. The substitution of transition elements for Ru from neighboring columns in the periodic table have been found to suppress the HO and to generate other magnetic phases [309, 310, 311, 312], while substitution of elements from the same column of the periodic table have been found to enhance the HO [311, 313, 314]. The substitution of Rh generates LMAFM phases [312], while the substitution of Mn, Tc and Re induces an itinerant heavy electron ferromagnetic phase [309, 310]. Non-Fermi liquid characteristics in the physical properties that persist deep into the ferromagnetic state in the $URu_{2-x}Re_xSi_2$ system have been reported [315, 316]. The substitution of Fe and Os for Ru produces a large two-fold enhancement of the HO/LMAFM phase boundary with a “kink” at a critical substituent concentration that is apparently associated with a transition from the HO to the LMAFM phase [313, 314]. It has been suggested that the enhancement of the HO/LMAFM phase boundary for Fe substitution is driven by “chemical pressure” generated by substitution of smaller Fe ions for Ru ions [313]; additional evidence supporting this interpretation was presented in a recent study of specific heat and neutron diffraction measurements on $URu_{2-x}Fe_xSi_2$ single crystals [317]. However, this argument cannot explain the enhancement of the HO/LMAFM phase boundary upon substitution of larger Os ions for Ru ions [311, 314].

URu_2Si_2 exhibits a type of unconventional d -wave spin-

Figure 10: (Color online) Schematic of the Fermi surface (opaque) and superconducting energy gap structure (transparent) of URu_2Si_2 after Ref. [328].

singlet multiband superconductivity with two distinct superconducting energy gaps. The jump ΔC in the specific heat at T_c decreases rapidly with pressure and is no longer detectable at pressures within the HO phase [318, 319, 320]. Insofar as this can be interpreted as a measure of bulk superconductivity, it indicates that bulk superconductivity only occurs within the HO phase and not in the LMAFM phase. In contrast, the resistive superconducting transitions extend well into the LMAFM phase, indicating that either filamentary superconductivity or superconducting fluctuations extend into the LMAFM phase [321].

Measurements of the specific heat in the superconducting state at low temperatures reveal a T^2 dependence that is consistent with line nodes in the energy gap [318, 292]. The ^{29}Si NMR relaxation rate, T_1 , varies as T^3 in the superconducting state at low temperature, which is also consistent with line nodes [322, 323]. Point-contact spectroscopy measurements on a URu_2Si_2 single crystal yield a superconducting energy gap that is not consistent with BCS behavior and evidence for a pseudogap between $T_c = 1.37$ K and 2 K [324]. Quantum oscillation [325, 326, 327], electronic transport [328], specific heat [329], and thermal conductivity [328] measurements indicate that URu_2Si_2 is a multiband superconductor containing a light spherical hole band and an anisotropic heavy electron band. Angle-resolved thermal conductivity and specific heat measurements have suggested two distinct superconducting gap structures having different nodal topology with horizontal line nodes in the hole band and point nodes in the electron band (see Fig. 10) [328, 329, 330, 331]. From a symmetry group analysis, a chiral d -wave state that breaks time-reversal symmetry has been proposed [328]. Evidence for time-reversal-symmetry-breaking has recently been reported by Schemm *et al.* [332]. There have been several studies of flux line lattice melting phenomena in URu_2Si_2 polycrystals [333] and single crystals [334].

3.3. Interplay of Ferromagnetic Order and Superconductivity

There are four U-based heavy-fermion compounds in which the interplay between ferromagnetism and superconductivity

plays a significant role: UGe₂ [245], URhGe [247], UCoGe [249], and UIr [254, 255]. The properties of these four heavy-fermion superconductors are reviewed in this special issue of Physica C in the article on ferromagnetic superconductors by Andrew Huxley. Furthermore, the compound UIr crystallizes with a noncentrosymmetric crystal structure, so its properties are also covered in this special issue's article on noncentrosymmetric superconductors by F. Kneidinger *et al.*. However, in addition to providing some pertinent information concerning the superconducting and normal-state properties of these compounds in Table 3, we would like to touch briefly on the compounds UGe₂ and UCoGe below.

3.3.1. UGe₂

Ferromagnetic order with an ordered magnetic moment of $1.48 \mu_B/\text{U}$ develops parallel to the short orthorhombic a axis in UGe₂ below $T_C = 52$ K [243]. The effective magnetic moment, obtained from Curie-Weiss analysis of magnetic susceptibility data, was determined to be $2.7 \mu_B/\text{U}$ [243]; this value is smaller than the saturation magnetic moment, which is consistent with itinerant U $5f$ electron states in UGe₂ [49]. Analysis of specific heat data at low temperature reveals that $\gamma \approx 32$ mJ mol⁻¹ K⁻², suggesting modestly-enhanced quasiparticle masses in UGe₂ [244]. A subtle feature is observed in $\rho(T)$ data at $T_x \approx 25$ K [335], below which, the ferromagnetic magnetic moment increases, suggesting that there are actually two distinct ferromagnetic phases in UGe₂ [336]. Under applied hydrostatic pressure, both T_C and T_x are suppressed monotonically. The ferromagnetic phase transition below T_C becomes first order above ~ 1.2 GPa [244] and T_C extrapolates to 0 K near 1.6 GPa [245, 244, 337]. The abrupt, first-order decrease of $T_C(P)$ at the critical pressure is especially dramatic in measurements on polycrystalline samples [338]. The other temperature scale, T_x , is expected to vanish near 1.2 GPa; however, the suppression is veiled by the emergence of a dome of superconductivity extending from near 1 GPa to 1.6 GPa with maximum $T_c = 0.8$ K at ~ 1.2 GPa [245, 244, 337]. Near 1.2 GPa, $\gamma \approx 110$ mJ mol⁻¹ K⁻² [246], indicating a strong enhancement of the quasiparticle masses relative to the ambient-pressure result. An enhancement of $\gamma(P)$ was observed in the pressure range where superconductivity emerges in polycrystalline samples [339]. The jump at T_c in specific heat data, $\Delta C/\gamma T_c \approx 0.2$ - 0.3 , observed under an applied pressure of 1.13 GPa, is small but consistent with bulk superconductivity [246].

The superconducting state of UGe₂ resides completely within the ferromagnetic phase, with each vanishing under an applied pressure of 1.6 GPa [245, 244, 337]. This observation strongly suggests that ferromagnetic order and superconductivity do not merely coexist, but that the mechanism underlying the emergence of superconductivity in UGe₂ depends upon the presence of ferromagnetic order. Attempts to elucidate the nature of the electron pairing in UGe₂ have led to odd-parity equal-spin triplet pairing as the most promising candidate [49]. However, studies on polycrystalline samples of UGe₂ with ρ_0 values at least an order of magnitude higher than those in single crystalline samples were able to resolve a pressure-temperature phase diagram [338] that is similar to

that in Refs. [245, 244, 337] (constructed from measurements on single crystals) and includes robust, bulk superconductivity as evidenced by jumps in specific heat at T_c [339]. These results may be inconsistent with a p -wave pairing symmetry for superconductivity in UGe₂, which should be extremely sensitive to disorder, especially when the mean free path approaches the coherence length. The small jump $\Delta C/\gamma T_c$ in specific heat at T_c and a residual value of C/T as $T \rightarrow 0$ K suggest that there are nodes in the superconducting energy gap of UGe₂ [246]; more specifically, line nodes are suggested [60] by the linear temperature dependence of C/T in the superconducting state.

3.3.2. UCoGe

Unlike UGe₂ [245] and URhGe [247], for which superconductivity resides deep within ferromagnetically-ordered states with large ordered moments, superconductivity in UCoGe coexists with a weak itinerant ferromagnetic order. In polycrystalline samples of UCoGe and at ambient pressure, ferromagnetic order is observed below $T_C = 3$ K with an ordered magnetic moment of $0.03 \mu_B/\text{U}$ (polarized along the c axis [250]) with superconductivity being observed near $T_c = 0.8$ K [249]. An effective magnetic moment from Curie-Weiss behavior analysis of $1.7 \mu_B/\text{U}$ is much larger than the ordered moment and the magnetic entropy released at T_C ($S_{\text{mag}} \approx 0.03R \ln 2$) is small; both results are consistent with weak itinerant ferromagnetic order [249]. μSR measurements demonstrate that this weak ferromagnetism coexists with superconductivity on a microscopic scale [340]. In measurements of specific heat, a Sommerfeld coefficient $\gamma = 57$ mJ mol⁻¹ K⁻² is obtained, suggesting that the effective quasiparticle masses are moderately-enhanced, and a jump at T_c , $\Delta C/\gamma T_c \approx 1$, indicates that superconductivity in UCoGe is bulk [249]. The physical properties of UCoGe are strongly sample-dependent [249] and high-quality single crystals tend to have transition temperatures $T_C = 2.5$ K and $T_c = 0.5$ - 0.6 K [251, 253, 252].

Significant anisotropy was observed in the upper critical field curves measured on single-crystalline samples of UCoGe [250]. The results include: large value of $H_{c2}(0) \approx 5$ T for $H\|a, b$; large anisotropy, $H_{c2}^a(0) \approx H_{c2}^b(0) \gg H_{c2}^c(0)$, of a factor ~ 10 ; a pronounced upturn of $H_{c2}(T)$ with decreasing temperature along all three principle axes [250]. The upper critical fields $H_{c2}(T)$ along $H\|a, b$ significantly exceed the Pauli paramagnetic limit. The anisotropy and values of $H_{c2}(0)$ provide evidence for spin-triplet pairing and a superconducting gap with axial symmetry and point nodes along the c axis [250]. Neutron scattering measurements also suggest nodes are present in the superconducting energy gap along the c axis [341]. Angle-resolved NMR measurements on UCoGe demonstrate that magnetic fields applied along the c -axis strongly suppress critical ferromagnetic spin fluctuations [342, 253], and this suppression is believed to be intimately coupled to the unusual anisotropic behavior of $H_{c2}(T)$ in UCoGe [253]. Furthermore, it has been suggested that the critical ferromagnetic spin fluctuations with Ising anisotropy may mediate spin-triplet superconductivity in UCoGe [253].

Under applied pressure, T_C is suppressed at a rate of -1.4 K/GPa, while T_c is relatively unaffected up to 2.4 GPa

as it traces out a superconducting dome with weak curvature [343, 251]. In studies on a single crystal, ferromagnetic order is completely suppressed near 1.4 GPa, and unlike in the other ferromagnetic superconductors, superconductivity in UCoGe persists into the paramagnetic state at pressures above 1.4 GPa [251]. From symmetry considerations, it is expected that the superconductivity in the paramagnetic state is distinct from the superconducting state that coexists with weak itinerant ferromagnetism below 1.4 GPa [251]. The spectacular enhancement of the $H_{c2}(T)$ curves under applied pressure is certainly consistent with such a scenario [251]. Spin-triplet pairing and the presence of a ferromagnetic quantum critical point near 1.4 GPa are strongly implied by these results. It may also be possible to access such a quantum critical point via chemical substitution as has been reported near $x = 0.22$ in the alloy system $\text{UCo}_{1-x}\text{Fe}_x\text{Ge}$ [344].

3.4. U_6T , U_2PtC_2 , and UBe_{13}

As we did in Section 2, we conclude our discussion of U-based heavy-fermion superconductors with three examples that do not fall neatly into the categories of residing near or coexisting with antiferromagnetic or ferromagnetic order. The first is a family of isostructural compounds U_6T ($\text{T} = \text{Mn, Fe, Co, Ni}$), the second is the compound U_2PtC_2 , and the third is the compound UBe_{13} .

The compounds U_6T ($\text{T} = \text{Mn, Fe, Co, Ni}$) are among the earliest superconducting compounds comprised of magnetic $3d$ transition metals to be discovered [265]. Hill and Matthias [345] observed that the dependence of the T_c of pseudobinary $\text{U}_6\text{T}_{1-x}\text{T}'_x$ alloys on the d -element valence electron count is strikingly similar to the ‘‘Slater-Pauling’’ curve that describes the variation of the saturation magnetic moment with electron density for $\text{T}_{1-x}\text{T}'_x$ transition-metal alloys. This led them to speculate that a ‘‘magnetic mechanism’’ was responsible for the superconductivity of the U_6T compounds [345]. This intriguing suggestion foreshadowed the current interpretation concerning the pairing mechanism of many unconventional superconductors. Subsequent measurements of the specific heat, magnetic susceptibility, and the upper critical magnetic field [225, 224], revealed that U_6Fe and U_6Co are moderately heavy Fermi-liquid systems with electronic effective masses $m^*/m_0 \approx 20$. These properties have led many to compare U_6Fe with UPt_3 and UBe_{13} and count it among the heavy-fermion superconductors [346]; however, this interpretation is not universally accepted, and many consider U_6Fe ($T_c \approx 3.8$ K) and the Pu- and Np-based superconductors (see Section 4.3) to constitute links between heavy-fermion superconductors and other unconventional superconductors such as the cuprates.

Superconductivity was reported in the compound U_2PtC_2 with $T_c = 1.47$ K by Matthias *et al.* [227]. Subsequent studies demonstrated that there is no magnetic order in U_2PtC_2 [228, 229]; though, evidence for strong ferromagnetic fluctuations has been obtained in the superconducting state from measurements of a modified Korringa law in the spin-lattice relaxation rate $1/T_1$ [229]. The properties of U_2PtC_2 have been used to place it in an intermediate position between U_6Fe and the unambiguous heavy-fermion compounds UPt_3 and UBe_{13} [228].

Figure 11: Upper critical field curve for UBe_{13} , $H_{c2}(T)$, after Ref. [347].

Specific heat measurements confirm bulk superconductivity by observing a jump at T_c [228, 348] and provide a Sommerfeld coefficient of $\gamma = 75$ mJ mol- U^{-1} K $^{-2}$ [228]. This value of γ , which is consistent with moderately-enhanced quasiparticle mass, has been used to demonstrate a possible correlation between γ and the U-U separation for U-based superconducting compounds [228]. With increasing pressure, the electrical resistivity in the normal state just above T_c decreases, and T_c is suppressed linearly at a rate of $dT_c/dP \approx -0.53$ K/GPa [349]. Early measurements of the upper critical fields on polycrystalline samples found a large initial slope of $(dH_{c2}/dT)_{T_c} \approx -9$ T/K [228]. More recent measurements of $H_{c2}(T)$ indicate that $H_{c2}^c(0) \approx 7.8$ T and $H_{c2}^{ab}(0) \approx 9.2$ T [229]; these values significantly exceed the estimated Pauli limiting field of $H_{p0} \approx 2.7$ T, but are comparable to the orbital upper critical field $H_{c2}^*(0) \approx 10.2$ T [229], estimated using the WHH theory [59].

When $H_{c2}(0) \gg H_{p0}$ as it is in U_2PtC_2 [229], the possibility of spin-triplet pairing can be considered. NMR measurements of the ^{195}Pt nucleus in U_2PtC_2 samples observe a temperature-independent Knight shift, which is consistent with spin-triplet pairing [229]. Furthermore, $1/T_1$ data follow a T^2 temperature dependence in the superconducting state, which is consistent with nodes in the energy gap. On the other hand, strong spin orbit scattering can also increase the paramagnetic limiting field and reduce the Knight shift of a spin-singlet superconductor. Moreover, a recent study of the system $\text{U}_2\text{Rh}_{1-x}\text{Pt}_x\text{C}_2$ (the compound U_2RhC_2 is an itinerant antiferromagnet with $T_N \approx 22$ K) provides results that are difficult to reconcile with unconventional superconductivity in U_2PtC_2 [348]. Chemical substitution of Pt with Rh suppresses T_c , but not as rapidly as expected for a superconductor with spin-triplet pairing, which should be

extremely sensitive to the presence of nonmagnetic impurities [348]. Superconductivity is surprisingly robust, persisting from $x = 1$ to $x = 0.9$ (10% Rh), where the estimated mean free path is comparable to the estimated superconducting coherence length (*i.e.*, $l \approx \xi$) [348]. In such cases, superconductivity is predicted to be completely suppressed, but T_c is only reduced from 1.45 K at $x = 1$ to 1.09 K at $x = 0.9$ [348]. This insensitivity of T_c to impurities is hard to understand in the context of any non-*s*-wave type pairing [348], and suggests that additional research must be conducted on U_2PtC_2 to characterize its superconducting state.

The properties of the heavy-fermion compound UBe_{13} are quite extraordinary and bear some similarities with those of CeCu_2Si_2 . A particularly noteworthy example is the Sommerfeld coefficient $\gamma = C(T)/T$, which increases with decreasing temperature and reaches an enormous value of $\sim 1 \text{ J mol}^{-1} \text{ K}^{-2}$ just above $T_c \approx 0.9 \text{ K}$, below which UBe_{13} is superconducting. The specific heat jump ΔC at T_c is of the order of γT_c , which demonstrates that the heavy quasiparticles responsible for the large value of γ in the normal state are also involved in the superconductivity. The magnetic susceptibility has a Curie-Weiss-like temperature dependence at high temperatures, but approaches a constant value $\chi(0)$ as $T \rightarrow 0 \text{ K}$, indicative of a nonmagnetic ground state. Moreover, the value of $\chi(0)$ is consistent with the large value of γ ; *i.e.*, the Wilson-Sommerfeld ratio is of order unity. Magnetic penetration depth measurements on UBe_{13} yield a T^2 temperature dependence at low temperature, consistent with an axial state with point nodes in the energy gap [350]. In contrast, NMR measurements [351] reveal relaxation rates that are proportional to T^3 at low temperatures, indicative of a polar state with line nodes. However, NMR measurements yield T^3 behavior for nearly all other heavy-fermion superconductors, as noted by Heffner and Norman [267]. The upper critical field curve $H_{c2}(T)$ of UBe_{13} , shown in Fig. 11, has a very unusual shape. The value of the initial slope $(dH_{c2}/dT)_{T_c} \approx -42 \text{ T/K}$, is enormous and consistent with the large quasiparticle effective mass $m^*/m_0 \approx 300$ [347]. The $H_{c2}(T)$ curve rolls over and then exhibits another linear region below 0.7 K, with a smaller slope of $dH_{c2}/dT \approx -9.1 \text{ T/K}$, that persists to very low temperatures of the order of 50 mK [347].

Chemical substitution of Th for U in UBe_{13} yields a striking $T - x$ phase diagram, based on specific heat and other measurements, some of which reveal a region with multiple phase transitions; these phases consist of at least two superconducting regions, which appear to correspond to different types of superconductivity [267]. Additional evidence for the existence of two distinct types of superconductivity, presumably with different order parameter symmetries, are provided by measurements of T_c under pressure on samples of $\text{U}_{1-x}\text{Th}_x\text{Be}_{13}$ (see Fig. 12(a)) [268] and measurements of $H_{c2}(T)$ for Gd-substituted samples of $\text{U}_{1-x}\text{Th}_x\text{Be}_{13}$ with different values of x [352] in these two superconducting regions. The properties of this remarkable heavy-fermion superconductor are summarized in several reviews to which the reader is referred for further information [267, 269].

Figure 12: (Color online) (a) Superconducting critical temperature T_c for $\text{U}_{1-x}\text{Th}_x\text{Be}_{13}$ as a function of x for several applied pressures (explicitly labeled in units of kbar). Lines are guides to the eye. (b) T_c for $\text{U}_{1-x}\text{M}_x\text{Be}_{13}$ ($M = \text{La}, \text{Lu}, \text{Th}$) at ambient pressure from measurements of ac magnetic susceptibility. The data for $M = \text{Th}$ (filled triangles and crosses) are from two independent studies. Plus symbols represent a feature in measurements of specific heat for $M = \text{Th}$ samples that indicates a second phase transition within the superconducting state. Adapted from Ref. [268].

4. Pr-, Yb-, Pu-, and Np-based heavy-fermion superconductors

4.1. Pr-based compounds

Compared with Ce-, U-, and Yb-based compounds, not many Pr-based heavy-fermion compounds are currently known. A brief description of the necessary materials design it required to discover the first Pr-based heavy-fermion compound, PrInAg_2 [30], is provided in Ref. [353]. The main impediment to the formation of a heavy-fermion ground state in Pr-based compounds is that Pr is a non-Kramer's ion and, for most point symmetries, the singlet ground state that is observed does not supply the necessary degeneracy. A Γ_3 doublet ground state is observed in a few Pr-based heavy-fermion compounds and only occurs when Pr occupies a crystallographic position with cubic point group symmetry. Interestingly, Γ_3 is nonmagnetic, so the heavy-fermion states in these compounds must have a nonmagnetic origin. It is the localized electric quadrupolar moments, associated with the Γ_3 doublet ground state, that play a role analogous to the localized magnetic moments in conventional heavy-fermion compounds, and they can form a Kondo lattice through the two-channel or quadrupolar Kondo effect [27, 28, 29]. Therefore, it is the interplay between quadrupolar degrees of freedom and superconductivity that is typically of interest in Pr-based heavy-fermion superconductors.

4.1.1. $\text{PrOs}_4\text{Sb}_{12}$ and $\text{PrPt}_4\text{Ge}_{12}$

The compound $\text{PrOs}_4\text{Sb}_{12}$ is the first Pr-based heavy-fermion superconductor reported and one of the most notable filled skutterudite compounds. This compound has a large electronic specific heat coefficient γ of $\sim 500 \text{ mJ mol}^{-1} \text{ K}^{-2}$ [32, 354]. The specific heat jump at the superconducting critical temperature

T_c shows an unusual double peak feature, which has been observed in numerous studies [354, 258, 355]. The ground state of Pr in the CEF is a singlet, which is separated from a low lying triplet first excited state by only ~ 7 K [356, 357, 358]. Various types of measurements in high magnetic fields probing the normal state properties have revealed the existence of a high-field ordered phase (see Fig. 13) [359, 360, 361, 362], which was determined by means of neutron diffraction experiments in high magnetic fields to be an antiferroquadrupolar ordered phase [363]. Since $\text{PrOs}_4\text{Sb}_{12}$ has a nonmagnetic ground state, it has been conjectured that the superconducting electron pairing may be mediated by quadrupolar fluctuations [357]. Experiments that probe the superconducting energy gap have provided evidence for both nodal and nodeless energy gaps in $\text{PrOs}_4\text{Sb}_{12}$. Transverse muon spin rotation (TF- μSR) experiments yielded a temperature dependence of the penetration depth λ for $\text{PrOs}_4\text{Sb}_{12}$ that is consistent with an isotropic energy gap [364]. However, scanning tunneling microscopy measurements observed a gap that was open in large regions, discounting the possibility of line nodes [365], zero-field microwave penetration depth measurements revealed behavior best described with point nodes in the superconducting energy gap [256], and small-angle neutron scattering experiments reported distortions in the flux-line lattice that were attributed to gap nodes [366]. Thermal transport measurements on single crystals carried out as a function of magnetic field direction revealed two different superconducting phases. The energy gap has four or more point nodes at high fields (A phase), while it has two point nodes at the low fields (B phase) [257]. More recent studies also suggest that $\text{PrOs}_4\text{Sb}_{12}$ is a multiband superconductor [367, 368, 369, 370]. Muon-spin relaxation measurements on $\text{PrOs}_4\text{Sb}_{12}$ provide evidence for time-reversal symmetry breaking [371]. The magnetic field H vs temperature T phase diagram of $\text{PrOs}_4\text{Sb}_{12}$ is shown in Fig. 13.

A new class of filled skutterudites of the form $\text{RPt}_4\text{Ge}_{12}$ has recently been synthesized [372, 373], opening up an entirely new direction for filled skutterudite research. Several members of this new class exhibit superconductivity (R = Sr, Ba, Th, La, Pr) where the R = Pr member has one of the highest values of T_c of ~ 7.9 K [373]. Recent investigations have suggested that $\text{PrPt}_4\text{Ge}_{12}$ exhibits a type of strongly-coupled unconventional superconductivity that has point nodes in the energy gap [374] and breaks time-reversal symmetry [375]. More recent studies suggest that $\text{PrPt}_4\text{Ge}_{12}$ is a multiband superconductor [376, 377, 378]. It was also recently demonstrated that introducing magnetic Ce impurities through chemical substitution for Pr either rapidly suppresses one of the energy gaps or induces a crossover from a nodal to nodeless gap symmetry [379]. It is interesting that both $\text{PrPt}_4\text{Ge}_{12}$ and $\text{PrOs}_4\text{Sb}_{12}$ exhibit similar types of multiband unconventional superconductivity, but display striking differences in electronic structure. The CEF splitting δ between the Pr ground state singlet and triplet first excited state in the two compounds differs by an order of magnitude; $\delta \approx 7$ K for $\text{PrOs}_4\text{Sb}_{12}$ [356, 357] and $\delta \approx 130$ K for $\text{PrPt}_4\text{Ge}_{12}$ [373, 374, 380]. The electronic correlations are rather strong in $\text{PrOs}_4\text{Sb}_{12}$ as evinced by the large electronic specific heat coefficient $\gamma \sim 500 \text{ mJ mol}^{-1} \text{ K}^{-2}$, whereas they

Figure 13: Magnetic field vs. temperature (H - T) phase diagram for $\text{PrOs}_4\text{Sb}_{12}$ showing the high-field ordered phase, designated HFOP in the figure, which has been identified with antiferroquadrupolar order [363], and the superconducting phase (after Refs. [361, 356]).

are considerably weaker in $\text{PrPt}_4\text{Ge}_{12}$ as reflected in the much smaller value of $\gamma \sim 60 \text{ mJ mol}^{-1} \text{ K}^{-2}$ [373].

4.1.2. Superconductivity in $\text{PrT}_2\text{X}_{20}$ compounds

Interest has been steadily growing in members of the RT_2X_{20} (R = rare earth; T = transition metal; X = Al, Zn, Cd) family of compounds that adopt the $\text{CeCr}_2\text{Al}_{20}$ -type crystal structure characterized by space group $Fd\bar{3}m$. Superconductivity was first observed in 2010 among the “1-2-20” compounds, including at $T_c \approx 0.05$ K in $\text{PrIr}_2\text{Zn}_{20}$ [381]. Measurements of the specific heat of $\text{PrIr}_2\text{Zn}_{20}$ at low temperature reveal a $C/T \approx \gamma$ value of $\sim 5 \text{ J mol}^{-1} \text{ K}^{-2}$ at 0.4 K [381, 382], which was interpreted as evidence for heavy-fermion superconductivity in this compound. $\text{PrIr}_2\text{Zn}_{20}$ exhibits Curie-Weiss behavior for $T > 30$ K in magnetic susceptibility $\chi(T)$ measurements with $\mu_{\text{eff}} \approx 3.49(2) \mu_B/\text{Pr}$ (associated with paramagnetic Pr^{3+} ions) [381, 382]; however, analysis of $\chi(T)$ data at low temperature and of a Schottky anomaly in specific heat data provided compelling evidence that is consistent with a Γ_3 nonmagnetic Kramers doublet ground state in $\text{PrIr}_2\text{Zn}_{20}$ [382]. Inelastic neutron scattering measurements later confirmed this hypothesis, obtaining a Γ_3 (Γ_4) ground state (first excited state) split by ~ 30 K [383]. The measured crystal-field excitations are very clear, indicating there are well-localized $4f$ electron states that have not been broadened by correlation effects as typically occurs in Kondo systems [383]. This observation suggests that any heavy-fermion behavior in $\text{PrIr}_2\text{Zn}_{20}$ must originate from

nonmagnetic degrees of freedom. The Γ_3 ground state carries nonmagnetic quadrupolar degrees of freedom, and antiferro-quadrupolar order is observed at $T_Q \approx 0.11$ K [382]; superconductivity emerges from within this ordered state ($T_c < T_Q$) [382]. The entropy released at T_Q is only $0.2R \ln 2$, indicating that quadrupolar fluctuations could play an important role in the formation of Cooper pairs [382]. However, extremely low upper critical field values with upper limit $H_{c2}(0) < 20$ Oe are observed and cyclotron effective masses of order m_0 are obtained in quantum oscillation measurements [384], indicating that Cooper pairs are not formed from heavy quasiparticles in $\text{PrIr}_2\text{Zn}_{20}$. Though it is probably not a heavy-fermion compound, uncovering superconductivity in $\text{PrIr}_2\text{Zn}_{20}$ (and in the related compound $\text{PrRh}_2\text{Zn}_{20}$ at $T_c \approx 0.06$ K [385]) set the stage for the discovery of heavy-fermion superconductivity in other Pr-based 1-2-20 compounds with Γ_3 ground states.

A nonmagnetic non-Kramers Γ_3 doublet ground state is also observed in the compound $\text{PrTi}_2\text{Al}_{20}$. The well-localized quadrupoles associated with this Γ_3 ground state order at $T_Q \approx 2.0$ K [259]. A large feature is observed at T_Q in the specific heat and a corresponding entropy of nearly $R \ln 2$ is recovered at T_Q ; the low-temperature entropy and $\chi(T)$ behavior are consistent with a Γ_3 ground state [259]. The specific heat feature at T_Q broadens under applied magnetic field, suggesting that order is possibly ferroquadrupolar in nature [259]. This hypothesis was confirmed in ultrasound measurements of $\text{PrTi}_2\text{Al}_{20}$ that directly probe the quadrupolar susceptibility [386]. Curie-Weiss behavior is observed in $\chi(T)$ data for $T > 250$ K, characterized by $\Theta_{CW} \approx -40$ K and $\mu_{eff} \approx 3.43 \mu_B/\text{Pr}$ [259]. Such a large Θ_{CW} could not be associated with the RKKY energy scale and must instead characterize a Kondo energy scale associated with the excited multiplet states. At lower temperature, a Kondo resonance is observed at ϵ_F in resonant photoemission spectroscopy measurements [387], and the $\rho(T) \sim T^2$ behavior for $T_Q \lesssim T \lesssim 20$ K and enhanced value of the Sommerfeld coefficient $\gamma \approx 100 \text{ mJ mol}^{-1} \text{ K}^{-2}$ all suggest that $\text{PrTi}_2\text{Al}_{20}$ is a moderately-heavy Fermi liquid system [260]. This interpretation is supported by estimating the Kadowaki-Woods ratio $A/\gamma^2 \approx 3.3 \times 10^{-6} \mu\Omega \text{ cm K}^2 \text{ mol}^2 \text{ mJ}^{-2}$ [260], which is comparable to the quasi-universal values exhibited by heavy Fermi-liquid systems [20, 21].

Superconductivity with $T_c \approx 0.2$ K emerges in $\text{PrTi}_2\text{Al}_{20}$ at ambient pressure out of this ferroquadrupolar ordered state [260]. A volume fraction of $\sim 60\%$ was obtained in zero-field cooled measurements of $\chi(T)$, which suggests that superconductivity is bulk [260]. The upper critical field value was measured with $H \parallel [110]$ in this cubic compound to be $H_{c2}(0) \approx 6$ mT [260]. The upper critical field curve $H_{c2}(T)$ agrees with a calculation from WHH theory for orbital limiting except near T_c where the experimentally measured initial slope $(dH_{c2}/dT)_{T_c}$ is slightly smaller than the best-fit value $(dH_{c2}/dT)_{T_c} \approx -47 \text{ mT/K}$ [260]; this discrepancy could be related to a multigap scenario for superconductivity in $\text{PrTi}_2\text{Al}_{20}$ [260]. The WHH theory predicts $H_{c2}^*(0) \approx 6.3$ mT, which agrees much better with the measured $H_{c2}(0)$ value than the estimated Pauli paramagnetic limit of $H_{p0} \approx 335$ mT [260]. From analysis of the $H_{c2}(T)$ curve, the effective quasiparticle mass is

estimated to be $m^*/m_0 \sim 16$, which is consistent with a moderate mass enhancement [260].

An effort was made to enhance the hybridization strength in $\text{PrTi}_2\text{Al}_{20}$ and to induce a quadrupolar Kondo effect by applying pressure [31]. With increasing pressure, $T_Q(P)$ traces out a weak dome with maximum near 6 GPa and superconductivity emerges above 6.7 GPa [31]; the observed dome of superconductivity has maximum $T_c \approx 1.1$ K at 8.7 GPa [31]. This pressure-induced superconducting state is distinct from the superconductivity observed at ambient pressure ($T_c \approx 0.2$ K) and emerges from a much heavier Fermi-liquid state [31]. These phases can be seen in Fig. 14(a). Bulk superconductivity in $\text{PrTi}_2\text{Al}_{20}$ was suggested by a large diamagnetic response in measurements of ac magnetic susceptibility and confirmed by a jump at T_c in the specific heat under applied pressure [31]. At 8.7 GPa, the upper critical field is $H_{c2}(0) > 3$ T with a large initial slope $(dH_{c2}/dT)_{T_c} \approx -6.0$ T/K (see Fig. 14(b)) [31]. The orbital limiting field is estimated using WHH theory [59] to be $H_{c2}^*(0) \approx 4.7$ T [31], which exceeds the Pauli limit of $H_{p0} \approx 2$ T. Using the upper critical field values at 8.7 GPa, an effective mass of $m^*/m_0 \sim 106$ is estimated [31], unambiguously confirming the heavy-fermion character of superconductivity in $\text{PrTi}_2\text{Al}_{20}$ under applied pressure. The electrical resistivity in the normal state exhibits a robust T^3 temperature dependence that may be a consequence of fluctuations of quadrupolar order [31]. It is possible that the heavy-fermion superconductivity in $\text{PrTi}_2\text{Al}_{20}$ may emerge in the vicinity of a quantum critical point associated with the suppression of ferroquadrupolar order where strong fluctuations arise due to competition between quadrupolar order and the quadrupolar Kondo effect [31].

$\text{PrV}_2\text{Al}_{20}$ is another 1-2-20 compound that exhibits a nonmagnetic Γ_3 non-Kramers doublet ground state. In contrast to $\text{PrTi}_2\text{Al}_{20}$, stronger hybridization in $\text{PrV}_2\text{Al}_{20}$ leads to heavy-fermion behavior at ambient pressure. Quadrupolar order is observed at $T_Q \approx 0.6$ K that is sensitive to sample purity [259]; two clear and distinct transitions are observed at $T_Q \approx 0.75$ K and $T^* \approx 0.65$ in samples with residual resistivity ratio (RRR) > 7 , leading to speculations regarding the possibility of order from octapolar degrees of freedom as well [62]. A broad feature is observed in the specific heat of $\text{PrV}_2\text{Al}_{20}$ and the corresponding entropy is found to be $\sim (R/2) \ln 2$ at T_Q [259, 62]. The response of this feature to applied magnetic field is consistent with antiferroquadrupolar order [259]. Curie-Weiss analysis of $\chi(T)$ data at high temperature yields $\Theta_{CW} \approx -55$ K with $\mu_{eff} \approx 3.57 \mu_B/\text{Pr}$ [259]. A large Kondo energy scale is implied by the value of Θ_{CW} . Non-Fermi liquid behavior is observed for $T > T_Q$ in the low-temperature physical properties including $C/T \sim T^{-3/2}$, $\chi(T) \sim -T^{1/2}$, and $\rho(T) \sim T^{1/2}$ temperature dependencies [259]. These behaviors are consistent with predictions for the two-channel or quadrupolar Kondo effect [27, 28, 29], and this possibility is strengthened by the $(R/2) \ln 2$ entropy released at T_Q [62]. The $\rho(T) \sim T^{1/2}$ behavior was observed in samples with a wide-range of purity, indicating that this state is robust (*i.e.*, in contrast to superconductivity) [259]. Partial quenching of the quadrupole moment is manifested in the feature in the specific heat at T_Q which is weaker than the corresponding feature in $\text{PrTi}_2\text{Al}_{20}$. The Som-

Figure 14: (Color online) (a) Temperature-pressure ($T - P$) phase diagram for $\text{PrTi}_2\text{Al}_{20}$. Unfilled circles and squares represent T_{max} , determined from the maxima in electrical resistivity measurements, and the ferroquadrupole (FQ) ordering temperature T_Q , respectively. A dome of pressure-induced superconductivity (SC) is observed with maximum near 9 GPa and the T_c values are obtained from electrical resistivity (filled circles), ac magnetic susceptibility (filled triangles), and specific heat (filled squares) measurements, respectively. The inset displays the cubic crystal structure of $\text{PrTi}_2\text{Al}_{20}$. (b) The upper critical fields $H_{c2}(T)$ for $\text{PrTi}_2\text{Al}_{20}$ under applied pressures of 6.7 GPa, 7.7 GPa, and 8.7 GPa, where T_c was determined from the temperature where the electrical resistivity vanishes. The increase of $(dH_{c2}/dT)_{T_c}$ with increasing pressure is dramatic. (c) $H_{c2}(T)$ for single crystals of $\text{PrV}_2\text{Al}_{20}$ and $\text{PrTi}_2\text{Al}_{20}$ (at ambient pressure) with $H \parallel [110]$. The square, diamond, circle, and triangle data points are determined from measurements of ac-susceptibility, ac-susceptibility with a SQUID, electrical resistivity, and specific heat, respectively. The solid lines represent fits based on the WHH model [59] for the orbital critical field. The inset displays the real part of the ac-susceptibility for $\text{PrV}_2\text{Al}_{20}$ under various magnetic fields and the arrows indicate T_c values. Panels (a) and (b) are adapted from Ref. [31] and panel (c) is from Ref. [62].

merfeld coefficient value is $\gamma \approx 90 \text{ mJ mol}^{-1} \text{ K}^{-2}$ [62], which is modestly enhanced and consistent with the relatively strong hybridization in $\text{PrV}_2\text{Al}_{20}$.

From this antiferroquadrupolar ordered heavy-fermion state, superconductivity is observed at ambient pressure with $T_c \approx 0.05 \text{ K}$ in samples with high purity ($\text{RRR} \sim 19$) [62]. Superconductivity is not observed in samples with $\text{RRR} < 5$, suggesting that superconductivity in $\text{PrV}_2\text{Al}_{20}$ is unconventional [62]. Magnetic susceptibility measurements indicate superconducting volume fractions are as large as 82% and a jump in the specific heat at T_c of $\Delta C/\gamma T_c \approx 0.3$ [62] both act to confirm the bulk nature of superconductivity in $\text{PrV}_2\text{Al}_{20}$. The upper critical field at zero temperature is estimated to be $H_{c2}(0) \approx 14 \text{ mT}$ with an initial slope of $(dH_{c2}/dT)_{T_c} \approx -0.41 \text{ T/K}$ (see Fig. 14(c)), and it appears to follow a $H_{c2}(T)$ curve calculated using WHH theory [62]. This observation indicates that Cooper pairs are probably orbitally limited. The value of $(dH_{c2}/dT)_{T_c}$ for $\text{PrV}_2\text{Al}_{20}$ is an order of magnitude larger than the corresponding value in $\text{PrTi}_2\text{Al}_{20}$ at ambient pressure [260], indicating that quasiparticles have a significantly heavier effective mass. An enhanced effective mass of $m^*/m_0 \sim 140$ for $\text{PrV}_2\text{Al}_{20}$ is estimated using the upper critical field [62], which is comparable to that of $\text{PrTi}_2\text{Al}_{20}$ under an applied pressure near 8 GPa [31]. This similarity suggests that $\text{PrV}_2\text{Al}_{20}$ may also be in close proximity to a quantum critical point associated with quadrupolar order [62]. If this hypothesis is correct, the pairing mechanism for superconductivity in $\text{PrTi}_2\text{Al}_{20}$ and $\text{PrV}_2\text{Al}_{20}$ is probably the same and is likely associated with quadrupolar fluctuations.

This family of compounds that adopt the $\text{CeCr}_2\text{Al}_{20}$ -type crystal structure has been a fertile reservoir of new Pr-based

heavy-fermion superconductors so far. The exciting recent discovery of Cd-based 1-2-20 compounds [388, 389] includes $\text{PrNi}_2\text{Cd}_{20}$ and $\text{PrPd}_2\text{Cd}_{20}$, which are currently being studied to ascertain whether heavy-fermion superconductivity associated with potential Γ_3 ground state [390] might also be observed. Regardless of the outcome of those studies, it appears that the point-group symmetry of the crystallographic site filled by the Pr ion and the other properties arising from the crystal structure, make the 1-2-20 compounds an excellent place to search for new Pr-based heavy-fermion superconductors.

4.2. Yb-based compound: $\beta\text{-YbAlB}_4$

The trivalent Yb ion has a $4f^{13}$ electronic configuration, and is therefore often considered to be the hole analogue of trivalent Ce with its $4f^1$ electronic configuration. Naively, this similarity combined with the propensity for valence instability would be expected to produce similar Kondo physics in Yb compounds; yet, the number of Yb-based heavy-fermion compounds is far smaller than the number of Ce-based heavy-fermion compounds. This interesting empirical fact was discussed by Fisk and Maple who, based on the single Ce-based heavy-fermion superconductor known at the time (CeCu_2Si_2), speculated that there would not be many Yb-based heavy-fermion compounds that also exhibit superconductivity [391]. This prediction has so far been validated: only a single Yb-based heavy-fermion superconductor has been reported to date.

Superconductivity was observed in 2008 in high-purity samples ($\text{RRR} \sim 300$) of the heavy-fermion compound $\beta\text{-YbAlB}_4$ with a $T_c \approx 0.08 \text{ K}$ [63, 261]. This compound forms with an orthorhombic crystal structure, characterized by the space group $Cmmm$ [63]. The crystal structure is composed of Yb

and Al ions sandwiched between B layers, which might be expected to produce a two-dimensional Fermi surface; however, local density approximation (LDA) band-structure calculations [392] and quantum oscillation studies [393] demonstrate that β -YbAlB₄ has a three-dimensional Fermi surface composed of two sheets from heavy bands of f -like character.

We begin our discussion of β -YbAlB₄ by describing its normal-state properties. Calculations suggest that β -YbAlB₄ should exhibit an antiferromagnetic ground state, however, it remains paramagnetic instead [392]. Magnetic susceptibility $\chi(T)$ measurements demonstrate strong uniaxial anisotropy that is consistent with an Ising system with magnetic moments tending to align along the c axis [63]. With $H \parallel c$, Curie-Weiss behavior in $\chi(T)$ data is observed for $T > 100$ K with $\Theta_{CW} \sim -210$ K and an effective Ising moment of $\sim 3.1\mu_B$; in contrast, the in-plane magnetic susceptibility is only weakly temperature-dependent with a subtle peak near 200 K [63]. The electrical resistivity $\rho(T)$ displays a weak coherence peak near 250 K and goes as $\rho \propto T$ for $1 < T < 4$ K and $\rho \propto T^{1.5}$ for $T \lesssim 1$ K [63]. These are strong manifestations of non-Fermi liquid behavior in β -YbAlB₄. The features in $\chi(T)$ and $\rho(T)$ data near 200 K and 250 K, respectively, reveal a relatively large Kondo energy scale [63]; however, careful measurements of the Hall effect in β -YbAlB₄ later provided evidence for two distinct Kondo-like energy scales at 40 K and 200 K [394]. The Sommerfeld coefficient can be estimated by applying a small magnetic field, causing the diverging C/T data at low temperature to saturate; a value of $\gamma \simeq 150$ mJ mol⁻¹ K⁻² is obtained by this procedure [63]. An effective mass of the quasiparticles $m^*/m_0 \sim 180$ can be estimated [261] while values of $m^*/m_0 \sim 5$ -14 are obtained in Shubnikov-de Haas experiments [393]. These latter values of m^*/m_0 have been suppressed by the high magnetic fields used in the quantum oscillation measurements as we discuss below.

Astoundingly, the intriguing non-Fermi liquid state observed in the physical properties at low temperature [63] is accessed in β -YbAlB₄ without any external tuning [395]. Furthermore, this behavior is apparently robust [63], being observed in samples with RRR values between 75-300 including samples that do not exhibit superconductivity [261]. Fermi-liquid behavior is rapidly restored in β -YbAlB₄ by applying a magnetic field, with the $\rho \propto T^{1.5}$ behavior only being observed in early experiments when $H < 0.1$ T [63]; this upper limit for the crossover field was later reduced to 0.2 mT [395]. By fitting the Fermi-liquid $\rho \simeq AT^2$ behavior in several magnetic fields ($H \parallel c$), it is observed that $A \sim H^{1/2}$, which is consistent with the presence of a quantum critical point at zero-field [63]. Furthermore, unconventional quantum criticality is manifested in T/H scaling of the thermodynamic free energy over a wide range of temperatures and magnetic fields (see Fig. 15) and a diverging effective quasiparticle mass $m^* \sim H^{-1/2}$ [395]. When these unconventional signatures of quantum criticality are combined with the intermediate Yb valence in β -YbAlB₄ (discussed below), the zero-field quantum critical point must be unconventional as well [395]. A model to describe the intrinsic quantum criticality observed in β -YbAlB₄ has been proposed by Ramires *et al.* [396].

The valence of Yb in β -YbAlB₄ was initially predicted to be

Figure 15: (Color online) Scaling of the thermodynamic free energy of β -YbAlB₄, represented by $-(dM/dT)B^{1/2}$ as obtained from experimental measurements of magnetic susceptibility M , over several decades of the parameter T/B (where T is temperature and B is magnetic field). This scaling suggests that a quantum critical point (QCP) is found at zero field. If a QCP exists at $B_c \neq 0$ T, the free energy will scale with a parameter $T/|B - B_c|$. The best fits of $-(dM/dT)B^{1/2}$ using this more generalized scaling parameter place an upper bound of $|B_c| < 0.2$ mT as is seen in the upper inset showing Pearson's correlation coefficient R vs. B_c . The lower left inset displays the magnetic field-temperature ($B - T$) phase diagram of β -YbAlB₄. The filled circles are determined from the peak temperatures in $-dM/dT$, and denote a crossover between non-Fermi liquid and Fermi liquid behavior. The dashed line indicates $k_B T \sim g\mu_B B$. The unfilled circles depict the temperatures, below which, the electrical resistivity shows a quadratic temperature dependence (after Ref. [395]).

intermediate in LDA calculations [392], and hard x-ray photoemission measurements subsequently observed signatures of an intermediate Yb valence in the Yb 3d spectra [397]. From measurements at 20 K, the Yb valence was determined to be Yb^{2.75(2)+}, which is much lower than the 2.9+ to 3+ Yb valences typically observed in other Yb-based heavy-fermion compounds [397]. This intermediate Yb valence, which is a consequence of strong hybridization between 4f and conduction electron states, is consistent with the relatively large Kondo energy scale of order 200-250 K [395]. The valence fluctuations in β -YbAlB₄ are expected to play a role in producing the non-Fermi liquid behavior, which is intriguingly similar to the behavior of the intermediate valence materials YbRh₂Si₂ and YbRh₂(Si_{0.95}Ge_{0.05})₂ [398]. Adding credibility to this possibility, an electron spin resonance (ESR) signal is observed in β -YbAlB₄ [399] that is similar to ESR results for YbRh₂Si₂, begging the question of whether there is a connection between this ESR signal and quantum criticality in these intermediate valence compounds [399, 400]. While each compound exhibits a similar diverging Nernst coefficient in the vicinity of their respective quantum critical points, the response of the ratio of thermoelectric power divided by temperature, S/T , and γ for each is different [401]. This latter result suggests that comparisons between these two compounds need to be made carefully, but the present observations offer intriguing support for a rela-

tionship between valence fluctuations and the non-Fermi liquid behavior in β -YbAlB₄.

Superconductivity in β -YbAlB₄ emerges from this non-Fermi liquid state with a T_c that depends sensitively on sample purity (superconductivity is only present in samples with $RRR > 100$) [63]. This sensitivity to disorder is consistent with an unconventional superconductivity with non-*s*-wave character [63]. Measurements of the magnetization in a 0.1 mT magnetic field obtained a superconducting volume fraction of 15%-45% in zero-field cooled measurements [63, 261]. The reduced values of the volume fraction are partially related to the long magnetic penetration depth relative to the small dimensions of the sample [261]. To date, a jump in the specific heat has not been reported for β -YbAlB₄, but these magnetic susceptibility results may be consistent with bulk superconductivity.

The upper critical fields $H_{c2}(T)$ of β -YbAlB₄ are anisotropic with an anomalous suppression at low temperature that is likely associated with paramagnetic effects related to the *c*-axis magnetic susceptibility [261]. The initial slopes are measured to be $(dH_{c2}^a/dT)_{T_c} \approx -2.6$ T/K and $(dH_{c2}^c/dT)_{T_c} \approx -1.4$ T/K with extrapolated values at zero temperature of $H_{c2}^a(0) \approx 0.15$ T and $H_{c2}^c(0) \approx 0.025$ T [261]. An estimate for the orbital critical field yields $H_{c2}^{*,a}(0) \approx 0.15$ T, which is in excellent agreement with the observed results for $H_{c2}^a(0)$ [261]. However, $H_{c2}^c(0) < H_{c2}^{*,c} \approx 0.076$ T $< H_{p0} \approx 0.15$ T, indicating the presence of other pair-breaking effects beyond simple orbital and paramagnetic effects [261]. Superconducting coherence lengths at zero temperature of $\xi_a(0) \approx 66$ nm and $\xi_c(0) \approx 33$ nm are estimated using the Ginzburg-Landau formula for an anisotropic superconductor [261]. In a sample that did not exhibit superconductivity above 30 mK, the mean free path is only a factor of 4 times larger than $\xi_a(0)$, indicating that superconductivity in β -YbAlB₄ only appears in the clean limit [261].

4.3. Pu- and Np-based heavy-fermion superconductors

Around the same time as the discovery of the first heavy-fermion compound, CeAl₃ [9], it was recognized that a quadratic temperature dependence of the electrical resistivity at low temperatures and large values of the Sommerfeld coefficient γ could be found in transuranium compounds like PuAl₂ [402, 403]. These early studies demonstrated that such compounds could exhibit heavy Fermi-liquid states; though, this was not completely appreciated at the time. Superconductivity at ambient pressure was discovered in transuranium compounds with $T_c = 18.5$ K in PuCoGa₅ [107], $T_c = 8.7$ K in PuRhGa₅ [108], and $T_c = 4.9$ K in NpPd₅Al₂ [221]. The properties of these compounds have been reviewed in Refs. [404, 111, 262] and the Pu-based systems are also addressed in a dedicated article by Sarrao *et al.* in this special issue of Physica C. Therefore, we will only briefly summarize the highlights. Along with compounds like U₆T (*T* = transition metal), these compounds may constitute a link that bridges traditional Ce and U-based heavy-fermion superconductors and other classes of unconventional superconductors including the cuprates.

The compounds PuCoGa₅ and PuRhGa₅ crystallize in a tetragonal crystal structure characterized by space group

P4/mmm and are isostructural with the Ce-based “115” compounds discussed in Section 2.2. These compounds exhibit comparable, modestly-enhanced Sommerfeld coefficient values of $\gamma \approx 77$ mJ mol⁻¹ K⁻² and 70 mJ mol⁻¹ K⁻² for PuCoGa₅ and PuRhGa₅, respectively [107, 262]. These values can be compared to $\gamma \approx 50$ mJ mol⁻¹ K⁻² for δ -Pu [107]. Bulk superconductivity is demonstrated by the jumps observed at T_c in the specific heat measurements. For PuCoGa₅, a jump of $\Delta C/\gamma T_c \approx 1.4$ [107] is very close to the BCS value, while a smaller jump of $\Delta C/\gamma T_c \approx 0.65$ is observed for PuRhGa₅ [264]. In the superconducting state of each compound, the quadratic temperature dependence of the specific heat provides evidence for line nodes in the superconducting energy gap [264, 263]. The initial slope of the upper critical field of PuCoGa₅ is $(dH_{c2}/dT)_{T_c} \approx -5.9$ T/K, which implies an enormous $H_{c2}^*(0) \approx 74$ T [107]; measurements of the initial slope using measurements of specific heat suggest even larger values of $(dH_{c2}^a/dT)_{T_c} \approx -10$ T/K and $(dH_{c2}^c/dT)_{T_c} \approx -8$ T/K [264]. For PuRhGa₅, the initial slopes of the upper critical fields are smaller at $(dH_{c2}^a/dT)_{T_c} \approx -3.5$ to -4 T/K and $(dH_{c2}^c/dT)_{T_c} \approx -2$ T/K [264, 262]. The values of the upper critical at zero temperature for PuRhGa₅ are measured to be $H_{c2}^a(0) \approx 27$ T and $H_{c2}^c(0) \approx 15$ T, which are comparable to estimates of the orbital-limiting fields [262]. Superconductivity in these compounds degrades with time due to self-irradiation effects. For example, the rate of change $\Delta T_c/\Delta t$ is ~ 0.24 K/month and ~ 0.39 K/month for PuCoGa₅ and PuRhGa₅, respectively [49].

The compound NpPd₅Al₂ crystallizes with the tetragonal crystal structure with space group *I4/mmm*. Like the Pu-based superconductors, NpPd₅Al₂ is paramagnetic with an enhanced Sommerfeld coefficient of $\gamma \approx 200$ mJ mol⁻¹ K⁻² [221]. In the normal state, non-Fermi liquid behavior is observed as manifested by a linear temperature dependence of the electrical resistivity, followed by a transition to superconductivity at $T_c \approx 4.9$ K [221]. At T_c , a jump of $\Delta C/\gamma T_c \approx 2.33$ is observed in the specific heat, confirming the bulk nature of strongly-coupled superconductivity [221]. For $T < T_c$, the cubic temperature dependence of the specific heat suggests the presence of point nodes in the superconducting energy gap structure [221]. The strongly-anisotropic initial slopes of the upper critical fields are $(dH_{c2}^a/dT)_{T_c} \approx -6.4$ T/K and $(dH_{c2}^c/dT)_{T_c} \approx -31$ T/K, and the measured values of the upper critical fields of NpPd₅Al₂ at zero temperature are $H_{c2}^a(0) \approx 3.7$ T and $H_{c2}^c(0) \approx 14$ T [221]. This value of $H_{c2}^c(0)$ is strongly paramagnetically-limited ($H_{p0} \approx 9$ T) relative to the expected orbital critical field of $H_{c2}^{*,c}(0) \approx 105$ T [221].

5. Concluding remarks

5.1. General characteristics of superconductivity in heavy-fermion compounds

Throughout this selective review, we have frequently encountered the same, or strikingly similar, properties in the superconducting and normal states of the of heavy-fermion compounds that we have discussed. These characteristics, many of which are presented in Table 3, constitute a basic set of properties that

are shared by all superconducting heavy-fermion compounds. They can be divided into six properties that we briefly describe below.

(1) The superconducting transition temperatures T_c are generally of order 1 K with some being as low as 0.05 K (like in $\text{PrV}_2\text{Al}_{20}$ [62]) and some as high as 2.3-2.4 K (like in CeCoIn_5 [96] and CeRhIn_5 [94] under ambient and applied pressures, respectively). In this review, we have also briefly discussed a few compounds with T_c values that are significantly higher, including U_6Fe ($T_c \approx 3.8$ K) [225] and the actinide-based compounds PuCoGa_5 ($T_c \approx 18.5$ K) [107], PuRhGa_5 ($T_c \approx 8.7$ K) [108], and NpPd_5Al_2 ($T_c \approx 4.9$ K) [221]. However, despite sharing many compelling similarities with superconducting heavy-fermion compounds, these latter compounds may rather be links that connect the heavy-fermion compounds to the cuprates and other classes of unconventional superconductors.

(2) The specific heat jumps at T_c in heavy-fermion compounds are of order γT_c . Since heavy-fermion compounds are characterized by significantly-enhanced values of γ , this result reveals that it is the heavy quasiparticles that pair in their superconducting states. The measured $\Delta C/\gamma T_c$ values typically range between 0.2-4.5 (see Table 3). Unfortunately, there are many compounds for which $\Delta C/\gamma T_c$ has not yet been measured because of experimental challenges associated with measuring specific heat at either extremely low temperature (*i.e.*, when T_c values are very low) or under applied pressure (*i.e.*, when superconductivity is pressure-induced).

(3) The measured upper critical fields $H_{c2}(T)$ in heavy-fermion compounds have *very* large initial slopes $(dH_{c2}/dT)_{T_c}$ near T_c (see Table 2 for some examples). These values of $(dH_{c2}/dT)_{T_c}$ are generally on the order -1 T/K to -10 T/K with particularly high values for CeCu_2Si_2 (-23 T/K) [66], CeRhSi_3 (-23 T/K at 2.6 GPa) [213], CeCoIn_5 (-24 T/K for $H\parallel ab$) [133], and UBe_{13} (-42 T/K) [347]. Such large $(dH_{c2}/dT)_{T_c}$ values indicate that the orbital upper critical fields at zero temperature, $H_{c2}^*(0)$, are also quite large; as a consequence, superconductivity in many heavy-fermion compounds is paramagnetically limited (*i.e.*, $H_{c2}(0) \approx H_{p0} < H_{c2}^*(0)$).

(4) The large values of $(dH_{c2}/dT)_{T_c}$ and $H_{c2}^*(0)$ in heavy-fermion compounds also indicate that the Ginzburg-Landau coherence lengths at zero temperature, $\xi(0)$, tend to be short; $\xi(0)$ values of order 10-100 Å are typical. Such short coherence lengths are consistent with the heavy effective masses, m^* , of the quasiparticles involved in pairing, since $\xi(0) \propto 1/m^*$. The Ginzburg-Landau parameter, which is the ratio of the London penetration depth λ to ξ , is $\lambda/\xi \gg 1/\sqrt{2}$ in heavy-fermion compounds, indicating that they are extreme type II superconductors.

(5) Superconductivity in heavy-fermion compounds is unambiguously unconventional. In the superconducting state, experimental evidence is consistent with quasiparticle pairs that are characterized by either *d*-wave, spin singlet ($L = 2$, $S = 0$) or *p*-wave, spin triplet ($L = 1$, $S = 1$) states. Pairing in most of the heavy-fermion compounds is believed to be *d*-wave, but potential evidence for spin-triplet pairing has been observed in some compounds profiled in this article including

CePt_3Si , CeIrSi_3 , UNi_2Al_3 , UGe_2 , UCoGe , and U_2PtC_2 (see their respective sections). This evidence generally comes from NMR measurements of a temperature-independent Knight shift and/or by measuring $H_{c2}(0)$ values that dramatically exceed the Chandrasekhar-Clogston limit. The symmetry of the superconducting energy gap has not been established by phase-sensitive measurements in any of the heavy-fermion compounds as it has been in the cuprates [117], but point-contact [114] and tunneling spectroscopy [115, 116] measurements of CeCoIn_5 are consistent with a $d_{x^2-y^2}$ gap symmetry. In nearly all of the heavy-fermion compounds, power-law behavior in the temperature dependence of the specific heat, penetration depth, thermal conductivity, and other physical properties in the superconducting states are used to infer the existence of point or line nodes in the energy gaps [60]; additional information about the symmetry of $\Delta(\mathbf{k})$ and details concerning the nodal structure are sometimes obtained by studying modulations of the specific heat or thermal conductivity as a single crystal is rotated relative to a magnetic field with fixed orientation. The evidence from such studies on heavy-fermion compounds has been *nearly* universally consistent with anisotropic and nodal superconducting energy gaps; however, we note that evidence for nodeless gaps has been presented recently from measurements of the specific heat for CeCu_2Si_2 [75] and London penetration depth in the system $\text{Ce}_{1-x}\text{Yb}_x\text{CoIn}_5$ [182, 185]. These results may force us to re-examine the conventional understanding of quasiparticle pairing in these systems and emphasize that there is still a lot of work remaining to obtain a comprehensive understanding of superconductivity in heavy-fermion compounds.

(6) The final characteristic that we will discuss is the proximity of the superconducting ground state to another ordered phase that tends to involve the magnetic or, less frequently, electric quadrupole degrees of freedom. These ordered phases are highly tunable, and in the case of heavy-fermion compounds, are susceptible to being suppressed by applied pressure or chemical substitution. This is evident in the significant number of heavy-fermion compounds within which superconductivity is pressure induced, emerging only after the ordered state has been suppressed. Such compounds have a superscripted asterisk following their T_c values in Table 3 as well as an entry in the neighboring column to the right that provides the transition temperature of the magnetic or quadrupolar ordered phase at ambient pressure. For some compounds such as CeRhIn_5 , magnetic order need not be completely suppressed for superconductivity to emerge, and there are limited regions of phase space within which superconductivity and magnetic order coexist (see the phase diagram in Fig. 4 for example). When superconductivity is observed at ambient pressure, nature has already conveniently suppressed the nearby ordered phase. Compounds in this category exhibit an instability at ambient pressure towards ordering of the magnetic or quadrupole degrees of freedom. Sometimes the ordered phase that is on the verge of forming can be persuaded to emerge by modifying the chemical composition as in the spin-density wave order in CeCu_2Si_2 [66, 70], exists at “negative pressure” like antiferromagnetic order in CeCoIn_5 , or is accessed by applying pressure like the antiferromagnetic or-

der in URu_2Si_2 [304]. The abundance of spin (or quadrupolar) fluctuations that are found in these unstable environments are widely believed to play a role in mediating quasiparticle pairing in the superconducting state. Similarly, non-Fermi liquid behavior in the normal-state physical properties of many such heavy-fermion compounds is probably facilitated by the strong quantum fluctuations associated with the nearby quantum critical point [15, 8, 39].

5.2. Comparison of superconductivity in heavy-fermion compounds with that in the cuprates and iron pnictide/chalcogenide compounds

Now that we have outlined and articulated some of the characteristics of the superconducting state in heavy-fermion compounds, we can briefly compare these properties with those of other classes of unconventional superconductors including the cuprates and iron pnictide/chalcogenide compounds. Many instructive review articles have been published that discuss the superconducting properties of the iron pnictide and iron chalcogenide compounds [405, 406, 407, 408] as well as the cuprates [409, 410, 411]; furthermore, there are articles dedicated to each of these classes of superconducting materials in this special issue of *Physica C*. Similarities between these families of unconventional superconductors, including the quasi-two-dimensional layer components of their crystal structures, comparable phase diagrams, observations of a spin resonance in the superconducting states from inelastic neutron scattering measurements, and similar superconducting energy gap symmetries, have been discussed for some time [412, 204, 413]. We briefly address some of these similarities below.

The superconducting cuprates and iron pnictide/chalcogenide compounds are well-known for having layered crystal structures in which superconductivity resides within the CuO_2 planes [409, 410, 411] or corrugated Fe/pnictogen (or Fe/chalcogenide) layers [405, 406, 407, 408], respectively. Their quasi-two-dimensional crystal structures are also believed to play a significant role in the high T_c values that are encountered in these families of compounds. In contrast, a quasi-two-dimensional, layered crystal structure is not observed universally among the superconducting heavy-fermion compounds; however, CeCoIn_5 does serve as an interesting example wherein such a discussion is relevant. The cubic compound CeIn_3 has an antiferromagnetic ground state that can be suppressed by applied pressure, leading to the emergence of superconductivity with $T_c \simeq 0.2$ K [58]. This material is sometimes said to contain an infinite number of CeIn_3 layers. The structurally-related compound, CeCoIn_5 , has a tetragonal crystal structure that is composed of alternating CeIn_3 and CoIn_2 layers. Instead of an antiferromagnetic ground state, CeCoIn_5 exhibits superconductivity at ambient pressure with a T_c that is an order of magnitude larger than in CeIn_3 (i.e., $T_c \simeq 2.3$ K) [96]. In analogy with the cuprates and iron pnictide/chalcogenide compounds, its layered, quasi-two-dimensional crystal structure is sometimes invoked to explain the large enhancement of T_c in CeCoIn_5 relative to that in CeIn_3 .

We have already discussed in the previous section that heavy-fermion compounds are characterized by phase diagrams in which there is a close proximity (or sometimes coexistence) between superconductivity and a nearby magnetic or quadrupolar ordered state. This is also a common and defining element of the phase diagrams in superconducting cuprates and iron-pnictide/chalcogenide compounds. As their antiferromagnetic or spin-density wave ordered states are suppressed by a non-thermal control parameter such as pressure or chemical composition, the magnetic phase boundaries tend to zero temperature, often terminating in a quantum critical point [409, 410, 411, 405, 406, 407, 408]; though, there are cases, such as in $\text{LaFeAsO}_{1-x}\text{F}_x$, in which the ordered phase terminates in a first-order phase transition [414] and there is no quantum critical point. When it is present, the quantum critical point is typically protected by a dome of superconductivity. In the phase space near the quantum critical point, the physical properties in the normal state are unconventional as manifested in the “strange metal” phase in the cuprates or non-Fermi liquid behavior in heavy-fermion compounds. At values of the control parameter greater than where the quantum critical point is located, there is usually a crossover to a Fermi liquid ground state. Generic examples of some of the phase diagrams that are encountered in these classes of materials are provided in Ref. [8].

There are also broad similarities between the superconducting energy gap symmetries of these unconventional classes of superconductors [204]. Superconductivity in the cuprates and most heavy-fermion compounds is believed to involve d -wave pairing. The energy gaps associated with such pairing are nodal and undergo sign changes between regions on the Fermi surface or surfaces separated by wave vector $\vec{Q}$ (i.e., $\text{Sgn}\Delta(\vec{k} + \vec{Q}) = -\text{Sgn}\Delta(\vec{k})$) where $\vec{Q}$ is associated with spin-fluctuations that are peaked at that momentum. The iron pnictide/chalcogenide compounds are generally thought to exhibit $s^\pm$ -pairing, which also involves a sign change of the gap; though, any nodes are typically accidental. The normally repulsive interactions involving spin fluctuations are rendered attractive when there is such a sign change in the energy gap, enabling unconventional quasiparticle pairing by spin fluctuations in these compounds [204]. When $\vec{k} = \vec{Q}$, a spin resonance feature is expected in inelastic neutron scattering experiments [204]. Such spin resonance features have been experimentally observed in the superconducting states of CeCoIn_5 [200], $\text{YBa}_2\text{Cu}_3\text{O}_7$ [415, 416, 417], $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ [418], and $\text{Ba}(\text{Fe}_{0.925}\text{Co}_{0.075})_2\text{As}_2$ [419]; these results in examples from each class of unconventional superconductor strongly support a common pairing mechanism via spin fluctuations.

We complete our discussion concerning the similarities between the classes of unconventional superconductors by considering an intriguing empirical observation plotted in Fig. 16. The T_c values for various superconductors are plotted as a function of T_0 , the frequency spread of the wave-vector-dependent part of the spin fluctuations (or a characteristic spin-fluctuation temperature), on a log-log plot. The line in Fig. 16 serves as a guide to the eye to emphasize an apparent relationship between

Figure 16: (Color online) Superconducting critical temperature T_c plotted vs. characteristic spin fluctuation temperature T_0 on a log-log scale for several U-based compounds (blue triangles), Ce-based compounds (gold circles), Pu-based compounds (red circles), and cuprates (magenta squares). A roughly linear relationship between T_c and T_0 is evident for the compounds in this plot, suggesting a relationship between spin fluctuations and superconductivity that is emphasized by a line that serves as a guide to the eye. Figure adapted from Refs. [420, 111].

T_c and T_0 . In practice, T_0 is obtained from an analysis of data from nuclear quadrupole resonance, specific heat, or electrical resistivity measurements [420, 421, 111]. We wish to emphasize two points concerning Fig. 16. First, there is a striking and continuous relationship between T_0 and T_c among these compounds. Second, compounds like PuCoGa₅, PuRhGa₅, and U₆Fe fall between the heavy-fermion compounds and cuprates, bridging the void between them. Therefore, they share an intimate connection with the two classes of unconventional superconductors that bound them in Fig. 16. We might also briefly add that the effective quasiparticle mass m^* that is often used to classify heavy-fermion compounds exists on a continuum. Furthermore, the hybridization between the localized f - and conduction-electron states, which is embodied in the Friedel-Anderson model, includes both the Kondo limit (integral f -electron shell occupation number) and the valence-fluctuation limit (non-integral f -electron shell occupation number), both of which can lead to the heavy-fermion extreme. In this sense, the term “heavy-fermion physics” is probably a misnomer, since it represents one limit of a more general problem. In any case, this empirical relationship between T_c and T_0 is consistent with a common pairing mechanism based on spin fluctuations for all of the compounds included in Fig. 16.

5.3. Outlook for research on superconductivity in heavy-fermion compounds

The current understanding of superconductivity in heavy-fermion compounds is built upon 35 years of intense experimental and theoretical investigations. While many questions have been answered, there are numerous intriguing and unresolved issues to address, and more superconducting compounds to be discovered. In this selective review, we have attempted to

provide a basic assessment of the current understanding of the normal- and superconducting-state properties of heavy-fermion compounds. We end by attempting to provide an outlook for the future of research in this fascinating and rich field of physics.

Until a comprehensive understanding of unconventional superconductivity is obtained, one obvious and vital way for the field to advance is to discover new heavy-fermion compounds with superconducting ground states, and to investigate their properties. There is a plot in Ref. [49] showing the number of known f -electron compounds with superconducting ground states (most of them are classified as heavy-fermion compounds in this article) as a function of year. From this plot, it appears that a new compound was discovered every two years (on average) between 1979 and 2000, after which, an average of nearly three new compounds were discovered per year up to 2009. This is strong evidence that components of a successful strategy for discovering new superconductors have already been identified and are being utilized. The future approach to discovering superconductivity in new heavy-fermion compounds should naturally build upon these components, which include studying strongly-correlated electron compounds based on Ce, Pr, Yb, and U, and subjecting such materials to measurements at low-temperature under ambient and applied pressures. Measurements under applied pressure are particularly important when compounds exhibit magnetic (or electric quadrupole) ordered ground states that can be suppressed. New search strategies are also being identified; for example, the relatively recent discoveries of superconductivity in the heavy-fermion compounds PrTi₂Al₂₀ [31], PrV₂Al₂₀ [62], and β -YbAlB₄ [63] were only made possible by synthesizing and studying very high-quality single crystals. Superconductivity is not observed in samples of these compounds for which the measured residual resistivity ratio values fall below a sample-specific threshold. These examples demonstrate that exercising careful control of synthesis procedures to produce ultra-clean samples with low disorder may be extremely important when searching for superconductivity in some heavy-fermion compounds. It may also be rewarding to expand the search for superconductivity into relatively unexplored potential reservoirs of heavy-fermion compounds such as among the transition-metal oxides; though, we note that neither of the two known cases (LiV₂O₄ [40] and CaCu₃Ru₄O₁₂ [41]) exhibit superconductivity. The future of research on superconductivity in heavy-fermion compounds is full of promise, and there is every reason to believe that investigations of newly-discovered compounds as well as studies designed to obtain a more comprehensive understanding of known compounds will contribute to resolving the long-standing puzzle of how unconventional superconductivity works.

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