Femtosecond Filament-Laser Ablation Molecular Isotopic Spectrometry

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Abstract

A new remote sensing technology for real-time isotopic analysis is introduced: Femtosecond Filament-Induced Laser Ablation Molecular Isotopic Spectrometry (F²-LAMIS). The technique combines femtosecond (fs) laser filamentation and ablation-based molecular isotopic spectroscopy, thereby enabling isotopic analysis of samples at a distance, in ambient air and at ambient pressure conditions. Isotopic analysis of zirconium (Zr) samples by F²-LAMIS is demonstrated, and the molecular and atomic emission intensity, and properties of the filament-induced plasma generated at different filament propagation distances were investigated. Spectral fitting of F²-LAMIS spectra enabled semi-quantitative isotopic analysis without the use of calibration standards, which was independent of the filament propagation distance for the studied range. This technology provides new capabilities for direct isotopic ratio measurements at remote distances.

Keywords: Femtosecond Filament-Induced Laser Ablation Molecular Isotopic Spectrometry (F²-LAMIS); Isotopic Analysis; Laser Ablation Molecular Isotopic Spectrometry (LAMIS); Filamentation; Molecular Emission Spectra.

1. Introduction

Laser Induced Breakdown Spectroscopy (LIBS) is a powerful direct solid sampling analytical technique for rapid, all-optical elemental analysis of materials. The process involves a high-power pulsed laser beam directed and focused onto a sample surface to instantaneously convert a finite volume of the sample into plasma (laser ablation), and subsequent analysis of the resulting optical emission spectra. One of the advantages of LIBS is its all-optical nature, which enables stand-off elemental analysis. The most common configuration for creating the laser induced plasma at a distance is by focusing high energy nanosecond laser pulses with large open-truss telescope systems.[1,2] One of the challenges with using nanosecond (ns) lasers for stand-off LIBS is the limited operation range, associated with difficulty to tightly focus the laser beam at long distances. Classical optical diffraction causes the laser beam diameter at the focus to linearly increase with focusing distance, and as a result, delivering sufficient laser fluence for ablation at a distance is challenging. Today, conventional ns LIBS stand-off material analysis [1,2] is limited to a little over 100 meters.[3]

In contrast to nanosecond lasers, it is possible for femtosecond laser beams to propagate over long distances as a result of the non-linear process of laser filamentation.[4] Filamentation of an intense, ultrashort laser pulse arises from dynamic balance between beam Kerr self-focusing and defocusing action of free electrons produced by multi-photon ionization of air molecules.[4–7] Unlike ns lasers, self-sustained fs filaments do not require large telescope systems to focus the laser beam. Filaments have a central core (typical diameter: $10^2 \mu\text{m}$) with high intensity (10^{13} W/cm^2 [8]) that is surrounded by an energy reservoir, which can replenish the filament core and support the filamentation

1 process over long distances. The propagation distance before filament formation and the
2 filament length depend on the laser parameters, and can be formed with pre-focused or
3 freely propagating femtosecond laser beams.[9] Remote filament induced breakdown
4 spectroscopy has been previously reported for elemental discrimination of composite
5 graphite samples,[10] biological materials[11,12], metals[13] detection and sensing of
6 explosives.[14]

7 The ability to perform not just elemental analysis but also isotopic analysis at a distance
8 is important for some remote sensing applications, including nuclear non-proliferation
9 and forensics.[15,16] Despite all the research on LIBS, the ability to provide isotopic
10 information is limited to only a few studies (e.g., H, Li and U).[17–19] The recent
11 development of Laser Ablation Molecular Isotopic Spectrometry (LAMIS) introduced a
12 new way for direct isotopic analysis at atmospheric pressure. LAMIS uses radiative
13 transitions from molecular species either directly vaporized from a sample or formed by
14 associative mechanisms of atoms or ions in a laser ablation plume,[20,21] thereby
15 expanding all the advantages of LIBS to isotopic analysis. LAMIS analysis of several
16 isotope systems (H/D, $^{10/11}\text{B}$, $^{12/13}\text{C}$, $^{86/87/88}\text{Sr}$, $^{90/91/92/94}\text{Zr}$) has been reported[18,22–25]
17 using conventional nanosecond and femtosecond laboratory instruments involving short
18 focal length lenses.

19 In this work, we introduce a new technology, Femtosecond Filament-Induced Laser
20 Ablation Molecular Isotopic Spectrometry ($\text{F}^2\text{-LAMIS}$), which enables real-time isotopic
21 analysis at remote distances. We demonstrate that the stable filaments generated by high-
22 power, ultrashort laser pulses can be used for stand-off isotopic analysis of Zr, which
23 contains five stable isotopes. The filament-induced plasma characteristics and $\text{F}^2\text{-LAMIS}$

1 spectra were studied as a function of filament propagation distance. Spectral fitting of
2 F^2 -LAMIS spectra was incorporated for semi-quantitative isotopic ratio measurements of
3 Zr as a function of distance.

4 **2. Experimental system**

5 A Ti:Sapphire (800 nm) femtosecond laser system (Mai-Tai oscillator coupled to a TSA-
6 25 amplifier, Spectra Physics) was used for filament generation, delivering 100 fs, 7 mJ
7 pulses at a repetition rate of 10 Hz. Filaments were generated by focusing the
8 femtosecond laser beam with a plano convex lens ($f = 5$ m) (**Fig. 1**). The laser filaments
9 propagated over several meters up to a distance of 7.8 m which was the limit of the
10 available laboratory space. The filament propagation was clearly visible in reduced light
11 conditions, extending over several meters, well beyond the calculated Rayleigh length of
12 the focused laser beam (0.25 m). A schematic of the experimental system is shown in
13 **Fig.1**.

14 A zirconium (Zr) metal plate (99.2%, Alfa Aesar) was used as a sample. The Zr sample
15 was placed on a motorized yz micrometric stage which was mounted on moveable carrier
16 base along an optical rail, which was aligned parallel to the filament propagation
17 direction. The distance between the lens and the sample (filament propagation distance- x)
18 was controlled by translating the carrier on the rail. An iris with variable diameter was
19 placed 5 cm in front the sample to ensure that the alignment was maintained for all
20 sample positions along the rail. The iris remained open (diameter >1 cm) during the
21 emission and acoustic measurements, ensuring that the energy reservoir surrounding the
22 filament core was not blocked or influenced by the iris.[26]

The filament-induced plasma from the Zr sample was imaged onto a collection fiber by using a plano-convex lens ($f=5$ cm). The fiber was connected to the entrance slit of a Czerny-Turner spectrometer (focal length = 1.25 m, Horiba JY 1250M) equipped with an intensified charge-coupled device (ICCD) (PI MAX 1024, Princeton Instruments) for spectral acquisition. The grating of the spectrometer had a groove density of 3600 per mm. The instrumental resolution of the spectrometer was determined as 11.8 pm at 435.8 nm, by using a mercury lamp. An acoustic signal sensor connected to an oscilloscope, was used to record acoustic signals in the filament-induced plasma vicinity. Both the spectral emission collection optics and fiber system, and the acoustic sensor were directly mounted on the sample carrier base, to ensure that the collection remained unaffected as a function of filament propagation distance.

The sample was translated along the vertical axis at a constant translation speed of 0.02 mm/s, thereby forming craters on the Zr plate surface. Following ablation, the three dimensional morphology of the ablated craters was measured by using a white light interferometer (Zygo NewView 6K).

3. Results and discussion

3.1 F²-LAMIS spectra and spectral deconvolution

The spectral range of 461.90 to 463.70 nm was selected for spectroscopic analysis of the filament-induced plasma, covering the $\alpha(0,0)$ band the of $d^3\Delta_3 - a^3\Delta_3$ system of ZrO and four zirconium atomic lines (Zr I 462.64 nm/462.77 nm/463.40 nm/463.46 nm).[25]

Fig.2a shows the plasma spectral emission at a filament propagation distance of 6.8 m. In order to reconstruct the molecular and atomic emission from the acquired spectra, a

1 fitting procedure was implemented (**Fig. 2b**). The observed transitions in diatomic
2 molecules can be calculated by: $\Delta E = E(e', v', J') - E(e'', v'', J'')$, where $E(e, v, J) =$
3 $E_{elc}(e) + E_{vib}(e, v) + E_{rot}(e, v, J)$. E_{elc} , E_{vib} and E_{rot} are the electronic, vibrational
4 and rotational quantum states. The intensity was determined by the transition probability
5 and the population of the excited state $E(e', v', J')$. A detailed description of the fitting
6 procedure can be found in our previous work.[20,25] For the simulation, molecular
7 parameters reported by Kaledin *et al.*[27] were used, and the peak profile of atomic lines
8 was assumed to be a Lorentzian function.

9 Using this fitting procedure, the components of ZrO molecular band and four Zr atomic
10 lines were reconstructed, and are shown together with the experimental spectra in **Fig.2c**.
11 The intensity of the ZrO molecular emission is comparable to the zirconium atomic
12 emission. The rotational structure in the ZrO spectra is clearly resolved. Typical residual
13 (difference between experimental and fitted data) at each wavelength was less than 6%
14 (**Fig.2d**), with a distribution that was independent of wavelength, thereby demonstrating
15 that this fitting procedure allows for high precision molecular band and atomic line
16 component deconvolution.

17 **3.2 Characterization of filament-induced plasmas at different propagation distances**

18 In order to characterize the optical emission of plasmas generated at different filament
19 propagation distances, we studied the intensity variation of the zirconium oxide
20 molecular band ($\alpha(0,0)$ band of the $d^3\Delta_3 - a^3\Delta_3$ system) and the zirconium atomic line
21 (Zr I 462.64 nm). The acoustic signal and excitation temperature also were measured.
22 The vibrational bandhead intensity was used as the emission signal of the ZrO molecules.
23 The atomic and molecular emission intensities, acoustic signals and plasma temperatures

1 as functions of filament propagation distances are shown in **Fig.3**. The intensities of both
2 ZrO and Zr I initially increase with filament propagation distance before reaching a
3 maximum at a distance of 6.8 m. Following that, they gradually decrease to about 70% of
4 the maximal intensity at a filament propagation distance of 7.8 m (**Fig.2a**). Due to
5 limitations in available experimental space, the emission of the plasma generated after
6 7.8 m could not be measured.

7 Acoustic signals provide a versatile method for monitoring the general strength of
8 filament-induced plasma, and have been used in the past to monitor the laser ablation
9 threshold [28] or to correct for shot-to-shot analyte emission variations.[29] Higher
10 acoustic signal typically indicates that stronger plasma is generated. **Fig. 3b** shows the
11 variation of acoustic signal over distance, exhibiting behavior similar to that of the
12 plasma emission intensity. For the plasma excitation temperature measurements as a
13 function of filament propagation distance, we used the two zirconium atomic lines
14 (Zr I 463.40 nm and 462.64 nm) in the Boltzmann Plot method.[30] Unlike emission and
15 acoustic signal intensity, the excitation temperature showed a gradual increase with
16 filament propagation distance (**Fig. 3c**).

17 The variation of atomic and molecular intensity, as well as acoustic signal, as a function
18 of filament propagation distance, can be attributed to two main factors: excitation
19 temperature and ablated mass variation. First, we investigated the dependence of the Zr I
20 line intensity over plasma temperature. Treating the plasma as homogeneous and in
21 thermal equilibrium, we calculated the contribution of temperature variations on the
22 signal intensity. Both the ionization equilibrium, which follows the Saha equation, and
23 the electron population, which follows Boltzmann equilibrium, were used. For an

1 electron density, $n_e = 10^{17} - 10^{18} \text{ cm}^{-3}$, the maximum variation of relative spectral
2 emission intensity (ΔI) of Zr I 462.64 nm at different filament propagation distances,
3 attributed to temperature changes, is: $\Delta I = 27.8 - 28.6\%$. However, the experimental
4 variation of Zr I 462.64 nm intensities as a function of filament propagation distance can
5 be up to 70%, which indicates that the second contributing factor, ablated mass, may vary
6 with filament propagation distance.

7 **Fig.4** shows the depth profiles of filament-ablated craters at four selected propagation
8 distances, which correspond to the optical focal point of the lens (5 m), the half
9 maximum (6.0 m) and maximum (6.8 m) of the plasma emission intensity, and the
10 maximum distance (7.8 m). Each depth profile was obtained by averaging all individual
11 pixels in the white light interferometry three-dimensional sample morphology image.

12 **Fig.4(a)** shows that although the diameters of the craters obtained at the four distances
13 are similar ($\sim 450 \mu\text{m}$), their depths are quite different. Dynamic energy redistribution
14 along the filament path may directly affect the ablation efficiency characteristics. Deepest
15 craters were created at a filament propagation distance of 6.8 m, which indicates that the
16 laser intensity in the filament core was the highest in that position. The ablated volume
17 was measured by spatial integration of the crater profiles, which was in turn used to
18 calculate the relative ablated mass as a function of filament propagation distance (**Fig.4b**).
19 Correlations between the ablated mass and intensities of the Zr I line and ZrO molecular
20 band at different distances are shown in **Fig.3a**.

21 In order to further characterize the emission and physical characteristics of the plasma
22 generated at different filament propagation distances, we studied the temporal behavior of
23 the zirconium atomic emission, ZrO molecular emission and plasma excitation

temperature (**Fig.5**). For the zirconium atomic lines, the intensity decreases with time, a behavior which is commonly observed in laser induced plasmas. In contrast, the molecular emission intensity initially increases with delay time and reaches its maximum at 500 ns, following which, it decays with time. The different behavior between the atomic and molecular emission may be attributed to the fundamentally different plasma conditions that are required for ZrO molecule formation via the combination of zirconium and oxygen atoms. Figs. 5a and 5b show that both Zr I line and ZrO band emissions were stronger at distances over 6.0 m than those at 5.0 m. The plasma generated at the lens focal distance (5.0 m) has slightly lower temperature compared to that of the plasma generated at 6.0, 6.8 and 7.8 m. The temporal evolution of the excitation temperature for the plasmas generated at 6.8 and 7.8 m is very similar for all detection gate delays, in agreement with the temporally integrated mean excitation temperature shown in **Fig.3**.

3.3 Isotopic analysis with F²-LAMIS

The zirconium sample used in this work had natural isotopic abundance (⁹⁰Zr:⁹¹Zr:⁹²Zr:⁹⁴Zr:⁹⁶Zr=2.96:0.65:0.99:1:0.16).[31] Our previous report[25] showed that isotopic information can be obtained by analyzing the (0,1) and (1,0) ZrO molecular bands of $E^1\Sigma^+ - X^1\Sigma^+$ and $d^3\Delta - a^3\Delta$ systems and that the $\alpha(0,1)$ band of the $d^3\Delta_3 - a^3\Delta_3$ system is optimal for zirconium isotopic analysis. **Fig.6a** shows the typical spectra acquired at filament distances of 5.0, 6.0, 6.8 and 7.8 m. The ICCD gate delay and gate width were 3 μ s and 20 μ s respectively, and were optimized in order to improve the signal-to-noise ratio of the isotopic signatures. Molecular band intensities and interferences from nearby zirconium atomic and ionic lines were taken into account

during the optimization process. As shown in **Fig.6a**, four different isotopic zirconium oxide molecular bands, i.e. ^{90}ZrO , ^{91}ZrO , ^{92}ZrO and ^{94}ZrO , were clearly resolved. The molecular band of ^{96}ZrO could not be assigned with certainty due to the low concentration of ^{96}Zr in the sample that results in a weak emission line. The weak ^{96}ZrO is, in addition, interfered with noise and rotation structure of other molecular bands nearby.[32] The ratio of zirconium isotopes can be deduced by fitting of experimental to the theoretical spectra of the $\alpha(0,1)$ band of the $d^3\Delta_3 - a^3\Delta_3$ system, as demonstrated in our previous work.[25] **Fig.6b** shows the deduced isotope ratios of $^{90}\text{Zr}/^{94}\text{Zr}$, $^{91}\text{Zr}/^{94}\text{Zr}$ and $^{92}\text{Zr}/^{94}\text{Zr}$ as a function of filament propagation distance. Although these isotope ratios deviate from the true isotopic composition of the sample, each isotope ratio remains fairly constant with filament propagation distance. As with any analytical technique, more accurate quantitative analysis is expected with the use of standard samples for calibration. These results indicate that the influence of the filament propagation distance on quantification is minimal, and that F²-LAMIS can be a powerful and versatile technology for remote semi-quantitative isotopic analysis.

4. Conclusions

We introduced a new laser technology, F²-LAMIS, which enables all-optical isotope analysis at remote distances, through the combination of fs laser filamentation and ablation-based molecular isotopic spectroscopy. We demonstrated the first experimental measurement of isotopes with F²-LAMIS at distances up to 7.8 m. The plasma properties and the dependence of both molecular and atomic Zr emission over filament propagation distance were investigated. Spectral fitting of F²-LAMIS spectra allowed semi-quantitative

1 isotopic ratio analysis, thereby minimizing the need for standards. This spectral-fitting
2 approach is also applicable to other elements. For example, molecular bands with
3 appreciable isotope shifts have been experimentally observed for boron and carbon. This
4 technology, combined with a large diameter telescope for collection of plasma emission,
5 can be used for isotopic analysis at remote distances, in applications ranging from nuclear
6 non-proliferation to environmental research. For standoff plasma ablation, femtosecond
7 laser filament offers an advantage over nanosecond laser in delivering laser energy with
8 high fluence. A major challenge for determination at extended standoff distances is
9 collection of plasma emission as the solid angle of light collection decreases in a
10 quadratic fashion to the distance between the plasma and telescope. One possible
11 solution to improve the standoff plasma emission collection efficiency is through the use
12 of the filament self-created long-lived optical waveguides,[33] in which lifetimes were
13 reported to be up to millisecond; clearly, more work needs to be done to evaluate such
14 possibility and its performance.

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Figure Captions

Fig. 1 Schematic diagram of the F²-LAMIS experimental setup.

Fig. 2 (a) Typical F²-LAMIS spectrum acquired from the Zr target at a filament propagation distance of 6.8 m. (b) The molecular band and atomic lines were reconstructed through a fitting procedure. (c) Fitted and experimental spectra. The fitting residual is shown in (d). The ICCD gate delay and gate width were set at 1.5 μ s and 10 μ s, respectively.

Fig. 3 Variations of the emission intensity of the ZrO molecular bandhead and Zr I 462.64 nm (a), acoustic signal (b), and plasma excitation temperature (c) as a function of filament propagation distance. The error bar represents the standard deviation of 10 separate measurements. Each measurement is an accumulation of 64 laser shots. For spectral acquisition, the ICCD gate delay and gate width were set at 1.5 μ s and 10 μ s, respectively.

Fig. 4 (a) Femtosecond filament ablated craters on the zirconium metal target at different filament propagation distances (5.0, 6.0, 6.8 and 7.8 m), and (b) comparison of the relative ablated mass. The sample translation speed was 0.02 mm/s.

Fig. 5 Temporal evolution of the (a) Zr I 462.64 nm intensity, (b) ZrO molecular band head intensity and (c) excitation temperature of plasmas generated at filament propagation distances of 5.0, 6.0, 6.8 and 7.8 m.

Fig. 6 (a) Typical spectra of the ZrO $\alpha(0,1)$ band of the $d^3\Delta_3 - a^3\Delta_3$ system obtained at different filament propagation distances. The ICCD gate delay was 3 μ s and the gate width was 20 μ s. Each spectrum was the average of 500 laser shots. (b) Deduced atomic ratios of $^{90}\text{Zr}/^{94}\text{Zr}$, $^{91}\text{Zr}/^{94}\text{Zr}$ and $^{92}\text{Zr}/^{94}\text{Zr}$ as a function of filament propagation distance. Error bars represent the standard deviation of 10 measurements.

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Fig. 4 (a) Femtosecond filament ablated craters on the zirconium metal target at different filament propagation distances (5.0, 6.0, 6.8 and 7.8 m), and (b) comparison of the relative ablated mass. The sample translation speed was 0.02 mm/s.

Fig. 5 Temporal evolution of the (a) Zr I 462.64 nm intensity, (b) ZrO molecular band head intensity and (c) excitation temperature of plasmas generated at filament propagation distances of 5.0, 6.0, 6.8 and 7.8 m.

Fig. 6 (a) Typical spectra of the ZrO $\alpha(0,1)$ band of the $d^3\Delta_3 - a^3\Delta_3$ system obtained at different filament propagation distances. The ICCD gate delay was 3 μ s and the gate width was 20 μ s. Each spectrum was the average of 500 laser shots. (b) Deduced atomic ratios of $^{90}\text{Zr}/^{94}\text{Zr}$, $^{91}\text{Zr}/^{94}\text{Zr}$ and $^{92}\text{Zr}/^{94}\text{Zr}$ as a function of filament propagation distance. Error bars represent the standard deviation of 10 measurements.