HYDRATE BEARING CLAYEY SEDIMENTS: FORMATION AND GAS PRODUCTION CONCEPTS

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Abstract

Hydro-thermo-chemo and mechanically coupled processes determine hydrate morphology and control gas production from hydrate-bearing sediments. Force balance, together with mass and energy conservation analyses anchored in published data provide robust asymptotic solutions that reflect governing processes in hydrate systems. Results demonstrate that hydrate segregation in clayey sediments results in a two-material system whereby hydrate lenses are surrounded by hydrate-free water-saturated clay. Hydrate saturation can reach $\approx 2\%$ by concentrating the excess dissolved gas in the pore water and $\approx 20\%$ from metabolizable carbon. Higher hydrate saturations are often found in natural sediments and imply methane transport by advection or diffusion processes. Hydrate dissociation is a strongly endothermic event; the available latent heat in a reservoir can sustain significant hydrate dissociation without triggering ice formation during depressurization. The volume of hydrate expands 2-to-4 times upon dissociation or CO_2 - CH_4 replacement. Volume expansion can be controlled to maintain lenses open and to create new open mode discontinuities that favor gas recovery. Pore size is the most critical sediment parameter for hydrate formation and gas recovery and is controlled by the smallest grains in a sediment. Therefore any characterization must carefully consider the amount of fines and their associated mineralogy.

26	<u>Notation</u>	
27	α	metabolizable carbon content
28	α_g	ratio of $\rho_g c_g$ to $\rho_w c_w$, $\alpha_g = \rho_g c_g / \rho_w c_w$
29	α_h	ratio of $\rho_h c_h$ to $\rho_w c_w$, $\alpha_h = \rho_h c_h / \rho_w c_w$
30	α_m	ratio of $\rho_m c_m$ to $\rho_w c_w$, $\alpha_m = \rho_m c_m / \rho_w c_w$
31	β	ratio of carbon molecular mass to methane molecular mass
32	β_h	ratio of $\rho_h L_h$ to $\rho_w c_w$, $\beta_h = \rho_h L_h / \rho_w c_w$
33	β_l	ratio of $\rho_w L_l$ to $\rho_w c_w$, $\beta_l = L_l / c_w$
34	δ	thickness of hydrate lens
35	η	fluid volume expansion after hydrate dissociation
36	θ	contact angle
37	κ	volume fraction of segregated hydrate
38	λ	mole of methane per unit volume of hydrate
39	ρ_{CH_4-G}	methane gas density
40	ρ_{CO_2-G}	gaseous carbon dioxide density
41	ρ_{CO_2-L}	liquid carbon dioxide density
42	ρ_g	gas density
43	ρ_h	hydrate density
44	ρ_m	mineral density
45	ρ_w	water density
46	ρ_{w_hyd}	water mass in unit volume of hydrate
47	σ'	effective stress
48	$\square$	fraction of fines in sediment
49	χ	hydration number (e.g., $CH_4 \cdot \chi H_2O$ or $CO_2 \cdot \chi H_2O$)
50	ω	compressibility factor
51	γ_{hw}	interfacial tension between hydrate and water
52	γ_s	sediment unit weight
53	γ_w	water unit weight
54	c_g	specific heat of gas
55	c_h	specific heat of hydrate
56	c_m	specific heat of mineral
57	c_w	specific heat of water
58	C_A	solubility of methane in water after hydrate formation
59	C_B	solubility of methane in water before hydrate formation
60	C_C	sediment compressibility
61	C_H	methane concentration per kg of hydrate
62	d_{pore}	pore diameter
63	e	void ratio
64	e_c	void ratio of coarse particles
65	e_f	void ratio of fine particles
66	e_{100}	void ratio at $\sigma' = 100 \text{ kPa}$
67	E_{DIS}	energy needed to dissociate hydrate
68	E_{HBS}	sensible energy available in sediment before hydrate dissociation
69	FR_{WI}	fraction of ice formed during hydrate dissociation
70	G_s	specific gravity of minerals
71	ΔH	enthalpy

72	k_H^o	Henry's constant
73	m_h	molecular weight of gas hydrate
74	L	lens-to-lens spacing
75	L_H	transformation heat of hydrate
76	L_I	transformation heat of ice
77	M_C	mass of metabolizable carbon
78	M_{CH_4}	methane mass
79	M_F	mass of fine particles
80	M_H	hydrate mass
81	M_M	mineral mass
82	$M_{P,T}$	gas concentration in water under pressure P and temperature T condition
83	M_T	mass of sediment composed of coarse and fine particles
84	n	porosity
85	n_0	initial porosity of sediment before hydrate formation
86	n_f	final porosity of sediment after hydrate segregation
87	n_{CH_4-H}	mole of methane in CH_4 hydrate
88	P	pressure
89	P_C	capillary pressure
90	P_H	pressure inside hydrate
91	P_F	final pressure after hydrate dissociation
92	P_0	initial pressure before hydrate dissociation
93	P_W	water pressure
94	R	universal gas constant
95	S_H	hydrate saturation
96	S_s	specific surface
97	S_w	water saturation
98	T_{Bulk}	hydrate formation/dissociation temperature in bulk water
99	T	temperature
100	T_o	initial temperature before hydrate dissociation
101	T_F	final temperature after hydrate dissociation
102	T_T	temperature of hydrate phase boundary
103	ΔT_{dep}	hydrate formation/dissociation temperature depression in small pores
104	ΔT_{HW}	temperature change of water by the energy equivalent to dissociate the same
105		mass of hydrate
106	ΔT_{IW}	temperature change of water by the energy equivalent to melt the same mass
107		of ice
108	V_{CH_4-G}	volume of CH_4 gas
109	V_{CH_4-H}	volume of CH_4 hydrate
110	V_{CO_2-H}	volume of CO_2 hydrate
111	V_{CO_2-L}	volume of liquid CO_2
112	V_G	gas volume
113	V_H	hydrate volume
114	V_T	total sediment volume
115	V_V	volume of voids
116	V_W	water volume
117	z	depth

1. INTRODUCTION

Fine-grained sediments host more than 90% of the accumulated global gas hydrate [Boswell 2009; Boswell and Collett 2011]. Well known accumulations of hydrate-bearing clayey sediments include those in the Gulf of Mexico, Krishna-Godavari basin, Blake Ridge, Cascadia Margin, Ulleung Basin, and Hydrate Ridge [Dai et al 2011]. Hydrates in all these cases are found as segregated masses forming features such as lenses and nodules.

Hydro-thermo-chemo-mechanically coupled processes that occur during hydrate formation and dissociation affect the spatial distribution of hydrate in sediments and also control gas production during depressurization, heating and CO₂-CH₄ replacement.

Hydrate formation and dissociation in clayey sediments is strongly affected by pore size. The sediment porosity n decreases with sediment depth due to self compaction. In terms of void ratio $e=n/(1-n)$, the sedimentation compression curve can be expressed as a function of the overburden effective stress σ' [Burland 1990; Skempton 1969; Terzaghi and Peck 1948]:

$$e = e_{100} - C_C \log\left(\frac{\sigma'}{100 \text{ kPa}}\right) \quad (1)$$

where e_{100} is the void ratio at $\sigma'=100\text{kPa}$ and C_C is the sediment compressibility. The two constitutive parameters e_{100} and C_C increase with the sediment specific surface S_s [m²/g]. However, the change in vertical effective stress $d\sigma'$ between depths z and $z+dz$ depends on the sediments saturated unit weight $\gamma_s = \gamma_w(G_s+e)/(1+e)$

$$d\sigma' = (\gamma_s - \gamma_w)dz = \gamma_w \frac{(G_s - 1)}{(1 + e)} dz \quad (2)$$

where γ_w is the unit weight of water and G_s is the specific gravity of minerals that make the grains. Equations 1&2 are combined and integrated with depth to compute the depth varying overburden effective stress and void ratio (hence, porosity).

The mean pore size d_{pore} can be estimated from the void ratio e , specific surface S_s [m²/g] and the mineral mass density ρ_m :

$$d_{pore} = \frac{4e}{S_s \rho_m} \quad (3)$$

For reference, the mean pore size for kaolinite one meter below the seafloor, $z=1\text{mbsf}$, is $d_{pore} \approx 200\text{nm}$ ($e_{100}=1.04$, $C_c=0.35$, $S_s=10\text{m}^2/\text{g}$), while the mean pore size for bentonite at $z=1000\text{mbsf}$ is $d_{pore} \approx 5\text{nm}$ ($e_{100}=3.2$, $C_c=1.2$, $S_s=300\text{m}^2/\text{g}$). Small pore size in clayey sediments affects gas solubility, the phase boundary, hydrate morphology and the properties of the hydrate bearing sediments.

The purpose of this study is to review the fundamental concepts relevant to hydrate formation in clayey sediments and to explore potential phenomena pertinent to gas production. We analyze coupled pore-scale phenomena and present simple yet robust asymptotic expressions to obtain order-of-magnitude estimates that can aid in the understanding of hydrate bearing clayey sediments and guide the design of gas production strategies. The replacement of CH_4 with CO_2 is a possible production alternative; hence, parameters relevant to CO_2 solubility and phase boundaries are reported in parallel to parameters for CH_4 .

2. PHASE BOUNDARY AND GAS SOLUBILITY

Pressure and temperature affect the composition of the hydrate mass. The CH_4 molecule is smaller than CO_2 and fits more easily into the two small cages in Structure I hydrate. Thus, the stoichiometric ratio for CH_4 hydrate ($\chi=5.8\text{-to-}6.0$) is closer to the theoretical value $\chi=46/8=5.75$ and is less sensitive to pressure than the stoichiometric ratio of CO_2 hydrate ($\chi \sim 6.6$ at 1.3MPa and decreases to $\chi < 6$ at 4.5MPa) [Anderson *et al* 2003; Circone *et al* 2003; Jung *et al* 2010; Klapproth *et al* 2003]. More importantly, pressure and temperature define the stability field and gas solubility. The role of small pores in fine grained sediments and competing solutes on the phase boundary and gas solubility are reviewed next in relation to hydrate formation in clayey sediments.

2.1 Phase Boundary

The hydrate phase boundary is affected by several factors that alter molecular activity, e.g, the interaction with mineral surfaces and the presence of other ions and molecules, including salts and mixed gases.

Pore size effects. Small hydrate nuclei are in equilibrium with the pore fluid at higher gas concentrations than the concentration around larger hydrate crystals, known as the Gibbs-Thomson effect. Therefore, hydrate experiences formation/dissociation (or phase transformation) and temperature depression ΔT_{dep} for small pores sizes d_{pore} [Anderson *et al* 2003; Kwon *et al* 2008],

$$\Delta T_{dep} = -\frac{4}{d_{pore}} \left(\frac{\gamma_{hw} m_h \cos \theta}{\rho_h L_H} \right) T_{bulk} \quad (4)$$

where the variables are the hydrate-water interfacial tension γ_{hw} [N/m], the molecular weight of gas hydrate m_h [g/mol], the contact angle θ , the hydrate mass density ρ_h [kg/m³], the heat of hydrate dissociation L_H [kJ/kg], and hydrate formation/dissociation temperature in bulk water T_{Bulk} [K]. Tables 1 and 2 summarize typical values for these parameters.

Figures 1a&b present a compilation of measured temperatures during CH₄ and CO₂ hydrate formation/dissociation. The phase boundaries for hydrate in bulk water are obtained from experimentally validated thermodynamic models [Duan and Sun 2003; Jung *et al* 2010; Sun and Duan 2005]. Trends predicted by the Gibbs-Thomson equation (Equation 4) are superimposed on the figure. We can conclude that pore size effects vanish when pores are larger than $d_{pore} \sim 100\text{nm}$. The Gibbs-Thompson equation combines with the effective stress dependent pore size (Equations 1-through-4) to anticipate deviations in the stability field in deep clayey sediments [Dai *et al* 2011; Henry *et al* 1999].

Salinity effects. The Coulombic attraction between water molecules and ions is stronger than the attraction between the water molecules and the guest molecule in gas hydrate. Therefore, substantial sub-cooling is required to cause hydrate to form in salt water [Dickens and Quinby-Hunt 1997; Sloan and Koh 2008].

Mixed gases. The phase boundary for hydrate made from mixed methane and carbon dioxide lies between the boundaries for pure CH₄ and CO₂ hydrates. The relative position scales with the mixture ratio as shown in Figure 2 [Adisasmito *et al* 1991; Seo and Lee 2001]. The CO₂ hydrate boundary shifts to higher pressures even with small amounts of CH₄ [Donnelly and Katz 1954; Sloan and Koh 2008]. Note that the stability of CH₄ hydrate requires higher pressures than CO₂ hydrate for temperatures $T \leq 283.67\text{K}$. However, this is not the case at higher temperatures. In-situ methane hydrate bearing sediments are typically encountered under Pressure-Temperature (PT) conditions such that (1) CO₂ injection will be in the liquid phase and (2) any free water would usually form CO₂ hydrate (gas-limited reservoirs). This situation is revisited later in the context of gas production from hydrate bearing clayey sediments.

2.2 Gas Solubility

Gas solubility in water in the absence of hydrates. The pressure and temperature PT dependent gas concentration in water $M_{P,T}$ [mol/m³] can be approximated using Henry's law as a linear function of pressure P :

$$M_{P,T} = P k_H^0 \cdot \exp\left[\frac{-\Delta H}{R} \left(\frac{1}{T} - \frac{1}{298.15\text{K}}\right)\right] \quad \text{in bulk and without hydrates} \quad (5)$$

where k_H^0 is Henry's constant, T is temperature, ΔH is the enthalpy of the solution, and the universal gas constant is $R=8.314 \text{ J}/(\text{mol}\cdot\text{K})$. Typical values for CH₄ in water are $\Delta H=-14130 \text{ J/mol}$ and $k_H^0=1.3\times 10^{-3} \text{ M/atm}$ at 298.15K. These parameters for CO₂ in water are $\Delta H=-19940 \text{ J/mol}$ and $k_H^0=3.4\times 10^{-2} \text{ M/atm}$ at 298.15K [Osegovic *et al* 2006; Wilhelm *et al* 1977]. Hence, the solubility of CH₄ and CO₂ in water rises with increasing pressure and decreasing temperature.

Gas solubility in the presence of hydrates. The presence of hydrates stimulates the formation of additional hydrates. Hence the presence of hydrates results in a decrease in the equilibrium concentration of gas in water. In fact, gas solubility trends within the hydrate stability field and in the presence of hydrates are the opposite to trends outside the stability field. Therefore lower temperatures or higher pressures prompt additional hydrate formation and reduces the gas concentration in water [Lu *et al* 2008; Waite *et al* 2009].

Pore size effects. Gas solubility in water increases with decreasing pore size due to the lower water activity in small pores [Henry et al 1999; Sun and Duan 2007].

Competing solutes. Hydrated ions reduce the average mobility of water molecules. Therefore, the solubility of gas in water decreases inversely proportional to salt concentration [Davie et al 2004; Sun and Duan 2007; Tishchenko et al 2005; Zatsepina and Buffett 1998]. Likewise, coexisting gases compete for available cavities between water molecules and restrict each others solubilities [Qin et al 2008].

Summary: General Trends. Published solubility data and additional values computed with solubility calculators can be summarized as follows [Donnelly and Katz 1954; Duan and Sun 2003; Duan and Mao 2006; Folas et al 2007; Hashemi et al 2006; Henry et al 1999; Jung et al 2010; Servio and Englezos 2001; 2002; Sun and Duan 2007]:

- Before hydrate formation, the solubility of CH₄ in water is $C_B \sim 0.08$ -to- 0.20 mol/kg (for PT conditions $P < 25$ MPa and $T < 15^\circ\text{C}$). The solubility of CO₂ in water is an order of magnitude higher than that of CH₄ for the same PT conditions.
- By comparison, the methane concentration per kg of hydrate is $C_H = 8.06$ mol/kg, that is 40-to-100 times higher than the concentration in water.
- The solubility of gas in water after hydrate formation is approximately half of the solubility of gas in water in the absence of hydrate, for PT conditions common to seafloor hydrate accumulations of interest.
- Methane solubility in seawater is approximately $\sim 0.93 \pm 0.03$ of the methane solubility in fresh water. This ratio is similar in the presence or absence of hydrates.
- Methane solubility in 10nm small pores can be 1.2 times higher than the solubility of methane in bulk water (Sun and Duan 2007. Note: Henry et al. 1999 used less accurate factors and obtained an even higher solubility in small pores).

It follows from the these observations that the pore fluid in clayey sediments can sustain a gas saturation 2-to-2.5 times higher before hydrate is formed than after hydrate formation occurs.

3. HYDRATE FORMATION IN CLAYEY SEDIMENTS

3.1 Morphology

Force equilibrium requires that the capillary pressure inside hydrate lenses $P_C = P_H - P_W$ $= 4\gamma_{hw}\cos\theta/d_{pore}$ balances the pressure in the water p_w and the effective stress acting on the grain skeleton σ' [Clennell *et al* 1999; Santamarina and Jang 2010]

$$\sigma' = \frac{4\gamma_{hw}\cos\theta}{d_{pore}} \quad \text{condition for hydrate lens} \quad (6)$$

where d_{pore} is the pore diameter in the sediment, the contact angle can be assumed to be $\theta=0^\circ$ and the hydrate-water interfacial tension is $\gamma_{hw}=0.035$ N/m [Uchida *et al* 1999]. Equation 6 combines with Equation 3 and the integral form of Equation 2 to predict that hydrate will displace grains, segregate and form hydrate lenses or nodules in the upper 0.5m depth in silt sediments, to a depth of 1500m in kaolinite, and much deeper in illite and montmorillonite (see compilation of field data in Dai *et al.* [2012]). Consequently, hydrate bearing clayey sediments are two-material systems made of segregated hydrate lenses or nodules that are surrounded by hydrate-free water-saturated clay. Effective media properties must be evaluated accordingly.

3.2 Hydrate Volume Fraction from Initial Excess Gas (*at constant mass*)

Hydrate lenses may form in the absence of advection or diffusion (i.e., in a closed system). This occurs by concentrating the “excess gas” between the solubility of gas in water in the absence of hydrate (enhanced in small pores) and the lower solubility of gas in water after hydrate formation. Consider a water-saturated clayey sediment at an initial porosity n_o and gas concentration C_B before hydrate formation. After hydrate formation, the concentration of gas in water drops to C_A and the surrounding sediments compact to the final porosity n_f as a result of cryosuction (Figure 3). Mass conservation equations for water, gas and mineral species combine to predict the volume fraction of segregated hydrate κ and the final porosity n_f of the surrounding clay mass:

$$\kappa = \frac{V_H}{V_T} = \frac{C_B - C_A}{C_H - C_A} n_0 \approx \frac{C_B - C_A}{C_H} n_0 \quad \text{hydrate volume fraction} \quad (7)$$

$$n_f = \frac{n_0 - \kappa}{1 - \kappa} \quad (8)$$

288 where C_H is the gas concentration in hydrate. In relation to hydrate saturation S_H ,

$$S_H = \frac{V_H}{V_T} = \frac{\kappa}{n_0} \approx \frac{C_B - C_A}{C_H} \quad \text{hydrate saturation} \quad (9)$$

289 For example, consider two clayey sediments under a pore fluid pressure of 20MPa. The
 290 first case is a kaolinite sediment at 50mbsf with an initial porosity $n_o=0.45$ and mean pore
 291 size $d_{pore}=120\text{nm}$. The gas concentration before hydrate formation is $C_B \approx 0.18\text{mol/kg}$; under
 292 closed conditions, this sediment can develop an initial volume fraction of segregated
 293 hydrate $\kappa=0.6\%$ which corresponds to a hydrate saturation $S_H=1.4\%$. The surrounding
 294 sediment will experience a minor densification from $n_o=0.45$ to $n_f=0.447$.

295

296 The second case is a montmorillonitic deposit at 250mbsf, with $n_o=0.66$ and $d_{pore}=10\text{nm}$.
 297 Under these conditions, it can accumulate 1.5 times higher gas concentration before hydrate
 298 formation, $C_B=1.5C_A$, and it can form an initial volume fraction of segregated hydrate
 299 $\kappa=1.7\%$ or $S_H=2.2\%$. The surrounding sediment would compact from an initial porosity
 300 $n_o=0.660$ to a final porosity $n_f=0.655$.

301

302 These two end member clayey sediments (within PT ranges of interest) allow us to
 303 conclude that the volume fraction or saturation of segregated hydrate in lenses or nodules
 304 could reach $S_H \approx 1.4\%$ to 2.2% only when the excess dissolved gas is used in hydrate
 305 formation.

306

307 **3.3 Hydrate Volume Fraction from Available Organic Carbon (*at constant mass*)**

308 Hydrate may also form using methane produced by organic mass trapped in the sediment.
 309 The sediment in this case is both the source deposit and the reservoir. The maximum
 310 amount of hydrate that can form is a function of (1) the initial “metabolizable” carbon
 311 content $\alpha = M_C/M_M$, where M_M is the mineral mass and M_C is metabolizable carbon mass,

and (2) the ratio $\beta=M_{CH4}/M_C$ between the generated methane mass M_{CH4} and the original mass of metabolizable carbon M_C , i.e., the ratio of their molar masses $\beta=16/12$ (see detailed discussion in *Malinverno* [2010], and earlier analyses by *Paull et al.* [1994], *Davie and Buffett* [2001], *Bhatnagar et al.* [2007]). Then, the attainable hydrate saturation is:

$$\begin{aligned}
 S_H &= \frac{V_H}{V_V} = \frac{M_H}{\rho_h V_V} = \frac{\frac{120}{16} M_{CH4}}{\rho_h V_V} = \frac{\frac{120}{16} \alpha \cdot \beta \cdot M_M}{\rho_h V_V} \\
 &= \frac{120}{16} \alpha \cdot \beta \cdot \frac{1-n_0}{n_0} \frac{\rho_m}{\rho_h} \\
 &= 10 \alpha \frac{1-n_0}{n_0} \frac{\rho_m}{\rho_h} \approx 28 \alpha \frac{1-n_0}{n_0}
 \end{aligned} \tag{10}$$

where the ratio between the mineral and hydrate mass densities is $\rho_m/\rho_h \approx 2.8$. From Equations 7 and 9, the volume fraction of segregated hydrate κ is obtained from the hydrate saturation and the initial porosity $\kappa=S_H n_0$.

Reported hydrate saturations can reach $S_H=20-30\%$ in fine-grained sediments ($S_H=18.2\%$ in the Krishna-Godavari Basin - *Yun et al.* [2010]; $S_H=19.5\%$ in the Ulleung Basin - *Yun et al.* [2011]). This would require an initial metabolizable carbon content $\alpha \approx 0.5\%$, an unlikely situation in the field [*Paull et al.* 1994]. Limited bioactivity in the small pores of fine-grained sediments further aggravates this situation [*Phadnis and Santamarina* 2011; *Rebata-Landa and Santamarina* 2006].

In summary, the results from the two previous analyses of hydrate volume fraction formed in closed systems (from solution and from organic matter) imply that some high hydrate concentrations $S_H > 20\%$ found in the field have involved diffusive and/or advective methane transport.

4. ANALYSES RELEVANT TO GAS PRODUCTION

Gas may be produced from hydrate bearing sediments by combinations of depressurization, thermal stimulation or chemical injection. First order analyses are conducted in each case to assess the implications to potential recovery strategies.

4.1. Depressurization: Available Heat and Ice Formation

Depressurization is an unlikely production mechanism in fine-grained sediments as the permeability would be reduced due to the increase in effective stress. Yet, depressurization can be used in combination with other methods to develop optimal production strategies.

Hydrate dissociation is highly endothermic (relevant properties are summarized in Table 2). Notably, the energy density required to dissociate methane hydrate $\rho_h L_H$ is equivalent to the energy $\rho_w c_w \Delta T_W$ required to heat water by $\Delta T_{HW}=96^\circ\text{C}$. For comparison, the energy density required to melt ice $\rho_i L_I$ is equal to the energy required to heat the same mass of water by a temperature change $\Delta T_{IW}=73^\circ\text{C}$.

Endothermic hydrate dissociation may hinder gas production if secondary ice or hydrate forms along flow paths [Moridis *et al* 2011b]. During adiabatic conditions the heat for dissociation must be supplied by the sensible heat within the hydrate-bearing sediment. The initial temperature T_0 and pressure P_0 conditions are inside the hydrate stability field (Figure 4a). The system PT conditions cross the phase boundary at temperature T_T , and reaches the final pressure P_F at a final temperature T_F . The sensible heat E_{HBS} that is available in the volume V_T of the hydrate-bearing sediment is a function of the available heat in the mineral, water, gas, hydrate and the energy produced by ice formation

$$\begin{aligned} E_{HBS} = & V_T \left[(1-n) \rho_m c_m (T_0 - T_F) + n(1-S_H) \rho_w c_w (T_0 - T_F) + n S_H \rho_h c_h (T_0 - T_T) \right] \\ & + V_T \left[0.8 n S_H \rho_w c_w (T_T - T_F) + n S_H \rho_g c_g (T_T - T_F) \right] \\ & + V_T \left[n(1-S_H) + 0.8 n S_H \right] \rho_w L_I F R_{WI} \end{aligned} \quad (11)$$

where n is the porosity of the sediment, and the densities of the mineral, water, hydrate, and gas are ρ_m , ρ_w , ρ_h , and $\rho_g=16\rho_h/119.5$ [kg/m³]. Their specific heats are c_m , c_w , c_h , and c_g [kJ/kg·°C]. The term FR_{WI} represents the fraction of the total water converted into ice (the summation of the initial water and the water produced from hydrate dissociation).

However, the energy needed to dissociate hydrate E_{DIS} is a function of the total sediment volume V_T , porosity n , hydrate saturation S_H , hydrate density ρ_h , and the latent heat of hydrate dissociation L_h ,

$$E_{DIS}=V_T n S_H \rho_h L_H \quad (12)$$

There is no ice formation when the final temperature of the sediment is above the nominal $T_f=0^\circ\text{C}$, i.e., there is no heat from ice formation and the third term in Equation 11 is removed. Then, the maximum initial hydrate saturation S_h that does not cause ice formation during adiabatic hydrate dissociation is obtained by setting Equation 11 equal to Equation 12 and $T_f=0^\circ\text{C}$

$$S_H = \frac{(1-n)\alpha_m T_0 + nT_0}{n\beta_h + nT_0 - n\alpha_h(T_0 - T_T) - 0.8nT_T - n\alpha_g T_T} \quad (T_o \text{ and } T_i \text{ in } ^\circ\text{C}) \quad (13)$$

where the density times the specific heat of species pc is normalized by the corresponding value for water $\rho_w c_w$, so that $\alpha_m=\rho_m c_m/\rho_w c_w$, $\alpha_h=\rho_h c_h/\rho_w c_w$, and $\alpha_g=\rho_g c_g/\rho_w c_w$. The same normalization is enforced for the product of the hydrate density and the latent heat of dissociation $\beta_h=\rho_h L_H/\rho_w c_w$. For example, Equation 13 anticipates that ice would not form when the initial hydrate saturation is $S_H=9\%$ in a reservoir at the initial temperature $T_0=5^\circ\text{C}$, $S_H=17\%$ when $T_0=10^\circ\text{C}$, $S_H=25\%$ when $T_0=15^\circ\text{C}$, or $S_H=32\%$ when $T_0=20^\circ\text{C}$. These results correspond to a sediment porosity $n=0.4$ and transformation temperature $T_T=2.5^\circ\text{C}$; other parameters are in Table 2.

The fraction of ice FR_{wi} formed during hydrate dissociation when the hydrate saturation exceeds values predicted by Equation 13 is obtained by combining Equations 11 and 12:

$$FR_{WI} = \frac{nS_H\beta_h - (1-n)\alpha_m(T_0 - T_F) - n(1-S_H)(T_0 - T_F) - nS_H\alpha_h(T_0 - T_T) - 0.8nS_H(T_T - T_F) - nS_H\alpha_g(T_T - T_F)}{[n(1-S_H) + 0.8nS_H]\beta_i}$$

(14)

where β_l is the ratio of the heat of transformation of water to the specific heat of water
 $\beta_l = L_l / c_w$.

Figure 4b shows the fraction FR_{WI} of the total water converted into ice as a function of hydrate saturation S_H for reservoirs at different initial temperatures T_0 . All the water freezes when the initial hydrate saturation is $S_H \approx 0.78$ in a reservoir with initial temperature $T_0 = 5^\circ\text{C}$. These results highlight the advantages of deeper and warmer reservoirs, and are in agreement with observations based on complex reservoir simulators [Anderson et al 2011; Moridis et al 2011a].

4.2. Heating: Volume Change

The volume of hydrate V_H expands into a significantly larger volume of water and gas $V_W + V_G$ upon dissociation for PT conditions that are relevant to the marine hydrate accumulations currently under consideration. A simple expression for the fluid expansion $\eta = (V_G + V_W) / V_H$ is calculated using a modified ideal gas law $PV = \omega nRT$

$$\begin{aligned}
 \eta &= \frac{V_G + V_W}{V_h} \\
 &= \frac{\omega \lambda RT}{P} + \frac{18\chi}{16+18\chi} \frac{\rho_h}{\rho_w} \\
 &= \frac{\omega \lambda RT}{P} + \frac{18\chi}{16+18\chi} \frac{\rho_h}{\rho_w} \\
 &\approx 0.057 \left[\frac{\text{MPa}}{\text{K}} \right] \frac{T}{P} + 0.79
 \end{aligned} \tag{15}$$

The last approximation is obtained by setting the “compressibility factor” $\omega \approx 0.95$ to adjust the ideal gas law to the Peng-Robinson equation within the P - T range of interest, the amount of methane per unit volume of hydrate $\lambda \approx 7.37 \times 10^3 \text{ mol/m}^3$, the hydration number $\chi \approx 6$, the universal gas constant $R = 8.314 \text{ J/(mol}\cdot\text{K)}$, and the mass density ratio $\rho_h / \rho_w \approx 0.91$. For example, the volume of hydrate will expand $\eta = 4.0$ times just to cross the phase boundary during dissociation for $P_W = 5 \text{ MPa}$ and $T_T = 279.4 \text{ K}$; similarly, the expansion will be $\eta = 2.4$ times for $P_W = 10 \text{ MPa}$ and $T_T = 285.6 \text{ K}$. Clearly, further depressurization away from the phase boundary will lead to additional gas expansion. Note: capillary pressure is not

taken into consideration because we assume that gas produced from segregated hydrate will be found in relatively large open pores and discontinuities.

Fluid attempts to expand during dissociation; at the same time the small pores in clayey sediments hinder gas expansion. Consequently, widespread gas-driven fractures will develop in hydrate bearing clayey sediments during thermally driven dissociation (underlying mechanisms are analyzed in *Shin and Santamarina* [2011]).

4.3. CO₂-CH₄ Replacement: Thermal and Volumetric Changes

The volume hydrate occupies V_H is larger than the volume of water consumed V_w both for CH₄ hydrate ($V_{CH_4-H}/V_w \approx 1.23$) and for CO₂ hydrate ($V_{CO_2-H}/V_w \approx 1.28$). It follows that a relatively minor hydrate volume expansion will take place during complete CO₂-CH₄ replacement: $V_{CO_2-H}/V_{CH_4-H} = 1.28/1.23 = 1.04$ [*Jung et al* 2010]).

Given the latent heats for CH₄ $L_H = 440 \text{ kJ/kg}$ and CO₂ hydrate $L_H = 374 \text{ kJ/kg}$ and densities for CH₄ hydrate $\rho_{CH_4-H} \approx 0.91 \text{ g/cm}^3$ and CO₂ hydrate $\rho_{CO_2-H} \approx 1.10 \text{ g/cm}^3$, the CH₄-CO₂ replacement is exothermic (Table 2). The thermal analysis of CH₄-CO₂ replacement under adiabatic conditions demonstrates that the sediment temperature will increase by 0.2°C when the hydrate volume fraction is $S_H = 0.2$ and the sediment porosity is $n = 0.4$, Note: the local thermal transient at the point of exchange can exceed $\Delta T \sim 10^\circ\text{C}$ [*Jung et al* 2010].

The volume of liquid CO₂ V_{CO_2-L} required to fully replace CH₄ can be estimated by assuming complete replacement for a volume V_{CH_4-H} of methane hydrate:

$$\frac{V_{CO_2-L}}{V_{CH_4-H}} = \frac{\rho_{CH_4-H}}{\rho_{CO_2-L}} \frac{44}{16 + \chi 18} \approx 0.34 \quad (16)$$

The approximation on the right assumes the hydration number $\chi = 6$ and the density ratio between CH₄ hydrate and liquid CO₂ to be $\rho_{CH_4-H}/\rho_{CO_2-L} = 0.97$ (at $P = 10 \text{ MPa}$ and $T = 7^\circ\text{C}$ - Table 2).

The released CH₄ is a compressible gas and will occupy a volume V_{CH4-G} that can be significantly larger than the volume V_{CO2-L} of injected liquid CO₂. The volumetric ratio is estimated from the modified ideal gas law with the following assumptions: no mutual solubilities, no fluid extraction from the sediment and complete replacement,

$$\begin{aligned}
 \frac{V_{CH4-G}}{V_{CO2-L}} &= \frac{\omega n_{CH4-H} RT}{P} \frac{1}{V_{CO2-L}} \\
 &= \frac{\omega RT}{P} \frac{1}{V_{CO2-L}} \rho_{CH4-H} V_{CH4-H} \frac{1}{16 + \chi 18} \\
 &= \frac{\omega RT}{P} \rho_{CO2-L} \frac{16 + \chi 18}{44} \frac{1}{16 + \chi 18} \\
 &\approx 0.168 \left[\frac{\text{MPa}}{\text{K}} \right] \frac{T}{P}
 \end{aligned} \tag{17}$$

where n_{CH4-H} is the mole of methane in CH₄ hydrate. We obtain the final simplified expression for a compressibility factor $\omega=0.95$, hydration number $\chi=6$, and liquid CO₂ density $\rho_{CO2-L}=938\text{kg/m}^3$. We anticipate a large volume expansion under constant pressure conditions, e.g., $V_{CH4-G}/V_{CO2-L} \approx 4.7$ at 10MPa and 280K. Conversely, high fluid pressure builds up if a constant-volume is imposed, e.g., about 34.7MPa at 7°C. This upper bound estimate assumes all components are incompressible and disregards mutual solubilities. In fact, the most significant solubility is that of water in liquid CO₂, in the order of 0.063mol/kg, i.e., 1.13g of water per 1kg of liquid CO₂, at 8.3MPa and 287K [Song and Kobayashi 1987].

Implications. During CH₄-CO₂ replacement, a shell of CO₂ hydrates forms around existing CH₄ hydrates, which reduces the kinetics of the replacement process [Schicks *et al* 2011]. The liberated CH₄ molecules remain in pore spaces, which further reduces the driving force for the replacement process. While CO₂-CH₄ replacement presents these implementation challenges in the field, the analyses in this section provide two favorable conditions. Firstly, the heat released during CO₂-CH₄ replacement will sustain the reaction. Secondly, the volume expansion will maintain open lenses, prevent conductivity shut-off, and even create new open mode discontinuities that will favor gas recovery.

5. DISCUSSION: RELEVANCE TO OTHER SEDIMENTS

Pore size is determined by the smallest grains in a sediment. Let's define the mass fraction of fine particles ϕ as the ratio between the mass of fines M_F to the total mineral mass of the sediment M_T . It can then be demonstrated that the mass fraction of fine particles needed to fill the pores in a sandy sediment depends on the packing density or void ratio e_f of the fines within the pore space of the sand matrix packed at a void ratio e_c :

$$\phi = \frac{M_F}{M_T} = \frac{e_c}{1 + e_c + e_f} \quad \text{fines fraction} \quad (18)$$

The lower bound for ϕ corresponds to loosely packed fines within the pore space of a densely packed sand. Consider the case of fines packed at a void that corresponds to their liquid limit and sand at a void ratio $e_c=0.7$. Then, Equation 18 predicts that the fines fraction is $\phi=30\%$ when the sand is filled with a non-plastic silt (LL=25, $e_f=0.66$), $\phi=23\%$ for kaolinite (LL=55, $e_f=1.45$), and only $\phi=7\%$ when voids in the sand are filled with montmorillonite (LL=300, $e_f=7.95$). Therefore, special attention should be placed on the amount and mineralogy of fines within a sediment.

Fluid flow often introduces fine particles into otherwise clean sands and leads to clogging and gas-driven fractures during production [Jung *et al* 2012]. Grains also crush and produce fines within the formation when there is a high increase in effective stress, such as near wells in depressurization-driven gas production.

The analyses of secondary ice formation during depressurization (Equations 11~14), volume expansion in thermal stimulation (Equation 15), and thermal changes and expansion during CO₂-CH₄ replacement (Equations 16 and 17) are applicable to all sediments.

6. CONCLUSIONS

Hydro-thermo-chemo-mechanical coupled processes during hydrate formation and dissociation affect hydrate morphology in sediments and control gas production during depressurization, heating and CO₂-CH₄ replacement. Balance and conservation analyses anchored in published data provide robust asymptotic solutions that reflect a number of governing processes. Salient observations from this study are organized into three categories.

Relevant sediment characteristics:

- Specific surface and porosity define pore size. In turn, the pore size determines permeability and capillarity, and also affects the phase boundary when pores are < 100nm.
- Pore size is determined by the smallest grains in a sediment. Even a small amount of fine particles can fill the pore space in sands. Therefore the characterization of sandy deposits must carefully consider the amount and mineralogy of clayey fines.
- Particle size (i.e., specific surface), effective stress and capillarity regulate the potential for hydrate segregation. In agreement with field evidence, hydrate lenses and nodules are anticipated in clayey sediments.
- A hydrate bearing clayey sediment is a two-material system where segregated hydrate is surrounded by hydrate-free water saturated clay.

Hydrate formation:

- The excess dissolved gas in the pore water can concentrate to form $S_H \approx 2\%$ hydrate saturation. Furthermore, a hydrate saturation of $S_H \approx 20\%$ could develop in fine-grained sediments if the initial metabolizable carbon content was as high as $\approx 0.5\%$.
- Higher hydrate saturations that are often found in-situ in the form of lenses and nodules imply that additional methane was transported by advection and/or diffusion.

Gas production:

- Hydrate dissociation is strongly endothermic. The energy density required to dissociate methane hydrate is equivalent to the energy required to cause a 96°C increase in the temperature of the same mass of water. In the extreme case of adiabatic conditions, the available latent heat in a reservoir at an initial temperature of 10°C is sufficient to sustain the dissociation of $S_H=17\%$ without triggering ice formation during depressurization. However, all the available water will freeze when the initial hydrate saturation is $S_H\approx 80\%$. Ice or secondary hydrate formation hinders gas production if it accumulates along flow paths.
- Depressurization is an unlikely production mechanism in fine-grained sediments as the permeability would tend to decrease significantly. Yet, depressurization can be used in combination with other methods such as heating and chemical injection to develop optimal production strategies.
- The volume that hydrate occupies expands into a significantly larger volume of water and gas during dissociation. Expansion factors can vary between 2 and 4 for field conditions of interest. Widespread gas-driven fractures are anticipated upon volume expansion in fine grained sediments.
- The phase boundary for methane mixed with carbon dioxide shifts with the mixture ratio. Methane hydrate bearing sediments are typically encountered under PT conditions such that injected CO₂ will be in liquid phase and will tend to form CO₂ hydrate with free water. The heat released during CO₂-CH₄ replacement sustains the reaction. The volume of released methane is ~5 times larger than the volume of injected liquid CO₂ under common reservoir conditions. Volume expansion will maintain lenses open and create new open mode discontinuities that will favor methane gas recovery.

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Table 1. Interfacial tension and contact angle.

	Interfacial tension [mN/m]	Contact angle [°]
Water-CH ₄ (g)	72 ^a (P=0.1MPa, T=298K) 64 ^a (P=10MPa, T=298K)	105 ^b on PTFE (P=0.1MPa, T=298K)
Water-CH ₄ (h)	32 ^c 17 ^d 39 ^e	no available data
Water-CO ₂ (g)	72 ^b (P=0.1MPa, T=298K)	~38 ^b on calcite (P>7MPa, 298K)
Water-CO ₂ (l)	30 ^b (P=7MPa, T=298K)	~30 ^b on calcite (P>~7MPa, T= 298K) ~20 ^b on quartz (P<~7MPa, T= 298K)
Water-CO ₂ (h)	30 ^c 14 ^d	no available data

a-Ren et al. (2000), b-Espinoza and Santamarina (2010), c-Anderson et al. (2003), d-Uchida et al. (2002), e-Uchida et al. (1999).

Table 2. Physical properties of water, ice, mineral, methane, carbon dioxide, and methane and carbon dioxide hydrate.

Specific heat, heat of transformation, and density.

	Specific heat [kJ/(kg·°C)]	Heat of transformation [kJ/kg]	Density [kg/m ³]
Water	4.218 (273K) ^a 4.192 (283K) ^a 4.2174 (273K) ^c	For water mass, 334.2 (273.2K) ^b 336 (273.1K) ^c	999.9 (273K) ^a 999.7 (283K) ^a
Ice	2.014 (260K) ^b 1.957 (260K) ^c 2.097 (270K) ^b 2.052 (270K) ^c 2.097 (273K) ^d	-	917 (273K) ^c
Quartz	0.73 (273K) ^d 0.71 (273K) ^f 0.8 (286~373K) ^f	-	2650 ^e 2620 ^f
CH ₄ (g)	2.26 (298K, 0.1MPa) ^f 2.259 (280K, 1MPa) ^g 3.813 (280K, 20MPa) ^g	2290 (Heat of combustion) ^f	7.04 (280K, 1MPa) ^g 177.56 (280K, 20MPa) ^g
CO ₂ (g)	0.819 (275K) ^f 2.47 (273K) ^f	-	983 ^f (273K, 3.4MPa)
CO ₂ (l)	2.5694 (274K 3.5642MPa) ^h 2.8141 (280K, 4.1607MPa) ^h 2.2798 (280K, 10MPa) ^h	-	922.3 (274K 3.5642MPa) ^h 883.58 (280K, 4.1607MPa) ^h 938.22 (280K, 10MPa) ^h
CH ₄ hydrate	2.003 (260K for CH ₄ ·6H ₂ O) ⁱ 2.077 (270K for CH ₄ ·6H ₂ O) ⁱ 0.0061(T-273) + 2.16 (274~290K, 31.5MPa) ^j 0.0033·(T-273) + 2.14 (287.4K, 31.5~102MPa) ^j	For CH ₄ · χ H ₂ O 437.1 ⁱ 430.3 (283.15K, χ =5.98) ^k 470.4 (278.15K, χ =5.97) ^k 429.8 ^l 434.4 (273.65K, χ =6.38) ^m	922 (283K, 5MPa) ^j 910 ^{r&s}
CO ₂ hydrate	No data found	For CO ₂ · χ H ₂ O 374.5 (273.65K, χ =7.23) ^m 390.7~398.5 (at quadruple points, χ =6.6~5.6) ⁿ	1065 ^o 1054 ^p 1090~1110 ^q

a-Weast (1987), b-Handa et al. (1984), c-Leaist et al. (1982), d-Kaye and Laby (2007), e-Dvorkin et al. (2000), f-Engineering ToolBox (www.engineeringtoolbox.com), g-Sychev et al. (1987), h-Span and Wagner (1996), i-Handa (1986), j-Helgerud et al. (2009), k-Lievois et al. (1990), l-Rueff et al. (1988), m-Kang et al. (2001), n-Anderson (2003), o-Anderson et al. (2003), p-Uchida et al. (2002), q-Aya et al. (1997), r-Kieffe et al. (1985), s-Sloan and Koh (2008).

Figure 1. Hydrate stability in small pores. (a) CH₄ hydrate stability. Theoretical stability boundary of CH₄ hydrates in (black continuous line) bulk phase and (blue dotted line) 50nm, (green broken line) 20nm, (black chain line) 10nm pores. Experimentally obtained stability condition of CH₄ hydrate in (♦) 102.6nm [Uchida et al 2002], (○) 49.5nm [Uchida et al 2002], (▲) 30.9nm [Uchida et al 2002], (●) 30nm [Seo et al 2002], (■) 30.6nm [Anderson et al 2003], (×) 14nm [Handa and Stupin, 1992], (◇) 15nm [Seo et al 2002], (□) 15.8nm [Anderson et al 2003], (Δ) 11.9nm [Uchida et al 2002], (●) 9.2nm [Anderson et al 2003], (—) 6nm [Uchida et al 2002], (—) 6nm [Smith et al 2002^a], and (+) 6nm [Seo et al 2002] pores. Parameters for Gibbs-Thompson equation are $T_s=32\text{mN/m}$, $m_h=119.5\text{g/mol}$, $\cos\theta=1$, $\rho_{CH_4}=914\text{kg/m}^3$, and $L_f=53.2\text{kJ/mol}$ [Anderson et al 2003]. (b) CO₂ hydrate stability. Theoretical stability boundary of CO₂ hydrates in (black continuous line) bulk phase and (blue dotted line) 50nm, (green broken line) 20nm, (black chain line) 10nm pores. Experimentally obtained stability condition of CO₂ hydrate in (♦) 102.6nm [Uchida et al 2002], (○) 49.5nm [Uchida et al 2002], (▲) 30.9nm [Uchida et al 2002], (●) 30nm [Seo et al 2002], (■) 30.6nm [Anderson et al 2003], (×) 15nm [Smith et al 2002^b], (◇) 15nm [Seo et al 2002], (□) 15.8nm [Anderson et al 2003], (Δ) 11.9nm [Uchida et al 2002], (■) 10nm [Smith et al 2002^b], (●) 9.2nm [Anderson et al 2003], and (+) 6nm [Seo et al 2002] pores. Parameters for Gibbs-Thompson equation are $T_s=30\text{mN/m}$, $m_h=147.5\text{g/mol}$, $\cos\theta=1$, $\rho_{CO_2}=1065\text{kg/m}^3$, and $L_f=65.2\text{kJ/mol}$ [Anderson et al 2003].

Figure 2. Hydrate phase boundary – different methane and carbon dioxide gas mixtures. Molar fractions of methane n_{CH_4} and carbon dioxide n_{CO_2} : (red broken line) $n_{\text{CH}_4}/n_{\text{CO}_2}=0.25$, (blue dotted line) $n_{\text{CH}_4}/n_{\text{CO}_2}=1$, (green chain line) $n_{\text{CH}_4}/n_{\text{CO}_2}=4$. Boundaries are calculated using HydraFLASH [from HYDRAFACT v2.2]. The Liquid-Vapor (L-V) boundary is estimated using the equation developed by Jung et al. [2010].

Water saturated sediment

Hydrate lens formation

Before hydrate lens formation

After Hydrate lens formation

Water	$\rho_w L n_0$	=	$\rho_w (L - \delta) n_f + \rho_{w_hyd} \delta$
Methane	$C_B L n_0$	=	$C_A (L - \delta) n_f + C_H \delta$
Mineral	$\rho_m L (1 - n_0)$	=	$\rho_m (L - \delta) (1 - n_f)$

Figure 3. Anticipated hydrate lens thickness that could form from the initially dissolved excess gas. Hydrate lens thickness δ in a medium with lens-to-lens spacing L is a function of the initial porosity n_0 , gas solubility in the absence and in the presence of gas hydrate C_B and C_A , and gas concentration in hydrate C_H .

Figure 4. Hydrate dissociation and subsequent possible ice formation. (a) Hydrate bearing sediment with initial hydrate saturation S_H . Under adiabatic conditions, the energy needed to dissociate hydrate can be supplied by the medium's latent heat (case 1); additional heat may be gained from exothermic ice formation (case 2). (b) Consider hydrate bearing sediments with porosity $n=0.4$ at initial temperatures $T_o=5, 10, 15$, and 20°C depressurized to $P_{eq}=3\text{MPa}$ so that the hydrate equilibrium temperature is $T_{eq}=2.5^\circ\text{C}$. Ice does not form if initial hydrate saturation is $S_H=0.09, 0.17, 0.25$, and 0.32 for each initial temperature conditions. As the initial hydrate saturation increases, the amount of ice formed due to hydrate dissociation also increases. Ice fraction FR_{wi} is the portion of water (initial water and water from hydrate dissociation) converted into ice. Values of specific heat for minerals, water, gas, and hydrate and of latent heat of hydrate dissociation and ice formation are listed in Table 2.