A high-finesse Fabry-Perot cavity with a frequency-doubled green laser for precision Compton polarimetry at Jefferson Lab

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Abstract

A high-finesse Fabry-Perot cavity with a frequency-doubled continuous wave green laser (532 nm) has been built and installed in Hall A of Jefferson Lab for high precision Compton polarimetry. The infrared (1064 nm) beam from a ytterbium-doped fiber amplifier seeded by a Nd:YAG nonplanar ring oscillator laser is frequency doubled in a single-pass periodically poled MgO:LiNbO₃ crystal. The maximum achieved green power at 5 W infrared pump power is 1.74 W with a total conversion efficiency of 34.8%. The green beam is injected into the optical resonant cavity and enhanced up to 3.7 kW with a corresponding enhancement of 3800. The polarization transfer function has been measured in order to determine the intra-cavity circular laser polarization within a measurement uncertainty of 0.7%. The PREx experiment at Jefferson Lab used this

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system for the first time and achieved 1.0% precision in polarization measurements of an electron beam with energy and current of 1.06 GeV and 50 μ A.

Keywords: Compton polarimetry, Fabry-Perot cavity, Laser Polarization, Polarized electron beam

1. Introduction

The Continuous Electron Beam Accelerator Facility (CEBAF) at Jefferson Lab (JLab) delivers a highly polarized electron beam in the 1 – 11 GeV energy range for currents up to $\sim 200 \mu$ A. A key part of the JLab physics program consists of high-precision parity violating electron scattering experiments [1–3] that require a fast and precise electron beam polarization measurement. Conventional polarimetry techniques such as Møller [4] and Mott [5] are destructive for the beam properties due to solid targets they use and cannot be operated simultaneously with the physics experiments. They can only be operated at low intensity ($< 10 \mu$ A) and at low energy (< 5 MeV) respectively; therefore, the physics experiments have to assume that beam polarization remains constant when the intensity or the energy of the beam is several orders of magnitude higher. Alternatively Compton polarimetry has been used with great success at JLab [6, 7] and elsewhere [8–12] to measure the electron beam polarization in a continuous and non-destructive manner. However, unlike at high-current (> 20 mA) storage rings [8, 9, 12] and at high-energy (> 50 GeV) colliders [10, 11], the relatively low-current and low-energy nature of the CEBAF electron beam has required the use of high-finesse optical cavities [13, 14] to enhance the laser power beyond commercially available lasers to provide sufficient electron-photon collision luminosity.

Compton polarimetry determines the electron beam polarization based on a well-known spin-dependent scattering cross-section [15] between polarized electrons and photons. The longitudinal electron beam polarization P_e is extracted

24 from the experimental Compton scattering asymmetry A_{exp} , according to,

$$A_{\text{exp}} = P_e P_\gamma A_{\text{th}}, \quad (1)$$

25 where A_{th} is the theoretical Compton scattering asymmetry that can be de-
26 rived by combining the calculated spin-dependent Compton cross section with
27 the appropriate experimental response function [16], and P_γ is the circular pho-
28 ton beam polarization. The scattering asymmetry A_{exp} can be measured based
29 on the detection of either the scattered photons or the scattered electrons and
30 depends on the energies of the colliding electron and photon beams. For an
31 electron beam of 1.0 GeV, the maximum scattering asymmetry for infrared
32 (1064 nm) photons is 1.8%, whereas for green (532 nm) photons, it is 3.5%. For
33 an electron beam of 6 GeV, these values are about 10% and 18%, respectively.
34 Therefore, Compton polarimetry at low beam energies (< 2 GeV) is difficult to
35 perform.

36 External optical cavities have frequently been employed to increase the laser
37 power from a light source through a process of coherent addition. Recently
38 optical cavities have been widely employed in many areas such as X-/ γ -ray gen-
39 eration via inverse-Compton scattering [17, 18], high harmonic generation [19]
40 and electron beam polarimetry [14, 20]. According to the best of our knowledge,
41 there are only three facilities in the world have ever built a Compton polarimeter
42 with an optical cavity; Mainz Microtron (MAMI) [21], Hadron Electron Ring
43 Accelerator (HERA) [20] and JLab [14]. In Hall A of JLab, a Compton back-
44 scattering polarimeter had been operational since 1999 [22]. Its photon source
45 had a typical circulating power of ~ 1.5 kW inside a monolithic Fabry-Perot
46 cavity where the circularly polarized photons scattered from the longitudinally
47 polarized electrons. It provided 1.0% statistical (and 1.2% systematic) preci-
48 sion with ~ 25 minutes' data taking for 4.6 GeV, 40 μA electrons [22]. This
49 polarimeter used a continuous-wave (CW) infrared (IR, 1064 nm) laser as its
50 photon source and had serious limitations in providing a good signal-to-noise
51 ratio for beam energies below 2 GeV [23]. Under this circumstance, it is highly
52 desirable to have a shorter-wavelength and higher-power light source since this

will result in larger back-scattered electron and photon energies and a larger measured scattering asymmetry, and hence increased ability to control systematic uncertainties.

The Lead Radius Experiment (PREx) [1] at JLab aims to provide the first model-independent evidence of the existence of a significant neutron skin in ^{208}Pb . PREx proposed to obtain a statistical and systematic precisions of 3.0% and 2.0% respectively on the parity-violating electroweak asymmetry of polarized electrons from ^{208}Pb to determine the neutron radius of ^{208}Pb at 1.0% accuracy. The uncertainty goal for beam polarimetry at 1.06 GeV was 1.0%. In order to meet the high-precision requirement, the existing Compton polarimeter underwent an upgrade [24, 25] in 2010. The upgrade includes a new photon detector with an upgraded integrating data acquisition (DAQ) system, a new electron detector, and a new Compton photon source that includes a green laser (532 nm) with a new high-finesse Fabry-Perot cavity [26].

This paper will describe the upgraded experimental setup in Hall A at JLab, with an emphasis on the frequency-doubled green laser system and optical cavity. A unique technique to extract the laser beam polarization inside a resonant Fabry-Perot cavity will be given and finally, the first electron beam polarization measurement results from the PREx experiment [1] at a beam energy and current of 1.06 GeV and 50 μA will also be presented. With an enhancement factor and intra-cavity power of 3,800 and 3.7 kW, we report the highest power Compton polarimetry facility operating at 532 nm as compared to existing facilities such as MAMI [21] and Hall C at JLab [7].

2. Overview of upgraded Compton polarimeter

The upgraded Compton polarimeter in Hall A consists of a magnetic chicane, a photon source that is composed of a laser system and Fabry-Perot cavity, a photon detector, and an electron detector as shown in Fig. 1. The electron beam enters from the left. When the four identical dipoles of the chicane, referred to as D_1 , D_2 , D_3 and D_4 , are energized, the beam is deflected vertically

Fig. 1: A not-to-scale schematic of the upgraded Compton polarimeter in Hall A at JLab. A magnetic chicane consists of four identical magnetic dipoles (D_1 , D_2 , D_3 and D_4) that deflect the primary electron beam and send it through the Fabry-Perot cavity. The scattered Compton electrons and photons will be detected by electron and photon detectors, respectively.

and crosses the photon beam enhanced in the Fabry-Perot cavity that is located at the center of the chicane. The Fabry-Perot cavity is enclosed in a vacuum chamber that is connected to electron beam pipes from both ends and sits on an optical table where the laser and other optical elements are located. The Compton Interaction Point (CIP) is at the center of the beam crossing in the cavity. The crossing angle between the electron and photon beams is 24 mrad. The electrons undergo Compton scattering with circularly polarized photons resonating in the Fabry-Perot cavity fed by a CW green laser (532 nm). The backscattered photons are detected in the photon detector while the scattered electrons can be detected in the electron detector located a few mm above the primary beam in front of D_4 . Approximately one electron in every one billion

Fig. 2: A scale 3D view of the Compton polarimeter in the Hall A tunnel at JLab.

undergoes Compton scattering. Unscattered electrons, separated from the scattered particles by D_3 in the chicane, continue on into the Hall A target for the primary experiment. Independent electron and photon analyses give complementary determinations of the electron beam polarization. A scale 3D view of the Compton polarimeter in the Hall A tunnel at JLab is shown in Fig. 2.

The photon detector is located under dipole D_4 and consist of a single crystal of Ce-doped Gd_2SiO_5 (GSO) and a single PMT (Photomultiplier Tube). It is mounted on a motorized table with remote-controllable motion along both axes (horizontal and vertical) transverse to the electron beam direction. The scattered photons from the CIP go through a thin vacuum window and lead disk in the vacuum pipe before they hit the detector window. The photon detector DAQ uses a customized 12-bit Flash Analog-to-Digital Converter (FADC) that integrates the scintillation photon signals from the PMT and samples the data at rates of 200 mW [24].

The electron detector consists of four silicon microstrip planes spaced horizontally 1 cm from each other with a 200 micron vertical rising offset between planes. Each plane consists of 192 strips of silicon with a width of 240 microns. The planes are inclined at an angle of 58 mrad from the vertical position. The detector is mounted on a translator with a remote-controllable stepper motor and can travel vertically up to 120 mm from the main beam.

3. Optical and mechanical system

The optical elements of the polarimeter are mounted on a vibration-damped optical table between dipoles D_2 and D_3 (Fig. 2). A schematic of the optical system of the polarimeter is illustrated in Fig. 3. Based on their main functionality, we can categorize the optical elements into four groups necessary for achieving the required power and circular polarization in the cavity. The first group is the laser source that provides a green beam at the wavelength of 532 nm. The second group consists of the elements that transport, align and focus the incident beam for coupling to the optical cavity. The third group in-

Fig. 3: The optical system consists of a NPRO seed laser, a fiber amplifier, a frequency doubling setup and a Fabry-Perot cavity enclosed in a vacuum chamber. (YDFA: ytterbium doped fiber amplifier; PPLN: periodically poled lithium niobate; DC₁, DC₂: dichroic mirrors; BD: beam dump; FOI: Faraday optical isolator; HWP: half-wave plate; PBS: polarizing beam splitter; QWP: quarter-wave plate; HBS: holographic beam sampler; M_{ce}, M_{cs}: concave cavity mirrors; CCD: cameras; PDR, PDT: photodiodes; L: lenses; M: plane mirrors; W: vacuum windows; S: photodetectors)

cludes elements for controlling and measuring the polarization. The last group consists of elements which allow the use of the reflected beam from the cavity in the electronic feedback system to achieve frequency locking of the laser to the cavity.

3.1. Frequency doubling

As shown in Fig. 3, the seed laser is a narrow-linewidth (< 5.0 kHz) diode pumped Nd:YAG nonplanar ring oscillator (NPRO) laser (Lightwave 126; JDSU) that delivers a linearly polarized CW IR (1064 nm) beam of up to 250 mW. The output of this laser has been fiber-coupled to a ytterbium-doped fiber amplifier (YDFA, YAR-10K-1064-LP-SF; IPG Photonics) through

132 a single-mode polarization-maintaining (PM) fiber. The YDFA takes ~ 10 mW
 133 of seed laser and provides a linearly polarized (extinction ratio: 20 dB) output
 134 with a maximum power of 10 W at 1064 nm in CW mode. The frequency dou-
 135 bling crystal is bulk periodically poled MgO:LiNbO₃ (PPLN, HC Photonics)
 136 doped with 5% MgO in order to minimize photo-refractive damage. The crystal
 137 is 0.5 mm thick, 3 mm wide and 50 mm long, and the quasi-phase matching
 138 (QPM) period is $6.92 \mu\text{m}$ with a 50% duty cycle. The input and output surfaces
 139 are antireflection (AR) coated for 1064 nm and 532 nm, respectively. The crys-
 140 tal is placed in an externally controlled, temperature-stabilized oven developed
 141 in-house. The oven is mounted on a stage composed of a four-axis tilt aligner
 142 (9071-V; Newport) in order to establish a precise alignment for phase matching.
 143 A temperature controller (TECSource 5305; Arroyo Instruments) with a nomi-
 144 nal resolution of 0.01°C provides the required phase-matching temperature for
 145 second harmonic generation (SHG). The crystal optical axis is matched with the
 146 direction of the output polarization (vertical) of the YDFA. A pair of 0.5 inch
 147 lenses (L_a and L_b in Fig. 3) with focal lengths of 13.8 mm and 15 mm (with a
 148 total effective focal length of ~ 120 mm) are then used to focus the beam waist
 149 diameter ($\sim 80 \mu\text{m}$) into the center of the crystal. This makes the Rayleigh
 150 length of the pump laser focus to be around 5 mm and ensures the beam size at
 151 the crystal entry and exit faces to be around $400 \mu\text{m}$. This critical focusing also
 152 ensures the incoming beam is not clipped by the tiny crystal thickness while
 153 keeping the SHG efficiency close to the maximum. The generated green beam
 154 is separated from the residual IR beam after the crystal via a pair of 1.0 inch
 155 dichroic mirrors ($R > 99\%$ at 532 nm, $T > 95\%$ at 1064 nm) noted as DC₁ and
 156 DC₂ (Altos Photonics). The lenses, oven and dichroic mirrors are all mounted
 157 on a separate linear translation stage seated on a rail, and the whole system is
 158 contained in an enclosure box.

159 With the experimental setup as described above, we have measured sev-
 160 eral properties, such as crystal temperature tuning curve, beam quality and
 161 power stability, of the second harmonic beam. The measured temperature tun-
 162 ing curve at 5 W IR pump power is shown in Fig. 4. The red circles show

Fig. 4: Experimental (red circles) and theoretical [27, 28] (blue line) temperature tuning curve for PPLN crystal at beam waist diameter of $80\ \mu\text{m}$ and IR pump power of 5 W.

Fig. 5: Average green power (solid circles) output and corresponding phase matching temperature (open squares) at different IR pump power from the fiber amplifier. A theoretical fit (green line) defined by Eq. (2) is used to extract the normalized SHG conversion efficiency.

the experimental data while the blue line represents the theoretical fit for the first-order QPM interaction predicted by the Sellmeier equation for PPLN crystal [27, 28]. The experimental results give the full width at half-maximum (FWHM) phase-matching temperature bandwidth $\Delta T = 0.6\ ^\circ\text{C}$ at the phase-matching temperature $64.0\ ^\circ\text{C}$.

Fig. 5 shows the average green power (solid circles) output from PPLN

and corresponding phase-matching temperature (open squares) at different IR pump powers from the fiber amplifier. It is important to note that the value of the phase-matching temperature changes slightly when the IR pump power is changed. The phase-matching temperature ranges between 64.0 °C and 64.3 °C for IR pump power between 200 mW and 5 W. At each power level the crystal is maintained at the peak phase-matching temperature to ensure maximum green power. For a loosely focused Gaussian beam, the normalized conversion efficiency η_{nor} for first-order QPM is defined as [29],

$$I_2 = \eta_{nor,QPM} L I_1^2, \quad (2)$$

where I_1 and I_2 are the fundamental and SHG powers, ω_1 is the frequency of the fundamental beam, d is the nonlinear coefficient of PPLN, ε_0 is the permittivity of free space, and n_1 and n_2 are the refractive indexes at these wavelengths. In Fig. 5, as the theoretical fit (green line) defined by Eq. (2) shows, the green power varies quadratically with the IR pump power with a normalized conversion efficiency η_{nor} of $1.37\%W^{-1}cm^{-1}$. It is necessary to point out that all powers are direct measurements after DC₂ by an optical power meter (PM140; Thorlabs) without correcting for the residual reflection at the crystal face or losses in the dichroic mirrors. The experimental results show that there is no sign of saturation in the SHG power at 5 W IR pump power. This is mostly due to a larger beam waist size at the crystal center so that there is no pump depletion. Therefore, the achieved conversion efficiency is somewhat lower than the maximum conversion efficiency of $2.62\%W^{-1}cm^{-1}$ provided by the vendor. All of these considerations suggest that thermal lens effects are negligible. The maximum achieved green power at 5 W IR pump power is 1.74 W with a total conversion efficiency of 34.8%. A primary goal of this work is to develop a stable and good-quality green beam at the Watt level, so we did not pursue higher conversion efficiencies.

The quality of the green beam is of major importance in power enhancement

Fig. 6: The transverse intensity profile (shown in the inset) of the green beam measured by a laser beam profiler at 1.74 W green power. Closed and open circles are the beam diameters in the horizontal (x) and vertical (y) directions and continuous lines show the theoretical fits to extract the M^2 [30] values in both directions.

with an optical cavity, as any deviation from a perfect Gaussian profile will lead to a rejection of power by the high-finesse cavity and will not contribute to the power buildup inside the Fabry-Perot cavity. In order to check the beam quality, we focused the green beam after the PPLN into a $200\text{ }\mu\text{m}$ waist diameter with an additional lens and measured the beam size at different axial positions. Fig. 6 shows the green beam profile at 1.74 W monitored by a laser beam profiler (LBA-FW-SCOR20; Spiricon) along with the theoretical fit. Closed and open circles are the measured beam diameters in the horizontal (x) and vertical (y) directions. The result of the theoretical fits (solid lines) to the experimental data determines an M^2 [30] value of ~ 1.1 in both dimensions confirming the TEM_{00} spatial mode in the SHG process. However, there is a small astigmatism mainly arising from the difference in refractive indexes along the horizontal and vertical axes of the PPLN crystal. As shown in Fig. 7, the peak-to-peak stability of green power at 1.74 W is 0.8% for the entire period of 12 hours, while the fundamental IR power stability from the YDFA is measured to be better than 0.6% over 4 hours.

The frequency-doubled green beam based on single-pass SHG in a PPLN

Fig. 7: Second harmonic power stability at the output of PPLN is monitored at 1.74 W for 12 hours.

crystal pumped by a YDFA has been used with the high-finesse Fabry-Perot cavity as a photon source for the Compton polarimeter during the three-month run period of the PREx experiment [1] in 2010. In the following we describe how we establish a frequency locking of this beam to a resonant frequency of the high-finesse Fabry-Perot cavity.

3.2. High-finesse Fabry-Perot cavity

The green beam is propagated through a series of optical elements (Fig. 3) to properly match the fundamental cavity mode (TEM_{00}) at the injection point. After exiting the PPLN crystal and reflecting from two dichroic mirrors (DC_1 and DC_2), the green beam is focused by a lens L_0 ($f_0 = 75$ mm) at 6.0 cm from the frequency doubling setup with waist diameters $370 \mu\text{m}$ and $450 \mu\text{m}$ in the horizontal and vertical directions. The focusing of the incident beam at the CIP is accomplished by three lenses denoted L_1 , L_2 and L_3 , respectively. A diverging lens L_1 ($f_1 = -1.0$ m) at 405 mm from the frequency-doubling setup nearly collimates the beam after it passes through an optical isolator (isolation: 40 dB, IO-3-532-HP; Thorlabs) and a half-wave plate (HWP). In order to achieve the correct beam waist size at the cavity center, we have two more lenses, L_2 and L_3 ($f_2 = -50$ mm, $f_3 = 200$ mm), installed at 820 mm and 1.0 m from the frequency-doubling setup. Here in our setup, L_1 and L_2 are on fixed mounts

233 and L_3 is mounted on a remote controlled translation stage (M-605.1DD; Physik
 234 Instrumente). This allows fine tuning and precise alignment of the laser beam
 235 to the cavity by using another pair of remotely controlled mirrors (M_1 and
 236 M_2) that allow four degrees of motion (2 translations, 2 rotations) for the laser
 237 beam with respect to the optical axis of the cavity. Both the proper focusing
 238 and precise alignment of the impinging laser beam to the cavity are needed in
 239 order to achieve good mode matching. The mirrors M_{r1} , M_{r2} , M_e and M_s are
 240 fixed at 45° with respect to the incident beam. A camera (CCD_1) facing the
 241 mirror M_{r2} monitors the positions of the incident and reflected beams from the
 242 cavity. Another camera (CCD_2) at the cavity exit is used for monitoring the
 243 profile of the transmitted beam from the cavity.

244 As shown in Fig. 3, our cavity consists of two (M_{ce} , M_{cs}) identical highly
 245 reflective ($R = 99.975\%$) concave mirrors (Advanced Thin Films) separated
 246 by 850 mm. The mirrors have a typical transmittance of 240 ppm (parts per
 247 million) and total nominal (scattering and absorption) loss of < 10 ppm. This
 248 leads to a maximum power enhancement of $G \approx \sqrt{R}/(1 - R) = 4,000$. The
 249 coating is made of alternating dielectric quarter-wave layers of SiO_2 and Ta_2O_5
 250 on a super polished (surface RMS roughness = $0.5 \text{ \AA}$) fused silica substrate
 251 (thickness 4 mm, diameter 7.75 mm) by an ion beam sputtering technique. The
 252 mirrors have a typical radius of curvature of 0.5 m that requires a Gaussian
 253 beam waist diameter of $348 \text{ }\mu\text{m}$ at the center of the cavity [30]. This geometry
 254 was chosen to maximize the electron-photon collision luminosity when the laser
 255 light is frequency locked to the cavity and crosses with the electron beam.

256 A careful study of beam propagation from the frequency doubling setup to
 257 the cavity through each optical element has been performed using OptoCad [31].
 258 Fig. 8 shows the calculated beam size versus the distance along the beam path
 259 from the frequency doubling setup. Experimental verification of the laser waist
 260 size at the center of the cavity is not possible with the beam profiler. Therefore,
 261 we created an auxiliary optical path (2.375 m) that has the same path length
 262 from the doubling setup to the cavity with all the optical elements in place.
 263 Instead of M_{ce} , we used an uncoated mirror substrate made of the same fused

Fig. 8: The calculated beam size (beam envelope) versus the distance along the beam path from the frequency doubling setup.

silica material with the same radius of curvature. We experimentally checked the beam waist size and location after this mirror substrate, and compared it to our calculation. A small correction with L_3 (few mm) is necessary in order to get an average beam size of $350 \mu\text{m}$ at a distance of 425 mm (corresponding to the cavity center) from this mirror substrate. At the exit of the cavity, there is a set of optical elements composed of a quarter-wave plate (QWP_2), a holographic beam sampler (HBS) and a Wollaston prism (Fig. 3 and Fig. 9) that are used for measuring and monitoring the laser polarization (discussed in Section 4).

3.3. Mechanical design of the cavity

The strongest requirements on the design of a Fabry-Perot cavity in a Compton polarimeter are that it must be rigid and must have a small crossing angle with the electron beam. The small crossing angle increases the electron-photon interaction luminosity. The geometry of the cavity is determined by the total distance between the two mirrors (850 mm), the radius of curvature of the mirrors (500 mm) and the crossing angle between the laser and electron beams. With this design the crossing angle is 24 mrad, the gap between the electron beam and mirror edge is 6.12 mm and the laser beam size on the cavity mirror is $898 \mu\text{m}$.

Fig. 9: 3D mechanical drawing of the laser optics and Fabry-Perot cavity system in the Hall A tunnel at JLab.

282 A mechanical drawing of the cavity is shown in Fig. 9. The cavity and all
 283 the other optical elements are mounted on an optical table with a footprint of
 284 $1.5 \text{ m} \times 1.2 \text{ m}$. This table is placed on a laminar flow damping system consisting
 285 of four pneumatic posts with auto-leveling valves to isolate the vibrations from
 286 the ground. The optical table is located inside a small room equipped with a
 287 laminar flow fan filter unit. In order to ensure thermal and mechanical stability,
 288 an Invar (64FeNi) frame consisting of three cylindrical rods attached to two
 289 vertical plates, each with an octagonal cutout, forms the backbone of the cavity
 290 frame. The cavity vacuum chamber is a cylindrical vessel made of stainless steel
 291 with a diameter of 4.5 inches (Fig. 9) connected to two octagonal gimbal mounts

292 through two soft bellows. The bellows allow the gimbal mounts to tilt freely in
 293 both the horizontal and vertical planes when they are adjusted by four piezo
 294 actuators under atmosphere. However, in our experiment, the bellows were too
 295 stiff under vacuum for the piezo actuators to move the gimbals remotely. There-
 296 fore the procedure involves locking the cavity under atmosphere, then locking
 297 the gimbals and drawing vacuum¹. The cavity mirror is mounted on a mirror
 298 holder attached to these gimbal mounts which are also made of Invar. Each
 299 gimbal mount is supported by four stainless steel cylindrical bearings (C-Flex
 300 Bearing Co.) that form two axes (horizontal and vertical) for each gimbal mount
 301 and allow them to tilt freely around each axis. The mirror holder is machined
 302 such that the rotation axis of each mirror lies on the same axis as the gimbals.
 303 The bearings are 0.25 inch in diameter and 0.4 inch in length, and each can
 304 support a load up to 100 lbs. Two remote controlled picomotors (8302; New-
 305 focus) attached to each gimbal mount are used for aligning each cavity mirrors
 306 by tilting the gimbal mounts in both the vertical and transverse planes with
 307 respect to the laser beam propagation direction. A pair of counteracting spring
 308 plungers (maximum load 13 lbs) are attached to the gimbal mounts to keep the
 309 alignment in position. The picomotors are interfaced to the EPICS [32] slow
 310 control system (discussed in Section 3.4) that allows remote alignment of the
 311 cavity mirrors.

312 A pair of vacuum window substrates (W_e and W_s in Fig. 3) that are made of
 313 fused silica (3 mm thick and 0.7 inch in diameter) allow the laser beam to enter
 314 and exit the cavity via a pair of 0.5 inch turning mirrors (M_e and M_s in Fig. 3)
 315 oriented at 45° with respect to the incident laser beam. The vacuum windows
 316 are AR coated for 532 nm and welded to stainless steel flanges (Fig. 9) by the
 317 glass-metal soldering technique. Two soft bellows on both sides of each gimbal
 318 mount are connected to both sides of the cavity vacuum chamber through a pair

¹ Even though we were able to keep the cavity alignment in position during the three-
 month period of the PREx experiment, we believe this feature could be redesigned to make
 the remote alignment of cavity mirrors under vacuum possible.

319 of flanges and allow the gimbals to tilt freely. Each of the 45° turning mirrors
 320 is mounted to an aluminum holder that is attached to a stainless steel flange
 321 mounted on a post. Each aluminum holder has a slit 4 cm long and 1cm wide
 322 that allows the electron beam to pass through. When the cavity is installed in
 323 the electron beam line (Fig. 10), the stainless steel flanges are connected to the
 324 beam pipe by another set of soft bellows that isolates any vibrations from the
 325 rest of the electron beam pipe. Two beam position monitors located on both
 326 sides of the cavity are used to monitor changes in beam position of the elec-
 327 tron beam during beam tuning and data taking. Two ion pumps can provide a
 328 vacuum of $\sim 10^{-9}$ Torr inside the cavity after several hours of bake-out at $\sim$
 329 100°C .

330 *3.4. Feedback and slow control system*

331 Maintaining the resonance and therefore the enhancement in the cavity re-
 332 quires feedback control of the laser frequency. The optical frequency stabiliza-
 333 tion must be better than the free spectral range ($FSR=176.5$ MHz) divided by
 334 the finesse ($F=12,000$), which is ~ 15 kHz (cavity bandwidth). This is equiv-
 335 alent to a stabilization of the 850 mm cavity length to better than the laser

Fig. 10: The cavity vacuum chamber attached to two ion pumps on the optical table and connected to the electron beam pipe in the Hall A tunnel at JLab. The electron beam pipe above the cavity is used for a straight beam to the experimental Hall when the Compton polarimeter is not used.

wavelength divided by the finesse, which is ~ 0.04 nm. The electronic feedback system that controls the laser frequency uses the Pound-Drever-Hall technique [33]. The error signal is created by phase detection between the photodiode (PDR in Fig. 11) output of the modulated reflection signal and the modulation signal from the function generator (FG220, Yokogawa). The error signal includes information on cavity resonance, and is then used to build the feedback signals supplied on both the fast and slow control ports of the seed laser. The electronic feedback system has been designed and built by Saclay [13]. The simplified flow chart is shown in Fig. 11.

The optical elements that are critical to beam alignment and polarization control and measurement, the lasers (seed laser, fiber amplifier and PPLN doubling system) and the locking electronics are all interfaced to a remotely controlled system through a local workstation. Electronics specific to the feedback control loop, the function generator (ramp generator, modulation signal generator), the oscilloscope and the workstation are located in the control room. The lasers, stepper and servo motors with their control units, photodiodes, CCD cameras and the preamplifiers are located on the optical table in the Hall A tun-

Fig. 11: A simplified flow chart of the feedback control system used for laser frequency locking to the cavity fundamental mode.

Fig. 12: A functional view of the laser and cavity system illustrates the electronic control units with the optical elements.

nel. The monitors related to the cavity resonance mode and beam alignment are connected to cameras CCD_2 and CCD_1 through coaxial BNC cables and are located in the control room. Fig. 12 shows a functional view of the laser and cavity system with control units.

An automatic switching system from “open-loop” mode to “closed-loop” mode around the cavity resonance region permits the system to transition automatically between the resonant and locked states. It consists of an electronic circuit and an EPICS program that manage the laser temperature scan via the slow control port of the seed laser. A 10 V peak-to-peak triangular ramp, together with a sinusoidal modulation signal at $\Omega = 928$ kHz with 50 mV amplitude, is supplied on the laser piezoelectric transducer (PZT) via the fast control port of the seed laser.

365 Two fast photodiodes (S1223; Hamamatsu) are used for monitoring the re-
 366 flected (PDR) and transmitted (PDT) signals. They are held at a constant
 367 voltage level of 5 V. The currents from the photodiodes are transformed into
 368 voltage signals via a trans-impedance amplifier that allows signal transmission
 369 across 100 meters of coaxial cables. A band-pass filter is applied on the reflected
 370 signal from the cavity after it is mixed with the modulation signal at frequency
 371 Ω and amplified. The mixing and filtering extracts an error signal corresponding
 372 to the change in reflected light at the laser modulation frequency. The value
 373 of Ω was determined by minimizing the laser Residual Amplitude Modulation
 374 (RAM) [13]. The error signal is injected into a series of three separate inte-
 375 grators (proportional-integral-derivative or PID) common to the slow and fast
 376 control loops. The two control modes play complementary roles: the slow mode
 377 is for compensating the slow drift in laser frequency while the fast mode allows
 378 the efficient reduction of the laser frequency jitter. The output signals of these
 379 two modules are applied directly to the two laser control ports that control the
 380 seed laser frequency.

381 The VME (VERSA Module Eurocard) crate, used for controlling the elec-
 382 tronics, is located in experimental Hall A. The electronics are controlled from a
 383 workstation in the control room with the help of interface cards. The interface
 384 cards permit us to transmit numerical signals over a network to the optical ta-
 385 ble area which is about 100 meters from where the VME crate is located. The
 386 EPICS slow control program is used for regulating and activating the entire
 387 system from the workstation in the control room. It allows real-time control of
 388 analog and digital inputs and outputs to the various crates and modules. The
 389 VME crate houses the following cards: an ICV150 card that measures the volt-
 390 ages of the control signals (PDR, PDT, fast ramp, slow ramp); an ICV196 card
 391 that provides the digital interface between the electronic-card sequencer and
 392 the control screens by sending and receiving transistor-transistor logic (TTL)
 393 signals; and an MV712 card that allows RS-232 commands to control devices
 394 such as the laser, the PPLN temperature controller and the fiber amplifier. A
 395 servo motor controller is used for controlling the steering mirrors M_1 , M_2 and

the focusing lens L_3 . Beam position variations are monitored with two quadrant cell photodiodes, noted as $4Q_1$ and $4Q_2$, that detect a small amount of transmitted light ($< 0.1\%$) behind M_{r2} and M_e . The analog signals read by their electronics are fed to the ICV150 card and monitored by the control system. Each quarter wave plate (QWP_1 , QWP_2) is controlled by a separate stepper motor controller (KS491-2P, Suruga Seiki). With the help of the slow control interface, we can control the entire locking assembly from the workstation: the locking threshold level, the servo loop gain, the state of the feedback loop and the laser frequency scan program.

3.5. Cavity performance

Once the optical cavity is installed in the electron beam line, it is important to check various parameters (such as cavity finesse F , bandwidth $\Delta\nu_c$ and the intra-cavity power P_c) that are essential to the performance of an operational cavity. Two methods have been employed to characterize the cavity: a graphical method and a decay-time measurement method.

The graphical method analyzes the shape of the cavity resonance waveforms (transmission, reflection and error signals) while the seed laser frequency is being scanned by a triangular ramp voltage applied to the laser PZT. In this method, we first determine the FWHM of the reflection/transmission peak that corresponds to the cavity bandwidth. Then, one converts from time units to frequency units by setting the gap, $2\Delta T = |T_1| + |T_2|$, between the two sidebands (T_1 , T_2) equal to twice the modulation frequency Ω . Fig. 13 shows a theoretical fit [30] to the transmission (Fig. 13(a)) and reflection (Fig. 13(b)) signals that are used to extract the cavity bandwidth and therefore the cavity finesse. The measurement shows that the cavity exhibits a typical bandwidth of ~ 13 kHz with a corresponding finesse of $\sim 13,300$. Since the typical width of the resonance is ~ 0.04 nm, the measurement is susceptible to external disturbances and fluctuates for each measurement. In addition, due to a hysteresis exhibited in the laser PZT, the modulation sidebands would not be symmetric around the main peak as shown in Fig. 13. Therefore, the finesse measured in

Fig. 13: A theoretical fit [30] (red line) to the transmission (a) and reflection (b) signals used to extract the cavity bandwidth when the cavity is on resonance. A typical error signal (c) of the PDH feedback control is also used to convert the time units to the frequency units in order to calculate the cavity finesse.

426 this method has a large error at the order of 10% – 20%.

427 Once the laser beam and cavity are aligned with respect to each other,
 428 the laser frequency can be locked to the fundamental cavity resonance mode
 429 via its feedback system. Fig. 14 shows a digital oscilloscope trace that includes
 430 waveforms corresponding to the locked (feedback on) and unlocked (feedback
 431 off) states of the cavity. In the cavity decay-time measurement method, while
 432 the cavity is locked, we switch off the laser diode and immediately record the
 433 transmitted power via a fast photodiode (S1223; Hamamatsu) and a digital os-
 434 cilloscope (TDS3054B; Tektronix). For a high-finesse cavity, the cavity decay

Fig. 14: The digital oscilloscope traces are, from top to bottom, power reflected at the entrance of the cavity (cyan), the power transmitted by the cavity (blue), the PDH error signal (magenta) used for generating the fast feedback signal (green) that is given to the laser PZT. The trace shows cavity locking signals corresponding to locked and unlocked states of the cavity.

time T_d is directly related to the cavity parameters by [36, 37],

$$T_d \approx \frac{FL_c}{\pi c} = \frac{1}{2\pi\Delta\nu_c}, \quad (4)$$

where L_c is the cavity length and c is the speed of light. Here, it is necessary to take into account the decay time of the laser diode (T_l) itself in order to determine T_d correctly. Fig. 15 shows a typical cavity decay curve measured (black dots) for the optical cavity and an exponential fit [37] (red line) to extract the decay time. Here, after correcting the fitted value of the decay time to the measured laser decay time ($6 \mu s$) [14] and taking the sampling error of the oscilloscope as $0.5 \mu s$, we have $T_d = 11.40 \pm 0.5 \mu s$ with the corresponding $F = 12,637 \pm 554$ and $\Delta\nu_c = 14.00 \pm 0.32$ kHz from this measurement.

Now that T_d and $\Delta\nu_c$ are determined, the maximum cavity enhancement ($G_{\max}$), optical coupling of laser fundamental mode to the cavity (α) and mirror characteristics such as loss (γ) and transmittance (T) need to be calculated to determine the intra-cavity power. Based on the theoretical models described in Refs. [14, 38, 39], cavity parameters can be determined from several external

Fig. 15: Decay curve of the intra-cavity power. The exponential curve [37] (red line) is fitted to the transmitted power of the cavity (black dots) to extract the cavity decay time. The finesse is corrected for the laser diode decay time of 6 μ s.

Table 1: Characterization of the cavity parameters for a typical run during the PREx experiment.

Parameters	Symbol	Value	Unit
Incident Laser Power:	P_i	1.24 ± 0.012	W
Transmitted Power:	P_t	0.75 ± 0.007	W
Cavity Decay Time:	T_d	11.40 ± 0.50	μ s
Finesse:	F	12600 ± 550	
Cavity Bandwidth:	$\Delta\nu_c$	14.00 ± 0.32	kHz
Optical Coupling:	α	0.79 ± 0.08	
Loss Ratio:	β	0.14 ± 0.013	
Mirror Transmittance:	$T = \frac{\pi}{F(1 + \beta)}$	200 ± 9	ppm
Mirror Losses:	$\gamma = \frac{\pi\beta}{F(1 + \beta)}$	30 ± 3	ppm
Maximum Enhancement:	$G_{\max} = \frac{T}{(\gamma + T)^2}$	3800 ± 170	
Intra-cavity Power:	$P_c = \alpha G_{\max} P_i$	3750 ± 120	W

measurements such as the power going into the cavity (P_i), the power transmitted out of the cavity (P_t) and the power reflected from the cavity (P_r). If we ignore the power contained in modulation sidebands, the loss ratio ($\beta = \gamma/T$) of the mirrors can be written as,

$$\beta = \frac{1}{2} \left[\frac{P_i}{P_t} \left(1 - \frac{P_r^{\text{on}}}{P_r^{\text{off}}} \right) - 1 \right], \quad (5)$$

where P_r^{on} is the reflected power measured when the cavity is locked, and P_r^{off} is the reflected power measured when the cavity is unlocked. Now the optical coupling α is related to β by,

$$\alpha = \frac{P_t}{P_i} (1 + \beta)^2 \quad (6)$$

According to Fig. 14, and measured values of P_i and P_t , we can calculate β and α , which will allow us to calculate T , γ , G_{max} and P_c . Table 1 summarizes the cavity parameters measured during the PREx experiment. The stored power in the cavity is estimated to be ~ 3.7 kW with a corresponding enhancement of $\sim 3,800$. As seen in Fig. 14, the reflected and transmitted power from the cavity is extremely stable after turning on the feedback system, suggesting that there is no thermal effect due to high power photons incident on the cavity mirrors during an extended period of time.

We have described the optical, mechanical and electronic systems of our setup and have discussed the results obtained during the PREx experiment. Robust cavity locking with stable high power is essential to achieve a good signal-to-noise ratio, but in order to observe Compton scattering asymmetry and therefore measure the electron beam polarization, we have to create a highly circularly polarized photon beam at the CIP. In the following section, we describe the polarization aspects of our system.

4. Intra-cavity laser polarization

In terms of polarization, our optical setup needs to fulfill several functions such as creation of a highly circularly polarized photon beam at the CIP, switching of left- and right-circular polarization at regular intervals and monitoring

of the laser beam polarization at the CIP in situ by using a laser polarization transfer function.

4.1. Circularly polarized light

As we described in Section 3.2, the IR beam from YDFA is vertically polarized (extinction ratio: 20 dB), as is the green beam after the PPLN doubler (99.88%). As shown in Fig. 3, a well collimated beam ensures the purity of polarization states after it passes through various polarization-shaping elements, such as HWP, PBS and QWP₁. After passing through the FOI, HWP and PBS (extinction ratio: 27 dB), the polarization of the green beam is horizontal before it is converted to circular (left/right) by QWP₁ (zero-order), which is mounted on a stepper motor. The stepper motor reverses the helicity of the circular polarization at a time interval of 40 seconds.

The system must provide the highest degree of circular polarization at the CIP. It is crucial not only for a high experimental asymmetry but also to achieve a good precision in the electron beam polarization measurement. In our setup, the polarization state is controlled by the PBS and QWP₁. We have a circularly polarized beam generated after QWP₁ and the signal reflected by the cavity can be separated from the incident beam after the PBS and detected by a fast photodiode (PDR). However, we must take into account the unavoidable degradation of the polarization (birefringence) between the output of the QWP₁ and the CIP. In our setup, the main source of birefringence is the dielectric steering mirrors after QWP₁ which have a difference of $\sim 0.5\%$ between the reflection coefficients for S and P polarizations at 45° . This effect can be reduced by using a well established compensated mirror scheme for laser polarization transport [11, 14]. In this scheme, two pairs of identical 45° dielectric mirrors ($M_1 - M_{r2}$ and $M_2 - M_e$) are oriented at the same angle of incidence, but with perpendicular incident planes. In this way, the S -wave at the first mirror becomes the P -wave at the second mirror. If the mirrors are identical, then the difference in reflectivity and phase between the components is canceled after the last mirror (M_e). With this scheme, without the cavity mirrors in place, we obtained a maximum left

505 circular polarization of 99.57% for a QWP₁ angle of -50° (counter-clockwise)
 506 and a maximum right circular polarization of -98.07% for a QWP₁ angle of
 507 50° (clockwise) at the CIP. In this optimization, the initial polarization state
 508 was also adjusted by tilting the QWP₁ slightly off normal to the beam. Table
 509 2 summarizes the degree of circular polarization (*DOCP*) measurement after
 510 QWP₁ and at the CIP without cavity mirrors in place. Here, we believe the
 511 measured asymmetry of 1.5% between the two polarization states at the CIP is
 512 due to manufacturing variations in the compensating mirror coatings.

513 The highly circularly polarized laser beam at the CIP, must be monitored
 514 during the data taking of the physics experiment. Since intra-cavity param-
 515 eters are inaccessible from outside, this involves mapping a precise polarization
 516 transfer function that can extract the intra-cavity polarization from the external
 517 polarization measurement.

518 4.2. Laser polarization transfer function

519 The principle of our approach is to characterize the polarization state at
 520 the center of the cavity for a measured state of polarization at the cavity exit.
 521 The transfer function gives full information about the elements of the Jones
 522 matrix [40, 41] for a given optical system based on well known initial and final
 523 states, thus one can propagate a polarized beam through a system and calculate
 524 its final state. Similarly, a final polarization state can be back-propagated to
 525 its initial state. In our case, the transfer function allows us to determine the

Table 2: Measurement of the degree of circular polarization (*DOCP*) after QWP₁ and at the CIP without cavity mirrors.

Location	<i>DOCP</i> (%)
exit of QWP ₁	99.96 ± 0.1 (Left)
	-99.98 ± 0.1 (Right)
at the CIP (without cavity mirrors)	99.57 ± 0.1 (Left)
	-98.07 ± 0.1 (Right)

526 polarization and its orientation at the cavity center (i.e. CIP) based on the
 527 degree and orientation of the polarization measured at the cavity exit. The
 528 system we have to model is composed of two mirrors M_s and M_3 (Fig. 16).
 529 The Jones vector representing the polarization state at the cavity center $\hat{J}_{\text{CIP}}$
 530 is related to the exit polarization $\hat{J}_{\text{Exit}}$ using,

$$\hat{J}_{\text{Exit}} = [TF]^{-1} \hat{J}_{\text{CIP}}, \quad (7)$$

531 where $[TF]$ represents the transfer function between them. $[TF]$ is a 2×2 com-
 532 plex matrix which includes information about the phase shift δ upon reflection
 533 on the mirror, the polarization orientation rotation θ introduced by a mirror
 534 with respect to the axis Ox (Fig. 16) and another rotation angle ϕ caused by
 535 any change of orientation of the coordinate frame. The characteristic transfer
 536 matrix of a dielectric mirror is represented by the product of associated matrices
 537 [42],

$$M(\delta, \theta, \phi) = P(-\theta) R(\delta) P(\theta) T(\phi), \quad (8)$$

538 and the total transfer function of a system composed of two mirrors (M_s and
 539 M_3 in Fig. 16) is,

$$[TF] = [M_s(\delta_s, \theta_s, \phi_s) M_3(\delta_3, \theta_3, \phi_3)], \quad (9)$$

540 and $\hat{J}_{\text{CIP}}$ is calculated by,

$$\hat{J}_{\text{CIP}} = [TF] \hat{J}_{\text{Exit}} \quad (10)$$

541 As seen from Eq. (9), for a system with two dielectric mirrors, six parameters
 542 characterize its full transfer function. We begin by preparing a set of polariza-
 543 tion states with a well known *DOCP* and ellipse angle at the CIP and then
 544 measure the corresponding polarization state at the cavity exit. Once we have
 545 the initial and final state vectors based on these states with orientations cover-
 546 ing the range from 0° to 180° , theoretically we have enough equations to solve
 547 and determine the parameters.

548 The experimental determination of the polarization transfer function in-
 549 volves breaking the cavity vacuum, removing the cavity mirrors and conducting

Fig. 16: Propagation of polarization ellipse from the CIP to the cavity exit line. The schematic illustrates a case in which the cavity between the two stands is removed.

Table 3: A comparison between the measured values of $DOCP$ and θ at the CIP without cavity mirrors and those calculated from the exit line measurement with cavity mirrors are in place. The measurement corresponds to the case when the QWP_1 angles were set at $50^\circ/-50^\circ$ giving a nominal left/right polarization state at the CIP.

CIP (Measured)		CIP (Calculated)	
$DOCP$ (%)	θ (deg)	$DOCP$ (%)	θ (deg)
99.57	58.60	99.26	83.52
-98.07	19.35	-97.59	17.50

Exit (Measured)	
$DOCP$ (%)	θ (deg)
95.93	-61.05
-97.32	16.21

Fig. 17: A contour map of the transfer function for the left (a) and right (b) circularly polarized states of the CIP with respect to the exit polarization states. The Exit *DOCP* was zoomed in to between $\pm 83\%$ to $\pm 100\%$ for illustration purposes. The numbers corresponding to blue (a) and red (b) dots in figures are the values of nominal *DOCP* at the CIP based on exit polarization measurements that are also shown in Table 3.

550 a set of polarization measurements both at the CIP and cavity exit as shown
 551 in Fig. 16. A station that is composed of a Glan-Laser polarizer (extinction
 552 ratio: 50 dB) and a quarter-wave plate (zero-order) is used for generating a
 553 set of polarization eigenstates at the CIP. When we have a given polarization
 554 state with a corresponding θ , we rotate both elements (Glan-Laser polarizer
 555 and quarter-wave plate) by the same angle which leads to a rotation of θ for
 556 a fixed degree of polarization. We have started with light of $DOCP = \pm 92\%$
 557 with various orientations ($10^\circ - 170^\circ$) at the CIP by rotating both the polarizer
 558 and the quarter-wave plate with a step size of 20° [26]. The corresponding final
 559 polarization state ($DOCP, \theta$) at the cavity exit was measured at the analysis
 560 station (Fig. 9) by using a rotatable quarter-wave plate (QWP_2), a Wollaston
 561 prism and two photo detectors (S_1 and S_2) that are mounted on integrating
 562 spheres. A total of 18 data sets were used in a ROOT [43] script to extract the
 563 transfer function parameters for mirrors M_s and M_3 . Fig. 17 shows contour
 564 maps of the transfer functions for the left and right circularly polarized states

Fig. 18: The evolution of $DOCP$ for the left- (a) and right-circularly (b) polarized state at the cavity exit was monitored over 7 hours during the PREx experiment.

565 obtained from these measurements. We have also used an auxiliary set of data
 566 measured for the circular polarization states of $\pm 97\%$ with θ being $10^\circ - 170^\circ$
 567 to validate the transfer function. The uncertainty in validation of the transfer
 568 function is,

$$\frac{\Delta DOCP_{CIP}}{DOCP_{CIP}} = \left| \frac{DOCP_{CIP}^m - DOCP_{CIP}^c}{DOCP_{CIP}^c} \right| \quad (11)$$

569 where $DOCP_{CIP}^m$ and $DOCP_{CIP}^c$ are the measured and calculated values of
 570 $DOCP$ at the CIP respectively. The calculation shows that using $\pm 97\%$ data
 571 gives an average uncertainty of $\Delta DOCP_{CIP}/DOCP_{CIP} = 0.12\%$ in determina-
 572 tion of $DOCP$ for a series of polarization states of $DOCP = \pm 97\%$.

573 With the parameters extracted and validated with good precision ($< 0.5\%$),
 574 the transfer function is fully established and can be used to determine the CIP
 575 polarization from any exit polarization state for a running cavity.

576 4.3. Determination of intra-cavity polarization

577 As shown in Eq. (1), the precision in the measurement of P_e depends on
 578 the accuracy of P_γ . Several factors can affect the accuracy of P_γ , such as the
 579 transfer function, the stability of intra-cavity polarization, the beam alignment
 580 and the birefringence of the optical elements.

581 Table 3 shows a comparison between the measured values of $DOCP$ and
 582 θ at the CIP without cavity mirrors and the values predicted from the exit

583 line measurement with cavity mirrors in place. The measurements correspond
 584 to the case when QWP₁ angles were set at 50°/-50°, giving nominal left/right
 585 polarization states at the CIP. The incoming beam alignment to the cavity was
 586 kept the same during operation of the cavity as when the transfer function was
 587 measured. We have validated the transfer function for the nominal polarization
 588 state at the CIP (99.57%, -98.07% in Table 3) created by QWP₁ by comparing
 589 the measured and calculated values of *DOCP* at the CIP. The largest uncer-
 590 tainty in the calculation of the nominal *DOCP* from the transfer function is
 591 calculated according to Eq. (11) and $\Delta DOCP_{CIP}/DOCP_{CIP} = 0.49\%$. We
 592 believe that this uncertainty is mostly originating from various sources of bire-
 593 fringence in our system.

594 Birefringence induced by multi-layer coatings of the cavity mirrors [44–46]
 595 can be estimated according to the measured finesse. For our case, the maxi-
 596 mum birefringence induced by multilayer cavity mirror coatings is estimated to
 597 be $\sim 10^{-4}$ rad for a measured finesse of $\sim 13,000$. This effect causes $\pm 0.1\%$
 598 change between the two polarization states in *DOCP* inside the cavity. The
 599 birefringence coming from the cavity mirror substrate was studied by measur-
 600 ing the difference in polarization of the signal transmitted through an uncoated
 601 substrate, and no degradation of polarization was observed.

602 We have measured the *DOCP* of the incoming laser beam before and after
 603 the vacuum window (W_e and W_s in Fig. 12) without vacuum and the differ-
 604 ence was negligible. However, when the cavity is under vacuum (10^{-9} Torr),
 605 there could be a birefringence coming from the pressure difference between air
 606 and vacuum [47]. Since the measurement of the transfer function can only be
 607 accomplished without cavity mirrors or vacuum it was not possible to evaluate
 608 this effect.

609 The stability of the intra-cavity polarization is crucial to achieve precision
 610 Compton polarimetry. A thermoelastic deformation of cavity mirrors due to
 611 high power circulating inside the cavity could cause birefringence [48]. While
 612 the cavity is locked, we monitored the long-term stability of the exit line po-
 613 larization online. Fig. 18 shows a measurement for left- and right-circular

614 polarization states monitored over 7 hours. The data indicates that the varia-
615 tions are at the order of 0.03%.

616 Other sources of systematic errors include the measurement of exit line po-
617 larization ($DOCP$ and θ) and beam alignment by steering mirrors (M_1 and M_2
618 in Fig. 12) to maximize the light coupling to the cavity is listed in Table 4.

619 After taking into account all the systematic errors described, the total sys-
620 tematic error in the determination of the intra-cavity laser polarization was es-
621 timated to be 0.70%. The averaged statistical errors during three-month period
622 of the PREx experiment were 0.1% and 0.13% for the left- and right-circularly
623 polarized states respectively. Based on the transfer function measurement, the
624 average left- and right-laser polarizations ($P_\gamma = DOCP_{CIP}$) with uncertainties
625 during the PREx experiment are summarized as $P_\gamma^L = 99.26\% \pm 0.70\%$ (sys) $\pm$
626 0.10% (stat), $P_\gamma^R = -97.59\% \pm 0.70\%$ (sys) $\pm 0.13\%$ (stat).

627 So far we have discussed how to make a reliable photon target with a pure
628 circular polarization inside a high-finesse optical cavity for the electron beam so
629 that there is efficient Compton scattering. The green cavity has been combined
630 with the photon arm [24] of the upgraded Compton polarimeter to continuously

Table 4: Summary of systematic errors on the measurement of the laser polarization at the CIP during the PREx experiment.

Source of Error	(%)
Validation of transfer function	0.49
Transmitting through M_{ce}	0.10
Transmitting through M_{cs}	0.10
Variation in time	0.03
Variation of $DOCP$ at exit line	0.02
Variation of θ at exit line	0.13
Beam alignment to the cavity	0.10
Total	0.70

631 measure the electron beam polarization.

632 5. Electron beam polarization measurement

633 The electron beam polarization measurement can be achieved by one of the
 634 three ways at the down stream of the optical cavity: detecting the backscattered
 635 Compton photons, detecting the scattered Compton electrons, and detecting
 636 both the Compton photons and Compton electrons simultaneously. At the time
 637 we commissioned our laser system and cavity, the electron detector had not
 638 been fully commissioned and there is no way to detect the scattered Compton
 639 electrons. Therefore, the results presented here are solely based on the data
 640 from the upgraded photon detector and DAQ that are described in Ref. [24]. In
 641 the following section, without going into the details, we will briefly present the
 642 results of the electron beam polarization measurement conducted for the first
 643 time during the PREx experiment with electron beam parameters of 1.06 GeV
 644 and $50 \mu\text{A}$ [1].

645 5.1. Compton spectrum

646 The upgraded Compton polarimeter measures the electron beam polariza-
 647 tion based on the detection of scattered Compton photons during electron he-

Fig. 19: Scattered Compton photon rates (red) along with the background rates (black), where each point is measured at an accelerator helicity timing signal (called the MPS signal) for a given accelerator helicity setting during a run.

648 helicity reversal at a rate of 120 Hz [49]. The helicity of the electron beam at
 649 JLab can be flipped at a rate of between 1 ms to 33 ms at the injector with a
 650 pseudo-random pattern. Fig. 19 shows the scattered photon rates versus accel-
 651 erator helicity timing signal (called the MPS signal) measured with the photon
 652 detector for an electron beam energy and current of 1.06 GeV and 50 μ A. Dur-
 653 ing the data taking, the laser polarization is flipped periodically between right-
 654 and left-circular state and the cavity is locked for ~ 90 seconds in each polar-
 655 ization state. Between each polarization state, the cavity is out of resonance
 656 for ~ 40 seconds to measure the background rate, which is subtracted from the
 657 signal rate measured when the cavity is locked. Lower background rates can
 658 be achieved by several steps. Low vacuum pressure in the cavity (10^{-9} Torr
 659 in our case) can reduce the scattering between electron beam and residual gas.
 660 Properly controlling the electron beam parameters upstream and carefully cen-
 661 tering and focusing the beam at the interaction point is a key to achieve low
 662 background rates. During background rate optimization, the electron beam is
 663 scanned vertically until it crosses the photon beam at the CIP by using all four
 664 dipoles connected in series to the power supplies in the Compton chicane (Fig.
 665 1).

666 The Compton photon energy spectrum is measured using the triggered
 667 mode of the DAQ. In this readout mode, a discriminator with a very low thresh-
 668 old is used to trigger a readout of the FADC samples over a 500 ns window,
 669 allowing study of the sampled pulse shape and size. The sum of samples in
 670 the pulse represents the total energy deposited in the GSO crystal for each de-
 671 tected photon. This energy spectrum is plotted in (Fig. 20), with the horizontal
 672 axis in raw ADC units. To determine the experimental Compton asymmetry
 673 A_{exp} , the measured ADC response is calibrated to the well known Compton
 674 scattering photon energy spectrum and the result is compared to a full Monte
 675 Carlo simulation of the photon detector by GEANT4 [50]. After confirming
 676 good agreement with data, this same simulation is then used to calculate the
 677 theoretical asymmetry A_{th} in Eq. (1).

678 *5.2. Compton asymmetry*

679 The integrating photon detector DAQ (as described in Ref. [24]) sums the
 680 FADC samples over the entire period of stable beam helicity between flips, using
 681 a gate supplied by an accelerator timing board. These integrated signals (S)
 682 are used to calculate the asymmetry A_{exp} as:

$$A_{\text{exp}} = \frac{S^+ - S^-}{S^+ + S^-}, \quad (12)$$

683 for each laser helicity period with separate sums of integrals for all electron
 684 helicity ($\pm$) windows. A separate sum and difference of integrated signals for
 685 the adjacent cavity-unlocked periods, $B = (S^+ - S^-)_{\text{unlocked}} / (S^+ + S^-)_{\text{unlocked}}$,
 686 used to determine background for the cavity-locked period. After taking into
 687 account the background and helicity-dependent electron beam parameters at
 688 the accelerator source, Eq. (12) becomes,

$$A_{\text{exp}} = \frac{\langle M^+ \rangle - \langle M^- \rangle}{\langle M^+ \rangle + \langle M^- \rangle - 2\langle B \rangle}, \quad (13)$$

689 where $\langle \rangle$ denotes the mean integral per helicity window over each cavity (locked/unlocked)
 690 period. Here, $M^\pm$ is the measured integrated signal with the laser locked, and
 691 includes both the Compton-scattered signal $S^\pm$ and the background signal B .

Fig. 20: Measured Compton photon energy spectra correspond to cavity locked (black), cavity unlocked (red) and background-subtracted (blue) cases. The first two cases (black and red) are out of the vertical scale in order to show the background-subtracted Compton spectrum (blue).

Fig. 21: Histogram of a background-subtracted Compton asymmetry taken for every electron helicity pair in a single one hour run. Colors represent right circular (red), left circular (blue) and cavity unlocked (black) cases.

Fig. 22: Asymmetry versus left- (blue) and right-circularly (red) polarized laser cycles for an entire run. An average asymmetry is used for calculating the electron beam polarization for a typical run.

692 A_{exp} can be extracted separately for each laser polarization using one of the
 693 three averaging techniques discussed in Ref. [24]. Fig. 21 shows a histogram of
 694 a background-subtracted Compton asymmetry taken for every electron helicity
 695 pair in a single one hour run.

5.3. Electron beam polarization

The electron beam polarization is continuously monitored by the Compton polarimeter during the PREx experiment. As we described in Section 1, the electron beam polarization P_e is extracted from the measured experimental asymmetry A_{exp} , the laser polarization P_γ and the theoretical asymmetry A_{th} , according to Eq. (1). Fig. 22 shows the electron beam polarization measurement based on an average of two experimental asymmetry numbers obtained for the left and right laser cycles during a typical run. The average experimental asymmetry corresponding to the left and right laser cycles for this run are $-1.59\% \pm 0.02\%$ (stat) and $1.56\% \pm 0.02\%$ (stat). After taking the value of A_{th} as 1.825% and using the asymmetry numbers above, the extracted average electron beam polarization for this run is $87.40\% \pm 0.70\%$ (stat).

Finally, after taking into account all the uncertainties in other parameters (such as laser polarization, theoretical asymmetry, photon detector gain shift etc.), the average beam polarization measured by the Compton polarimeter during the PREx experiment is $P_e = 88.20\% \pm 0.12\%$ (stat) $\pm 1.04\%$ (sys). It was compared with an independent Møller polarimeter measurement made at different times during the run which gave an average $P_e = 90.3\% \pm 0.1\%$ (stat) $\pm 1.1\%$ (sys) [1]. The observed difference in electron beam polarization is consistent within the systematic errors between the two measurements.

6. Conclusions

The green Fabry-Perot cavity provided Hall A of JLab with a unique laser source to carry out precision Compton polarimetry. After combining with the upgraded Compton DAQ and photon detector [24], it extends the operating energy range of the previous Compton polarimeter [22] from 3 – 11 GeV to 1 – 11 GeV. High-precision electron beam polarimetry was tested for the first time at JLab with beam energy and current of 1.06 GeV and 50 μA , and achieved its 1.0% precision goal for the PREx experiment. The system we developed allows us to obtain a reliable intra-cavity power and stable photon beam polarization

725 for the long-term operation of the upgraded Compton polarimeter. The cavity
 726 mechanical and locking stability was excellent during the three-month period of
 727 the PREx experiment, despite the concern of a very high-radiation and acousti-
 728 cally noisy environment in Hall A at JLab. The frequency-doubled green laser
 729 power was stable indicating that the PPLN crystal could withstand high power
 730 for an extended period of time.

731 The frequency locking of the green laser generated by seeding the Nd:YAG
 732 NPRO laser to the YDFA makes the intra-cavity power scalable. This allows a
 733 possibility of boosting the intra-cavity power further (10 kW or more at 532 nm)
 734 by increasing the injection power to the cavity provided there is no thermal prob-
 735 lem in the cavity mirrors. A higher intra-cavity power may also be achievable by
 736 replacing the current cavity mirrors with higher finesse mirrors which is possible
 737 with the current feedback electronics. Regarding the intra-cavity laser polariza-
 738 tion, it is one of the dominant errors in our polarimeter with an uncertainty of
 739 0.7%. It is dominated by our ability to through direct measurement, effects that
 740 might alter the polarization over the numerous re-circulations within the cavity.
 741 Other factors include analyzing power and photon detector gain shift can also
 742 affect the systematic errors in the final electron beam polarization [24]. Recent
 743 studies at HERA [20] and JLab Hall C [7] show that it is possible to get $< 0.3\%$
 744 level precision for the intra-cavity laser polarization with proposed techniques.
 745 So far this result is only based on scattered photon analysis. This measurement
 746 could be combined with an independent electron analysis as demonstrated in
 747 Hall C at JLab with a reported precision of 0.6% [7]. All of this encourages us
 748 that, with a careful and dedicated study, it should be feasible to get $< 0.5\%$
 749 precision at electron beam energies below 2 GeV.

750 Future high-precision parity-violating electron scattering experiments at JLab,
 751 such as the MOLLER [51], PVDIS [52], PREx-II [53], and CREx [54] experi-
 752 ments, also require electron beam polarimetry with sub-1% precision and would
 753 rely on the green Compton polarimeter we built. This requires an improvement
 754 of the current precision by at least a factor of two. Finally, a Compton polarime-
 755 ter with a mode-locked pulsed-laser-based optical cavity [55, 56] would give a

756 much higher signal-to-noise ratio in scattered Compton events and would make
757 the system even more robust and efficient, especially in the more noisy electron
758 beam environment expected [57] after the upgrade of the CEBAF energy to
759 12 GeV.

760 Acknowledgements

761 The authors wish to thank the Hall A technical staff for their assistance
762 in installing the upgraded system and the JLab Accelerator Division for their
763 efforts to achieve and maintain the high electron beam quality necessary for
764 running the Compton polarimeter. This work is supported by DOE grants
765 DE-AC05-06OR23177, under which Jefferson Science Associates, LLC, operate
766 Jefferson Lab, and DE-FG02-84ER40146.

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