Cloud Enhancement of Global Horizontal Irradiance in California and Hawaii

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Abstract

Clouds significantly attenuate ground-level solar irradiance causing substantial reduction in photovoltaic power output capacity. However, partly cloudy skies may lead to temporary enhancement of local Global Horizontal Irradiance (GHI) above the clear-sky ceiling and, at times, the extraterrestrial irradiance. Such enhancements are referred to here as Cloud Enhancement Events (CEEs). In this work we study these CEEs and assess quantitatively the occurrence of resulting coherent Ramp Rates (RRs). We analyze a full year of ground irradiance data recorded at the University of California, Merced, as well as nearly five months of irradiance data recorded at the University of California, San Diego, and Ewa Beach, Hawaii. Our analysis shows that approximately 4% of all the data points qualify as potential CEEs, which corresponds to nearly 3.5 full-days of such events per year if considered sequentially. The surplus irradiance enhancements range from $18 \text{ W m}^{-2} \text{ day}^{-1}$ to $73 \text{ W m}^{-2} \text{ day}^{-1}$. The maximum recorded GHI of $\sim 1,400 \text{ W m}^{-2}$ occurred in San Diego on May 25, 2012, which was nearly 43% higher than the modeled clear-sky ceiling. Wavelet decomposition coupled with fluctuation power index analysis shed light on the time-scales on which cloud induced variability and CEEs operate. Results suggest that while cloud-fields tend to induce variability most strongly at the 30 minute time-scale, they have the potential to cause CEEs that induce variability on time-scales of several minutes. This analysis clearly demonstrates that CEEs are an indicator for periods of high variability and therefore provide useful information for solar forecasting and integration.

Keywords: Global Horizontal Irradiance; Cloud Enhancement; Total Sky Imager.

1. Introduction

The total extraterrestrial beam irradiance incident on the earth's atmosphere I_0 fluctuates about an average value of approximately $1,360 \text{ W m}^{-2}$ (Kopp and Lean, 2011). This incident radiation is attenuated as it negotiates its way to ground level through a complex series of multiple reflections, absorptions and re-emissions due to interactions with atmospheric constituents (Goody and Yung, 1995). This results in the division of the incident extraterrestrial beam radiation into two distinct components; Direct Normal Irradiance (DNI) and Diffuse Horizontal Irradiance (DHI), the geometric sum of which is

the Global Horizontal Irradiance (GHI), defined by the closure equation,

$$\text{GHI} = \text{DNI} \cos \theta_z + \text{DHI} \quad (1)$$

where θ_z is the solar zenith angle, see Figure 1.

In addition to the partitioning of the radiation, atmospheric cloud-formation is typically associated with a pronounced decrease in the intensity of solar irradiance components. In fact, the attenuation of incoming solar radiation by clouds is routinely larger than any other atmospheric component (Inman et al., 2013). Furthermore, the driving effects of clouds on radiative energy budgets include short wave cooling, as a result of absorption of incoming solar radiation, and long wave heating, due to reduced emission of thermal radiation by relatively cool cloud tops (Schade et al., 2007). However, partly cloudy skies

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Figure 1: Components of solar irradiance sampled every 30 seconds at the University of California, Merced, on March 21, 2011. Global Horizontal Irradiance (GHI) was measured with a Precision Spectral Pyranometer (PSP), manufactured by the Eppley Laboratory, Inc. Direct Normal Irradiance (DNI) was measured using a Normal Incidence Pyrheliometer (NIP) and 2-axis automatic solar tracker (SMT-3), both of which are also available from the Eppley Laboratory, Inc. Diffuse Horizontal Irradiance (DHI) was measured using an additional PSP and SMT-3 with accompanying Shade Disk Kit (SDK). Solar zenith angle is also plotted and observations with $\cos \theta_z \leq 0.3$ ($\theta_z \geq 72.5^\circ$), shown outside solid red-lines, being excluded from the study. The Clear-Sky Model (CSM) used in this figure is explained in detail in §3.2.

may lead to the reverse; i.e., multiple scatterings and reflections of short wave radiation by cloud fields may lead to increased irradiance from a portion of the sky above the corresponding cloud-free value (Franceschini, 1968; Wen et al., 2001; Wyser et al., 2002; Pfister et al., 2003; Emck and Richter, 2008; Berg et al., 2011). In rare occasions, these enhancements can cause the local GHI to instantaneously exceed the extraterrestrial solar constant I_0 (McCormick and Suehrcke, 1990; Tapakis and Charalambides, 2014). Such enhancement of GHI above the corresponding clear-sky value are referred to here as Cloud Enhancement Events (CEE).

With the exception of two studies, one by Luoma et al. (2012) and a second by Tapakis and Charalambides (2014), little work has been done in the realm of CEEs with respect to PhotoVoltaic (PV) power generation. In this work we do not intend to suggest a new mechanism by which CEEs occur, but rather investigate the coherent Ramp Rates (RRs) associated with CEEs and their potential impact on the quality of PV power generation. To clarify, a coherent CEE RR is defined as

a series of monotonically increasing or decreasing GHI observations whose maximum value exceeds the expected clear-sky value by a given threshold. These CEEs and their associated RRs are of interest for several reasons: current models typically do not consider the ability of clouds to increase the local available irradiance, these events commonly precede or follow periods of lower than normal irradiance associated with the presence of passing opaque clouds leading to relatively large RRs, large RRs can cause voltage flicker that in turn trigger tap chargers on distribution feeders increasing operations cost for utilities, and therefore the successful forecasting of these events could lead to an effective control scheme to reduce the cost associated with high levels of variability in photovoltaic power generation.

Analysis of the amplitude, persistence, and frequency occurrence of ground-level irradiance fluctuation requires a decomposition of the input time-series into a set of orthogonal sub-signals each representing a specified time-scale of fluctuation. Due to the stochastic and non-periodic nature of the atmo-

spheric processes that drive ground-level fluctuations in clearness, Fourier analysis is typically not suitable. Alternatively, spectral analysis of high frequency (e.g., 1 s - 1 min) irradiance time-series on a wavelet basis rather than a periodic basis can be found in the literature. Kawasaki et al. (2006) decomposed 2-10 years of 1-min irradiance data from 9 sites in a 4x4 km grid using the Daubechies 4 wavelet (Hazewinkel, 2001). Woyte et al. (2007) applied the Haar (1911) wavelet to clearness index time-series and defined a fluctuation power index (fpi) that quantified the amplitude and frequency occurrence of variability on specified time-scales. Perpiñán and Lorenzo (2011) analyzed several days of 1 s irradiance time-series using the MOD-WT wavelet and later used wavelet transform correlations to study fluctuations of the electrical power generated by an ensemble of 70 DC/AC inverters from a 45.6 MW PV plant (Perpiñán et al., 2013). Lave et al. (2012) applied a wavelet transform to clear-sky index time-series from a single site to the average of six sites and showed a strong reduction in variability at short time-scales (i.e., shorter than 5-min) with lesser reductions at longer time-scales. Lave et al. (2013) also developed a wavelet-based variability model for PV plant output and Lave et al. (2013) employed the wavelet-based model to study the impact of cloud speed on solar variability scaling. Similarly, Peled and Appelbaum (2013) used statistical tools and wavelet analysis to develop estimators for the magnitude of voltage and power variations within PV systems due to climatic conditions.

The time-scales of these events have been shown to range from seconds (Schade et al., 2007), to 15-30 mins (Segal and Davis, 1992; Tapakis and Charalambides, 2014), and occasionally as long as hours (Cede et al., 2002). Here we employ a wavelet decomposition using the top-hat wavelet to show that while the CEE RRs typically only last a few minutes they are generally correlated with variability on longer time-scales associated with the passing of cloud fields.

This study makes use of a full year of irradiance data recorded at the University of California, Merced, as well as nearly five months of irradiance data recorded at the University of California, San Diego, and Ewa Beach, Hawaii, see §2. Methods

are described in §3 which includes descriptions of the clear-sky model, statistical analysis, ramp rate calculation, wavelet decomposition, and fluctuation power index analysis. The results of these analyses are covered in §4 and the conclusions in §5 respectively.

2. Data

2.1. Irradiance Data

Irradiance data are collected at three locations characterized by different micro-climates: Merced California (continental), San Diego California (coastal), and Ewa Beach Hawaii (island). A broadband (285 - 2,800 nm) Eppley Precision Spectral Pyranometer (PSP) and Normal Incidence Pyrheliometer (NIP) are used in Merced (Mar. 21, 2011 to Jun. 19, 2012) to collect GHI and DNI data, respectively. Two Multi-Filter Rotating Shadowband Radiometers (Model MFR-7), available from Yankee Environmental Systems (YES), which measure both GHI and DNI are used to collect irradiance data in San Diego and Ewa Beach during the period from Jan. 27, 2012 to Jun. 17, 2012. Irradiance data are logged using Campbell Scientific CR-1000 data-loggers at a sampling rate of 30 seconds. It is important to note that due to the 30 second sampling rate used in this study the observed RRs are likely lower than what would be observed with an increased sampling rate, see for example Yordanov et al. (2013)a, Yordanov et al. (2013)b, and Almeida et al. (2014).

2.2. Selection of GHI

This work focuses on GHI rather than DNI due to the nature of the cloud enhancement process. CEEs are necessarily observable in the diffuse component of irradiance and manifest in the global component of irradiance as a result of Eq. (1). This is because CEEs result from clouds elevating short wave diffuse irradiance above that of the corresponding clear-sky value with little or no change in DNI, which is illustrated through an analysis of DNI clear-sky indices,

$$k_D(t) = \frac{DNI(t)}{DNI_{clr}(t)} \quad (2)$$

Figure 2: Scatter plots of k_D versus k_G for irradiance measurements in Merced, CA (left); San Diego, CA (center); and Ewa Beach, HI (right). Each marker stands for a single observation. Red markers represent GHI CEE cases and the dash lines represent the 1.05 threshold for both k_D and k_G .

Table 1: Correlation coefficients between DNI clear-sky indices and GHI clear-sky indices for overall, non-CEE, and CEE periods at different locations.

	Correlation coefficient		
	Overall	Non-CEE	CEE
Merced	0.9	0.92	0.07
San Diego	0.9	0.91	-0.16
Ewa Beach	0.94	0.95	-0.03

and GHI clear-sky indices

$$k_G(t) = \frac{\text{GHI}(t)}{\text{GHI}_{\text{clr}}(t)} \quad (3)$$

where $\text{GHI}_{\text{clr}}(t)$ and $\text{DNI}_{\text{clr}}(t)$ are generated from the Clear-Sky Model (CSM) described in §3.2. As shown in Figure 2, k_D generally increases with k_G for non-CEE periods and typically results in correlation coefficients greater than 0.9, which is to be expected (see Table 1). On the other hand, during CEE periods, the correlation between k_D and k_G is low and in some cases negative (see Table 1). It is also clear that during CEE periods, k_G is typically in the range of 1.05-1.5 while k_D tends to occupy the range from 0.5-1.0. It is also important to note that there are some occasions where k_D did exceed 1.05, however, such enhancement was found to result from errors in the DNI CSM at elevated zenith angles under cloudless skies and, as a result,

were excluded from the study.

3. Methods

3.1. Data Quality

Data from the early morning and late afternoon are excluded from the analysis. There are several motivations for their removal: primarily, the cosine response of pyranometer measurements are typically maximized for $\theta_z \gtrsim 70^\circ$; secondly, times when $\theta_z \gtrsim 70^\circ$ are associated with a relatively high airmass resulting in a large fraction of GHI originating from the diffuse component; and finally, the high solar zenith angle in combination with an elevated airmass results in rather low photovoltaic power production. To this end, a threshold is applied to the solar zenith angle θ_z according to,

$$\cos \theta_z \geq 0.3, \quad (4)$$

with data not satisfying Equation (4), which corresponds to $\theta_z \geq 72.5^\circ$, being removed from the data set, see Figure 1.

Furthermore, in order to avoid erroneous observation of CEEs resulting from reflections from local surfaces, a quality filter based on the summation method to obtain GHI was used (Gueymard and Myers, 2009). This filter calculates GHI from Equation (1) and compares it against the independently observed GHI. Observations where the ratio of calculated and observed GHI differ from 1.0 by more than 0.2 were excluded as they

typically correspond to an error in the observation of at least one irradiance component.

3.2. Clear-Sky Model

In addition to the measured irradiance data, a Clear-Sky Model (CSM) is used to characterize events that exceed the clear-sky ceiling. The clear-sky GHI is modeled using the CSM developed by Ineichen and Perez (2002), which requires Linke Turbidity as an input. Maps of monthly average Linke Turbidity developed by Remund et al. (2003) were used. These maps account for seasonal changes of aerosol content in the atmosphere and their performance has been confirmed internally by Sandia National Laboratories (Reno et al., 2012). The CSM was calibrated against several clear days and a linear fit is used in order to ensure agreement between measured and modeled values.

3.3. Statistical Analysis

A statistical analysis was carried out in order to characterize the individual events that exceed the CSM into bounded ranges. Only GHI measurements that exceed the CSM by at least 5% and satisfy Equation (4) are considered potential CEEs. Potential CEEs are then grouped by the degree to which they exceed the CSM (5-10%, 10-15%, etc). Statistical analysis of these subsets of CEEs provides insight into the distribution and probability of GHI measurements as a function of the degree to which they exceed the CSM.

3.4. Ramp Rate Analysis

Analysis of the RRs uses the same set of GHI data from the statistical study with data not satisfying Equation (4) or violating the quality filter being removed. As was done in §3.3, only events which exceed the CSM by a threshold of at least 5% are considered potential CEEs. However, rather than grouping the individual measurements by the range with which they exceed the clear-sky model (5-10%, 10-15%, etc), the present study employs a sliding lower bound which classifies coherent ramps by the amount with which their maximum value exceeds the CSM (>5%, >10%, etc), see Figure 5.

In order to study the coherent CEE RRs, characteristic events must be located and quantified. This was accomplished through the identification of successive measurements which lie on opposite sides of the CSM. These points were then extrapolated to their respective local maxima and minima. This is illustrated in Figure 3 in which the ramps associated with CEEs, along with their local maxima and minima, have been identified in the Eppley PSP data from March 21, 2011 in Merced. It is important to note that while raw GHI data was used to locate potential CEEs (and the degree to which they exceed the CSM) the calculation of the RRs themselves ignores deterministic diurnal variations through the removal of the CSM values as described below,

$$|RR| = \frac{(GHI_{\max} - CSM_{\max}) - (GHI_{\min} - CSM_{\min})}{\Delta t}. \quad (5)$$

3.5. Wavelet Analysis

Wavelet analysis allows for decomposition of non-periodic time-series into sets of orthogonal sub-signals representing fluctuations on specific time-scales, see for example Mallat (2009). For the purposes of the present study a wavelet similar to the top-hat wavelet employed in Lave et al. (2012, 2013) is also used here. The top-hat wavelet used here is centered at zero and is defined as,

$$\psi(t) = \begin{cases} 1 & -1/4 < t < 1/4 \\ -1 & -1/2 < t < -1/4 \parallel 1/4 < t < 1/2 \\ 0 & \text{else} \end{cases} \quad (6)$$

so that the dictionary of top-hat atoms can be written,

$$\mathcal{D} = \left\{ \psi_{\tau, 2^j}(t) = \frac{1}{\sqrt{2^{j+1}}} \psi\left(\frac{t - \tau}{2^j}\right) \right\}_{\tau \in \mathbb{R}, j \in \mathbb{Z}^+} \quad (7)$$

where the wavelet has been offset by τ and scaled by $1/\sqrt{2^{j+1}}$ in order to compensate for the total length of the wavelet. The corresponding wavelet transform is written

$$\Psi f(\tau, 2^j) = \frac{1}{\sqrt{2^{j+1}}} \int_{-\infty}^{+\infty} f(t) \psi\left(\frac{t - \tau}{2^j}\right) dt \quad (8)$$

Figure 4 shows the $\psi_{0, 2^2}(t)$ top-hat wavelet centered at zero as well as two scaled, dilated, and translated versions of the

Figure 3: Ineichen clear-sky model as well as GHI data from the Eppley PSP located in Merced for the portion of March 21, 2011 satisfying Equation 4. The local maxima and minima of the coherent ramps associated with CEEs are highlighted in red. Coherent CEE ramps are defined as a set of monotonically increasing or decreasing irradiance observations whose maximum exceed the CSM by a specified threshold.

wavelet $\{\psi_{8,2^3}(t), \psi_{24,2^4}(t)\}$. These wavelets, which have a length of 2^j , when applied to a stationary time-series of irradiance measurements would capture clear periods of length 2^{j-1} surrounded by overcast periods or vice versa.

In order to determine the power contained in each of the time-series $\Psi f(\tau, 2^j)$, a wavelet periodogram $I_j(\tau)$ is calculated. In analogy to the Fourier periodogram as well as the work by Woyte et al. (2007) and Lave et al. (2012, 2013) the wavelet periodogram is defined as the square of the wavelet transform, normalized by the period of the wavelet,

$$I_j(\tau) = \frac{[\Psi f(\tau, 2^j)]^2}{2^{j+1}} \quad (9)$$

However, information regarding the variability from the wavelet periodograms is inconvenient to examine periods longer than a day. To remedy this, a fluctuation power index as described by Woyte et al. (2007) and employed in Lave et al. (2012) is used here to characterize the amount of power included in each time-scale. The fluctuation power index (fpi) is defined as,

$$\text{fpi}(j) = \frac{1}{T_j} \int_0^{T_j} \frac{[\Psi f(\tau, 2^j)]^2}{2^{j+1}} d\tau \quad (10)$$

where T_j is the total duration of the wavelet periodogram $I_j(\tau)$. It should be noted that while all of the definitions concerning wavelet transforms have been written in the continuous sense, our dataset is discrete in nature. Therefore, discrete forms of equations (7 - 10) must be employed. The discrete forms are,

$$\mathcal{D} = \left\{ \psi_{\tau, 2^j}(t) = \frac{1}{\sqrt{2^{j+1}}} \psi\left(\frac{t-\tau}{2^j}\right) \right\}_{\tau \in \mathbb{N}, j \in \mathbb{Z}_{\geq 2}}, \quad (11)$$

$$Wf(\tau, 2^j) = \frac{\Delta t}{2 \sqrt{2^{j+1}}} \quad (12)$$

$$\left[f(0)\psi\left(\frac{-\tau}{2^j}\right) + f(N)\psi\left(\frac{N-\tau}{2^j}\right) + 2 \sum_{t=1}^N f(t)\psi\left(\frac{t-\tau}{2^j}\right) \right],$$

$$I_j(\tau) = \frac{[Wf(\tau, 2^j)]^2}{2^{j+1}}, \quad (13)$$

and

$$\text{fpi}(j) = \frac{\Delta t}{2T_j \sqrt{2^{j+1}}} \left[I_j(0) + I_j(T_j) + 2 \sum_{t=1}^{T_j-1} I_j(t) \right], \quad (14)$$

Figure 4: Illustration of the $\psi_{0,2^2}(t)$ top-hat wavelet centered at zero as well as two scaled, dilated and translated versions of the wavelet $\{\psi_{8,2^3}(t), \psi_{24,2^4}(t)\}$.

respectively, where $\mathbb{N}$ represents integers between 2^{j-1} and $N - 2^{j-1}$.

4. Results

4.1. Statistics

A plot of the entire year of GHI data from Merced along with suspected cloud enhancement events where the measured GHI exceeds the modeled clear-sky ceiling are shown in Figure

5. Allowing for errors in the measurement of GHI and modeling of clear-sky irradiance ceiling, potential enhancement events are associated with measured values which exceed the clear-sky model by at least 5%. Our analysis shows that 10,228 of the 262,281 data points, corresponding to approximately 4% of the data, qualify as potential CEEs. Multiplying the number of potential data points by 30 second time-steps corresponds to over 3.5 full-days of these events per year if considered sequentially. The surplus irradiance enhancements range from 18 $\text{W m}^{-2} \text{ day}^{-1}$ to 73 $\text{W m}^{-2} \text{ day}^{-1}$. The maximum GHI in Merced was measured on May 8th, 2011 at 12:08p.m. ($\theta_z = 20.5^\circ$) with a value of 1,365 W m^{-2} , or approximately equal to the extraterrestrial beam irradiance I_0 . This value is nearly 40% higher

than the modeled clear-sky ceiling suggesting substantial gains may result from these events.

Statistical results from the data in Merced as well as similar results for data sets collected in San Diego and Ewa Beach, are shown in Tables 2 and 3 respectively, all of which recorded maximum values of $\text{GHI} \geq I_0$. The maximum recorded GHI in San Diego of 1,396 W m^{-2} , which is 42.7% higher than the modeled clear-sky ceiling, occurred on May 25, 2012 at 12:45p.m. ($\theta_z = 17.6^\circ$). Similarly, a maximum recorded value of 1,380 W m^{-2} , which is 32.95% higher than the modeled clear-sky ceiling, occurred on April 29, 2012 in Hawaii at 12:18p.m. ($\theta_z = 7.2^\circ$). It is beneficial to note that the magnitude, mean and deviation of these potential enhancement events across all three observatories do not vary greatly. In addition, cloud enhancements in Merced are seasonally dependent and are more likely to occur in the spring months. Moreover, there are very few potential cloud enhancement events during the summer months when the skies are relatively cloudless over Merced. Due to the difference in local climatology between Hawaii and California, there are less clear skies per year in Hawaii. Consequently, cloud enhancement events are more likely to occur and provide higher surplus local energy than the other two observatories during the same season, see Table 3.

4.2. Ramp Rate Probabilities

Cumulative Distribution Functions (CDFs) of the previously defined coherent CEE RRs are shown in Figure 6. The CDF for the entire data set satisfying Equation (4) is also shown for reference and labeled as ‘Day Values’. It should be noted that, as a result of varying climates, cloud induced RRs vary by location. Cloud induced RRs resulting in a change of at least 5% in k_G for Merced, San Diego and Hawaii account for 6.86%, 15.6% and 44.3% of the data, respectively. It is clear from Figure 6 that the CEE RR distributions corresponding to increasing thresholds are quite similar. In addition, one can see that CEEs are associated with elevated RRs. Figure 6 also includes a horizontal line corresponding to $P = 0.95$. The intersection of this line with the CDFs represent the RR magnitude which is exceeded

Figure 5: Plot of the entire year of GHI data from Merced as a function of the expected clear-sky value illustrating the set of potential CEEs.

Threshold	Standard			Probability	Surplus	
	Mean	Deviation	Occurrence		Energy	
	[W m ⁻²]	[W m ⁻²]	[-]	[%]	[W h m ⁻²]	[W h m ⁻² day ⁻¹]
5 - 10%	53	16	4,238	1.62	1,850	4.06
10 - 15%	91	21	2,660	1.01	2,010	4.41
15 - 20%	125	28	1,483	0.57	1,540	3.38
20 - 25%	157	37	890	0.34	1,170	2.57
25 - 30%	195	46	575	0.22	930	2.04
≥ 30%	249	56	382	0.15	790	1.73
Total	95	58	10,228	3.9	8,300	18.19

Table 2: Statistical Results for CEE analysis for an entire time period (456 days) in Merced, CA.

Location	Range	Standard			Surplus		Fraction of Total GHI
		Mean	Deviation	Probability	Energy		
	[-]	[W m ⁻²]	[W m ⁻²]	[%]	[W h m ⁻²]	[W h m ⁻² day ⁻¹]	[%]
Merced	Jan 29 - Jun 19, 2012	104	60	6.07	6,430	45.3	1.2%
San Diego	Jan 29 - Jun 17, 2012	92	51	5.59	5,370	38.4	1.0%
Hawaii	Jan 27 - Jun 17, 2012	101	52	10.71	10,350	72.9	1.3%

Table 3: Statistical results of CEEs at three observatories for the time period when all data from all sites was available (142 days).

	$\sum_i \Delta t_i$ (Up RRs) [hours]	$\sum_i \Delta t_i$ (Down RRs) [hours]	$\sum_i \Delta t_i$ (CEE RRs) [hours]
5%	67.81	66.36	134.2
10%	45.61	44.00	89.60
15%	29.11	29.54	58.65
20%	18.01	18.39	36.40
25%	12.11	11.88	23.98
30%	6.77	6.60	13.37
Year	3,160		

Table 4: Data used in the calculation of $P(RR)$ separated in to both up ramping events and down ramping events.

5% of the time. This intersection occurs at approximately $76 \text{ W m}^{-2} \text{ min}^{-1}$ for the Day Values and an average value of $633 \text{ W m}^{-2} \text{ min}^{-1}$ for the CEE RR distributions. This suggests a significant increase in the probability of inflated RRs associated with CEEs. The inset of Figure 6 shows the PDF of the 10% CEE RR case as well as the PDF for the Day Values. The PDF is included to show the symmetry of the CEE RR distribution. This symmetry indicates that each ramp is associated with a corresponding ramp of similar magnitude and opposite sign. This is to be expected from the passing of a discrete and opaque cloud field. This behavior is also clear from a careful examination of Figure 3 and is summarized in Table 4. Only the 10% PDF case is shown for clarity, however it should be noted that the remaining distributions are quite similar.

4.3. Wavelet Decomposition

The wavelet transforms and periodograms from the clear-sky index for Merced at each time-scale, $j = 1$ to 7 for the entire year of data separated into days with and without CEEs of increasing thresholds were calculated. As mentioned in §3.5, it is important to note that when the top-hat wavelet of time-scale j is applied to a stationary time-series of irradiance measurements, it captures clear periods of length 2^{j-1} surrounded by overcast periods or vice versa. The wavelet transform and periodogram for March 21, 2011 over modes $j = 1$ (60 seconds) to $j = 7$ (about an hour) are shown in Figures 8 and 9 respectively. This day was chosen not only because it was used to illustrate the previous concepts but also because it has transitions

between clear and cloudy periods at several time-scales which would be detected by the top-hat wavelet transform. Upon inspection, it is clear from Figure 8 that the wavelet transforms tend to be zero for times when no variability is present and increase in amplitude as fluctuations at the time-scale in question increase, as is to be expected. This is illustrated with clarity during the time period from approximately 1:00PM to 2:00PM, where only the $j = 7$ mode has a non-zero amplitude while all other modes, i.e. $j = 1 - 6$ are nearly zero. This is a result of the cloudy period that lasts on the order of an hour with very little variability on shorter time-scales. This result is even more evident upon inspection of the periodograms in Figure 9, where the periodogram is a non-negative number that increases in amplitude with the fluctuations at the time-scale in question.

As described in §3.5 the average annual fluctuation power indices are plotted as a function of time-scale (mode) and CEE threshold in Figure 7(a). It is clear that days without CEEs tend to possess fluctuation power indices that are typically 5 to 15 times lower in magnitude, which is to be expected from the increased variability associated with the passing of cloud fields. However, regardless of the time-scale (mode) all of the fluctuation power indices for a particular threshold are maximum at the $j = 6$ time-scale, suggesting that this is the dominant time-scale of cloud-fields/weather-systems that are in turn responsible for CEEs. To clarify, this mode corresponds to a clear period of 15 minutes surrounded by overcast periods or vice versa, which is in agreement with the results from Kassianov et al. (2004), which suggest that the typical decorrelation time for sky-cover is on the order of 15 minutes.

The ratio of the annual average fluctuation power indices of CEE to Non-CEE days are shown in Figure 7(b) as a function of CEE threshold. This is performed in order to examine the impact of CEEs at each time-scale; that is, at which time-scale do the CEEs have the most impact. Unlike the results in Figure 7(a), which show a peak at the $j = 6$ mode associated with approximately 30 minutes, the ratios show a peak at the $j = 3$ mode which is associated with a time-scale of approximately 4 minutes. This suggests that while the clouds that are responsi-

Figure 6: Cumulative Distribution Functions (CDFs) of the coherent Ramp Rates (RRs) whose maximum values exceed the CSM by a increasing threshold and are associated with Cloud Enhancement Events (CEEs). The CDF of the entire year of data that satisfy Equation (4) is also shown for comparison and labeled as 'Day Values'. Intersection of the $P=0.95$ line and the Day Values CDF occurs at $76 W m^{-2} min^{-1}$ and an average value of $633 W m^{-2} min^{-1}$ for the CEE RRs. Inset: Probability Distribution Function (PDF) of the Day Values as well the 10% threshold distribution showing the symmetry of RR associated with the passing of opaque clouds as well as the increased probability of elevated RRs.

ble for creating CEEs tend to introduce variability on the order of 30 minutes, the CEEs themselves tend to operate on time-scales about one eighth as long (~ 4 minutes).

5. Conclusions

This study investigates the observational frequency of CEEs and the associated coherent RRs. A statistical analysis showed that nearly 4% of the observations at Merced qualify as potential CEEs corresponding to nearly 3.5 days of CEEs per year. The increases above the predicted clear-sky ceiling for these CEEs ranged from 10 to 520 W m^{-2} and maximum GHI values on the order of 1,300 W m^{-2} were observed at all three observatories. The maximum CEE was observed in San Diego on the 25th of May, 2012, with a value of nearly 1,400 W m^{-2} , which was 43% higher than the modeled clear-sky ceiling.

Cumulative Distribution Functions (CDFs) show that CEEs are associated with elevated RRs. For days with no CEEs RRs greater than 76 $\text{W m}^{-2} \text{ min}^{-1}$ occur only 5% of the time. On the other hand, for days containing CEEs RRs exceeding 633 $\text{W m}^{-2} \text{ min}^{-1}$ occur 5% of the time. In addition, Probability Distribution Functions (PDFs) were used to illustrate the symmetry of the CEE RR distributions, which suggests that each CEE RR is associated with a ramp of similar magnitude and opposite sign.

Finally, wavelet decomposition coupled with fluctuation power index analysis shed light on the time-scales on which cloud induced variability and CEEs operate. An examination of the magnitude of the fluctuation power indices showed that regardless of the presence of CEEs, cloud induced variability tends to have a maximum fluctuation power index at the 30 min time-scale. However, upon inspection of the ratios of the fluctuation power indices for both CEE and non-CEE at each time-scale showed a maximum increase at the 4 minute time-scale, regardless of CEE threshold. In other words, this result suggest that while clouds tend to induce variability most strongly at the 30 minute time-scale, they have the potential to cause CEEs that induce variability on time-scales of several minutes. This analysis clearly demonstrates that CEEs are an indicator for periods

of high variability and therefore provide useful information for solar forecasting and integration.

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Figure 7: (a) Average annual fluctuation power indices as a function of time-scale and CEE threshold. Days without CEEs tend to possess fluctuation power indices that are typically 5 to 15 times lower in magnitude. Regardless of the time-scale (mode) all of the fluctuation power indices for a particular threshold are maximum at a time-scale of approximately 30 minutes ($j = 7$), suggesting that this is the dominant time-scale of clouds that are in turn responsible for CEEs. (b) Ratios of annual average fluctuation power indices of CEE to non-CEE days as a function of CEE threshold. Unlike (a), which show a peak at the $j = 7$ mode associated with approximately 30 minutes, the ratios show a peak at the $j = 4$ mode which is associated with a time-scale of approximately 4 minutes, suggesting that while the clouds that are responsible for creating CEEs tend to introduce variability on the order 30 minutes, the CEEs themselves tend to operate on time-scales about one eighth as long (~ 4 minutes).

Figure 8: The wavelet transforms from the clear-sky index for Merced at each time-scale, $j = 2 - 8$ for the entire day of March 21, 2011 satisfying Equation (4).

Figure 9: The wavelet periodogram from the clear-sky index for Merced at each time-scale, $j = 2 - 8$ for the entire day of March 21, 2011 satisfying Equation (4).

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