Studies of Premixed and Non-Premixed Hydrogen Flames

Okjoo Park,¹ Peter S. Veloo,² Hugo Burbano,¹ Fokion N. Egolfopoulos¹

¹*Department of Aerospace and Mechanical Engineering
University of Southern California, Los Angeles, CA 90089-1453, USA*

²*Exponent, Failure Analysis Associates, Los Angeles, CA 90066, USA*

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Corresponding Author:

Fokion N. Egolfopoulos

Department of Aerospace and Mechanical Engineering,

University of Southern California

Los Angeles, California 90089-1453, USA

Phone: 213-740-0480

Fax: 213-740-8071

Email: egolfopo@usc.edu

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Okjoo Park^a, Peter S. Veloo^b, Hugo Burbano^a, Fokion N. Egolfopoulos^{a,*}

^a *Department of Aerospace and Mechanical Engineering*

University of Southern California, Los Angeles, CA 90089-1453, USA

^b *Exponent, Failure Analysis Associates, Los Angeles, CA 90066, USA*

ABSTRACT

The hydrogen oxidation chemistry constitutes the foundation of the kinetics of all carbon- and hydrogen-containing fuels. The validation of rate constants of hydrogen-related reactions can be complicated by uncertainties associated with experimental data caused by the high reactivity and diffusivity of hydrogen. In the present investigation accurate experimental data on flame propagation and extinction were determined for premixed and non-premixed hydrogen flames at pressures between $p = 1$ and 7 atm. The experiments were designed to sensitize the three-body $\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$ reaction, whose rate is subject to notable uncertainty. This was achieved by increasing the pressure and by adding to the reactants H_2O and CO_2 whose collision efficiencies are high compared to other species. In the present study, directly measured flame properties were compared against computed ones, in order to eliminate uncertainties associated with extrapolations, as is the case for laminar flame speeds. The measured extinction strain rates exhibit both a positive and negative dependence on pressure with and without weighting with the density, and this non-monotonic behavior is caused by the competition between the $\text{H} + \text{O}_2 \rightarrow \text{O} + \text{OH}$ and $\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$ reactions as well as the HO_2 kinetic pathways as pressure increases. The various kinetic models considered in this investigation did not reproduce equally well the non-premixed flame extinction data with added H_2O . On the other hand, the predicted extinction strain rates were consistent between the various models in the case of added CO_2 . Finally, it was shown that the formulation of binary diffusion coefficient pairs including $\text{H}-\text{N}_2$ and H_2-N_2 has a first order effect on the prediction of extinction strain rates of non-premixed H_2 flames.

Keywords: Flame propagation, flame extinction, pressure effects, kinetic modeling, hydrogen kinetics

1. Introduction

The study and development of kinetic models for the oxidation of hydrogen has historically been motivated by its hierarchical importance in combustion chemistry. Recent interest in utilizing synthesis gas (syngas) as a fuel for Integrated Gasification Combined Cycle (IGCC) will require the validation of existing H_2/CO chemical kinetic reaction models at conditions relevant to those encountered in gas turbines. This will require accurate experimental results at elevated pressures and low flame temperatures (e.g., [1,2]). Adding to challenges in accurately modeling syngas oxidation is the possibility of significant H_2O vapor and CO_2 present in the fuel stream after coal gasification. Nitrogen oxide (NO_x) mitigation strategies for stationary gas turbines include H_2O vapor injected into gas turbine combustors or the utilization of exhaust gas recirculation (e.g., [3-6]).

The development of accurate syngas oxidation chemical kinetic models has been the focus of a number of recent investigations (e.g., [7-12]). The kinetics of H_2 oxidation at elevated pressures was recently studied by Burke et al. [2], and a negative pressure dependence of the mass burning rate was derived for flames of $\text{H}_2/\text{oxidizer}$ and $\text{H}_2/\text{CO}/\text{oxidizer}$ at low flame temperatures and pressures between $p = 1$ and 25 atm. It was shown also that predictions made using the majority of existing models for H_2 oxidation (e.g., [7-11]) fail to predict closely the reported data. Recently, an updated H_2/O_2 kinetic model was developed [12], by incorporating improvements in elementary rate coefficients, in order to provide better predictions of the high-pressure data of Ref. 2. Sheen [13] demonstrated that the inability to predict the data of Ref. 2 stems from the uncertainties inherent in the rate parameters and not from errors in kinetic pathways. Using USC Mech II [8] optimized using the Method of Uncertainty Minimization using Polynomial Chaos Expansion (MUM-PCE) Sheen [13] was able to reproduce the experimental measurements from Burke et al. [2]. In Refs. 2 and 13, the need for additional experimental flame data for H_2 oxidation to better constrain kinetic models is highlighted also.

Laminar flame speed, S_u° , data with accurately quantified uncertainties are also essential in constraining kinetic models. There is a large body of literature S_u° results for H_2/air flames at atmospheric pressure (e.g., [14-20]). The difficulty with utilizing this data is the large spread in these measurements and the little consensus between S_u° values at a fixed equivalence ratio, ϕ . The principal difficulty encountered in experimental measurements of atmospheric pressure H_2/air flames is that, S_u° 's for such mixtures range from the order of cm/s to m/s. At such large flow field velocities, there is large uncertainty in flow velocity measurements using either particle image velocimetry (PIV) or laser Doppler velocimetry (LDV). Another complicating factor is that the extrapolation of the strained flame velocity to zero stretch, to determine S_u° , introduces additional uncertainties depending on the

extrapolation method. Fuel lean H_2/air mixtures have a sub-unity Lewis number (Le) and are thermo-diffusionally unstable, adding thus ambiguity to the so-called measured S_u° 's of fuel lean H_2/air flames that cannot physically exist at the zero stretch limit due to cellular instabilities. Positive stretch suppresses cellular instabilities therefore reducing the dimensionality of the system (e.g., [21,22,23]). Thus, for lean premixed H_2/air flames, extinction strain rates, K_{ext} 's, measured in the counterflow configuration provide a more meaningful experimental validation for kinetic models compared to S_u° 's. Dong et al. [24] measured K_{ext} 's of premixed H_2/air flames and results showed that the sensitivity of K_{ext} to molecular transport could be as large as to kinetics.

The first goal of this present study was to provide experimental S_u° data for H_2 flames with systematically quantified uncertainties. Using a modified O_2/N_2 oxidizer with a larger N_2 dilution ratio relative to air, S_u° 's of $\text{H}_2/\text{O}_2/\text{N}_2$ flames at near stoichiometric conditions were measured accurately by avoiding large flow velocities needed to stabilize H_2/air flames. Both extrapolated S_u° 's and the directly measured reference flame speeds, $S_{u,\text{ref}}$, were used to evaluate a number of recently developed kinetic models for H_2 oxidation. The kinetics of ultra-fuel lean H_2/air were investigated further by the measurement of K_{ext} 's for the same mixtures.

There exists an extensive literature body of work on the extinction of non-premixed H_2 flames of motivated primarily by their relevance to high-speed propulsion applications (e.g., [25-30]). Pellett and coworkers [25-27] determined K_{ext} 's of N_2 diluted, atmospheric pressure, opposed-jet non-premixed H_2 flames.

The effect of pressure on extinction limits of non-premixed H_2 flames has been addressed to a limited extent in available literature (e.g., [28-32]). Papas et al. [28] measured local K_{ext} 's as a function of H_2 dilution between $p = 0.5$ and 1 atm and noted that flame temperatures exhibit a non-monotonic pressure dependence. Recently, Niemann et al. [32] studied the pressure dependence of global extinction limits of non-premixed H_2 flames between $p = 1$ and 15 atm. They confirmed the non-monotonic pressure dependent behavior of computed K_{ext} 's of non-premixed H_2 flames previously observed by Sohn and Chung [30].

The second goal of this study relates to the relative scarcity of H_2 flame data at elevated pressures with systematically quantified uncertainties. Extinction limits of non-premixed H_2 flames at atmospheric and elevated pressures over a wide range of fuel concentrations were measured and modeled.

Syngas combustion in stationary gas turbines at elevated pressures and in the presence of notable quantities of H_2O and CO_2 will readily result in the production of the hydroperoxyl radicals (HO_2). The

main source of HO_2 is via a three-body main termination reaction between H and O_2 . H_2O , and to a lesser extent CO_2 , exhibit large chaperon efficiencies when participating in three-body termination reactions. There is a well-known, large uncertainty (e.g., [12,13]) associated with the rate parameter used to express this three-body reaction in existing H_2 oxidation models. Adding to this uncertainty is the modeling of the associated collisional efficiency of the three body molecules H_2O and CO_2 . Reducing this uncertainty has driven recent studies with wet H_2 flames (e.g., [33-39]).

Seiser and Seshadri [31] studied the influence of H_2O addition on the measured global K_{ext} of premixed and non-premixed H_2 flames at $p = 1$ atm. They highlighted the need for accurate chaperon efficiency of H_2O in three body reactions including $\text{H} + \text{O}_2 \rightarrow \text{HO}_2 + \text{M}$, $\text{H} + \text{OH} + \text{M} \rightarrow \text{H}_2\text{O} + \text{M}$, and $\text{H} + \text{H} + \text{M} \rightarrow \text{H}_2 + \text{M}$. Das et al. [33] investigated the effect of H_2O on S_u^0 of $\text{H}_2/\text{CO}/\text{air}$ mixtures at $p = 1$ atm in the counterflow configuration, and it was recommended that the rate parameters for $\text{H}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{H}$ need to be revisited. Singh et al. [34] studied the effect of H_2O on S_u^0 of syngas/air mixtures using spherically expanding flames. Santner et al. [35] studied the effect of H_2O dilution on the propagation of spherically expanding flames of $\text{H}_2/\text{oxidizer}$ and $\text{H}_2/\text{CO}/\text{oxidizer}$ mixtures at pressures up to $p = 10$ atm., and it was found that the negative pressure dependence of the burning rate shifts to lower pressures with H_2O addition.

The final goal of this study was to perform systematic flame experiments by sensitizing important three-body reactions through H_2O and CO_2 additions and for flame temperatures in the 1000 K to 1400 K range. The present data can be used as targets to constrain kinetic models with emphasis on the main termination reaction involving H_2O or CO_2 , i.e. $\text{H} + \text{O}_2 + (\text{H}_2\text{O} / \text{CO}_2) = \text{HO}_2 + (\text{H}_2\text{O} / \text{CO}_2)$.

2. Experimental approach

The opposed-jet counterflow configuration was used in both the propagation and extinction studies [24, 40-50], and the schematics are shown in Figs. 1 and 2 for atmospheric and high-pressure conditions respectively.

In order to determine S_u^0 , the axial velocity profile along the system centerline is first measured. The minimum point of the axial velocity profile just upstream of the flame is defined as the reference flame speed, $S_{u,ref}$, and the absolute value of the maximum velocity gradient in the hydrodynamic zone is defined as the imposed strain, K [40], as shown in Fig. S1 of the supplementary material. Plotting $S_{u,ref}$ against K , S_u^0 could be determined, in principle, by linearly extrapolating $S_{u,ref}$ to zero imposed strain, i.e., $K = 0$ [40]. In this study the computationally assisted non-linear extrapolation technique to $K = 0$ was utilized [42,43,47].

K_{ext} 's of premixed flames were measured using the single-flame configuration by counterflowing fuel/air mixtures against an ambient temperature N_2 jet. For H_2 /air flames, a flame was established at a near extinction condition and the H_2 flow rate was slightly reduced for fuel-lean mixtures to achieve extinction and determine K_{ext} (e.g., [50]). For mixtures of H_2 /air/ H_2O , a flame was established at a fixed ϕ and a given K , H_2O concentration was slightly increased to achieve extinction and determine K_{ext} .

K_{ext} 's were measured also for non-premixed H_2 flames established by counterflowing an air or air/ H_2O jet against a H_2/N_2 jet. H_2O was added to the oxidizer jet to sensitize more effectively the main termination reaction compared. Extinction was achieved by slightly decreasing the H_2 concentration for dry non-premixed H_2 flames. To achieve extinction for wet non-premixed flames, H_2O concentration was increased until extinction was observed. Table 2 lists the experimental boundary conditions.

For all studies, the diameter of the burner nozzles (D) were, $D = 14$ mm for $K \leq 400$ s⁻¹ and $D = 10$ mm for $K > 400$ s⁻¹ at atmospheric conditions. The burner separation distance, L was equal to D . The experimental boundary conditions are shown in Table 1.

Both PIV and LDV were used to quantify accurately flow velocities. The flow was seeded using micron size silicone oil droplets. Figure 1 depicts the schematic of the experimental configuration for premixed H_2 /air flames at atmospheric pressure conditions that is integrated to a PIV system. Since H_2 flames are invisible to the naked eye, a shadowgraph technique was utilized to observe the flame.

Experiments in which H_2O (ACS de-ionized reagent grade) was introduced into the gas phase required the use of a vaporization system. The vaporization system consists of a syringe pump, nebulizer, and heated vaporization chamber shown in Fig. 2. H_2O mass flow rates were controlled using

high precision syringe pumps; a Harvard Apparatus® PHD 2000 for $p = 1$ atm experiments and a Chemyx® Nexus 6000 syringe pump for elevated pressure experiments.

To assist vaporization, air or N_2 were preheated above the boiling temperature of H_2O was co-flowed into the vaporization chamber. Additionally, the walls of the vaporization chamber were maintained at least 50 K above the boiling temperature of H_2O using a combination of heating tapes, insulation, and thermocouples. The vaporization chamber was connected to the burner using heated and insulated stainless steel tubing. The temperature of the gas was elevated throughout the system to the nozzle exit such that the partial pressure was consistently below the vapor pressure of H_2O at the prevailing ambient temperature and pressure.

Overall, the uncertainty in ϕ or mole fraction was determined to be no larger than 0.5%. The temperature of the fuel streams, measured at the center of the burner nozzle exit, fluctuated within ± 2 °C. The sampling errors in K were determined and their 2σ standard deviations are indicated with uncertainty bars.

3. Numerical approach

S_u^o 's were computed using the PREMIX code [51,52]. Stretched flames in the counterflow configuration were numerically modeled using an opposed-jet code [53]. The original opposed-jet code has been modified to allow for the simulation of asymmetric boundary conditions [54]. Both PREMIX and opposed-jet codes have been modified to account for thermal radiation from CH_4 , CO , CO_2 , and H_2O at the optically thin limit [54,55]. The code is integrated with CHEMKIN [56] and the Sandia Transport [57] subroutine libraries.

K_{ext} is computed by first establishing a vigorously burning flame at a given K . K is then increased by increasing the flow velocities at the burner exits to the point of extinction. At the extinction state, the response of any flame property to K is characterized by a turning-point behavior that introduces a singularity, if K is considered as the independent variable (e.g., [58,59]). The opposed-jet code has been modified to capture this singular behavior, and to allow for a more precise determination of K_{ext} [58]. More specifically, a two-point continuation approach is implemented by imposing a predetermined temperature or species mass fraction at two points in the flow field; thus K becomes the dependent variable.

In order to accurately compute K_{ext} and compare against the data, the experimental values of L (e.g., [54]) and the axial velocity gradient at the nozzle exit, α , (e.g., [43]) are necessary boundary conditions for all simulations. Egolfopoulos [54] numerically demonstrated that K_{ext} increases with nozzle

separation distance as a result of the reduction of the strain rate distribution within the reaction zone. In a recent study by Ji et al. [43], α was also found to have a considerable effect on the numerically determined K_{ext} . The values of α for premixed flames at 1 atm were $15 \pm 10 \text{ s}^{-1}$. For non-premixed flames, the values of α are listed in Table 3.

Full multi-component transport coefficient formulations were used in all simulations for S_u^0 's, $S_{u,\text{ref}}$'s, and K_{ext} 's along with the Soret effect. All simulation results are grid independent and utilized approximately 2000 grid points.

Five kinetic models were used to simulate experimental data, which are summarized in Table 4. The first model is the H_2/CO sub-model of USC Mech II [8]. This model will be referred to as Model I hereafter. Model II is the H_2/CO sub-model of Li et al. [7]. Model III is a recently updated H_2/O_2 model by Burke et al. [12]. Model Ia is the model by Davis et al. [10]. Model Ia is identical to Model I with the exception of the reaction rate parameter for the chain termination reaction, $\text{HO}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{O}_2$. In Model IIa, the transport parameters and formulation of Model II have been replaced by those of Model I.

The diffusion coefficients for Models I, Ia, IIa, and III were implemented in the simulations using updated H and H_2 diffusion coefficients for several key pairs based on a re-evaluated set of Lennard-Jones parameters by Wang and coworkers [24,54]. The elementary reactions common to all models in Table 4 are listed in a consistent manner in Table 5 to facilitate the proceeding analysis and discussion. Rate parameters and references for the elementary reactions listed in Table 4 are tabulated for Models I, II, and III in Tables S1 and S2 of the supplementary material.

4. Results and discussion

4.1 Laminar flame speeds of H_2 /oxidizer mixtures

Figure 3 depicts literature data [14-20,61] and computed S_u° 's of H_2 /air mixtures at $p = 1$ atm and unburned mixture temperature, $T_u = 298$ K. The calculations were performed using Models I, II, and III. Between $0.5 \leq \phi \leq 1.2$ (Fig. 3a) there is reasonably good agreement between all eight sets of experimental data. Within this ϕ range there is less than 30 cm/s difference between maximum and minimum measured S_u° that is within 18% of the mean (or nominal) value. The spread between the various experimental measurements significantly increases at larger ϕ 's as shown in Fig. 3b. For example, at $\phi = 2.6$, there is a 55 cm/s (28 %) spread in the measured S_u° . There is much less spread between the numerical calculations of S_u° in both Figs. 3a and 3b relative to experimental results. The S_u° predictions by Models I and II are nearly identical. For $\phi \leq 1.2$ Model III's predictions are in close agreement with those obtained using Models I and II. At larger ϕ 's, using Model III results consistently in higher S_u° 's. For all three models, ϕ at which S_u° peaks is nearly identical, $\phi \approx 1.75$, which coincides with the experimental observations.

Most of the literature results in Fig. 3 were determined using the spherically expanding flame technique except for the measurements performed by Egolfopoulos and Law [61], which were determined using flames established in the counterflow configuration. It should be noted that it is difficult to perform meaningful comparisons between existing literature results, depicted in Fig. 3, as there is a distinct lack of meaningful quantification of experimental uncertainties for these measurements. Nevertheless, from Figs. 3a and 3b, it can be observed that the present calculations lie well within the range (or scatter) of experimental results.

A new set of experimental measurements of S_u° 's of $H_2/(9.5\%O_2+90.5\%N_2)$ mixtures with carefully quantified experimental uncertainties were determined at $T_u = 298$ K and $p = 1$ atm. The percentage of diluent, N_2 , was determined in order to maintain a maximum $S_{u,ref}$ below 90 cm/s. Reducing $S_{u,ref}$ resulted in a lower propensity for the mixture to flash back and lower Reynolds numbers at the burner exit, thus minimizing flow instabilities and data uncertainty. The S_u° uncertainties in this study were determined by the 2σ standard deviations (95.45% confidence) of $S_{u,ref}$'s based on sampling errors in $S_{u,ref}$, and have been systematically quantified by the authors in Ref. 62.

Figure 4a compares literature results [61,63] and numerical calculations for S_u° 's of $H_2/(7.7\%O_2+92.3\%N_2)$ mixtures at $T_u = 298$ K and $p = 1$ atm. There is closer agreement between the two literature data sets over a wide range of ϕ 's compared to Fig. 3. For $\phi \geq 2.0$, the results from

Egolfopoulos and Law [61] are generally lower than those from Ref. 63. Figure 4b compares the present experimental results and numerical calculations for $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ mixtures.

Comparing model predictions of S_u° 's for flames of the two $\text{H}_2/\text{O}_2/\text{N}_2$ mixtures in Figs. 4a and 4b, reveals that there are now observable differences between predictions made using all three models. Detailed analysis, presented later in this section, demonstrates that this difference is kinetic in nature and stems from the various treatments of the 3rd body collision efficiency of N_2 . From Fig. 4b, it can be seen that for $\phi \leq 2.0$ results obtained using Model III agree best with the present data. At larger ϕ 's, calculations using Model II reproduce best the present data. Overall, with increasing diluent fraction in the oxidizer stream, all three models have a tendency to under-predict the measured S_u° 's.

Sensitivity analysis and computed flame structures highlight the kinetic similarities and differences between H_2/air and diluted $\text{H}_2/\text{O}_2/\text{N}_2$ flames that have a reduced adiabatic flame temperature, T_{ad} .

The logarithmic sensitivity coefficients of S_u° to kinetics for H_2/air (Figs. 5a and 5c) and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ (Figs. 5b and 5d) flames at $\phi = 1.1$ (Figs. 5a and 5b), and $\phi = 1.75$ (Figs. 5c and 5d) are shown in Fig. 5. Comparing the sensitivity coefficients of H_2/air and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames reveals that these two sets of mixtures appear to exhibit similar behavior. There is notable sensitivity to the chain branching (R1, R3, and R5), propagating (R4), and termination (R2, R10) reactions for all three models apparent in Fig. 5. The key difference in the sensitivity analysis results between these two flames is in their sensitivity to the main termination reaction, R2. For the H_2/air flames considered in this analysis, increasing the rate of R2 has a positive effect on reactivity, whereas for $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames, increasing the rate of R2 will have a strongly negative effect on the overall reactivity. To better understand this observation, computed species mole fraction profiles and reaction rates within these flames are analyzed.

Figure 6 depicts the concentrations of the important radicals H, OH, HO_2 , and O (Figs. 6a and 6c) and the reaction rates for R1, R2, and R5 (Figs. 6b and 6d) for H_2/air and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames at $\phi = 1.1$. Figure 6 clearly demonstrates some of the key differences between these two flames caused by increasing diluent ratio in the oxidizer stream. First, the concentration ratios of $\text{HO}_2:\text{H}$, $\text{HO}_2:\text{OH}$, and $\text{HO}_2:\text{O}$ are larger in the $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flame. Second, there is a change in the reaction rate ratio between R1 and R2. For the H_2/air flame, the reaction rate of R1 is greater than R2, whereas the opposite is true for the $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flame. Finally, the reaction rate of R5 is an order of magnitude lower in the $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flame compared to the H_2/air flame. The differences in the characteristics of the radical pools and elementary reaction rates between these two flames factor into the sensitivity of S_u° to R2 observed in Fig. 5. For H_2/air flames, approximately 70% of HO_2 , a

large majority of which is produced via R2, is consumed through R5. For the $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flame the reaction rate of R5 is reduced by an order of magnitude relative to the H_2/air flame greatly reducing the net flux of HO_2 through this pathway that would produce the highly reactive OH. These results and analysis demonstrate some key differences and similarities between the detailed flame structure for H_2/air and $\text{H}_2/\text{oxidizer}$ flames whereby the oxidizer has been diluted relative to air to reduce the overall reactivity of the mixture and make experiments more tractable. An alternative approach to this analysis has been previously presented in Ref. 2. In Ref. 2 analysis was performed by identifying the explosion limit temperature and subsequently comparing the predicted flame structure. This analysis has been performed and is included as supplementary material.

4.2 Experimental results and numerical calculations of stretched H_2/air and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames

There is ongoing debate regarding the value of modeling S_u° vs. modeling non-extrapolated directly measured data. Figures 7a and 7b compare linear vs. non-linear extrapolation methodologies to determine S_u° 's for H_2/air and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames over a range of ϕ 's. Clearly at the conditions depicted in Fig. 7b there is little discrepancy between S_u° 's determined using either extrapolation technique. For the fuel lean mixtures depicted in Fig. 7a, there can be as large as a 10 cm/s difference between linearly extrapolated S_u° 's compared with non-linearly extrapolated S_u° 's. In the present study the $S_{u,\text{ref}}$ vs. K data are directly modeled using the opposed-jet code eliminating uncertainties associated with extrapolations similar to Natarajan et al. [37].

Figures 8a to 8f depict the $S_{u,\text{ref}}$ as a function of strain rate for a subset of the experimental results for H_2/air and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames at $\phi = 0.32, 0.35, 0.45, 1.10, 1.75,$ and 2.40 respectively. For the $\phi < 1$ cases depicted in Figs. 8a, 8b, and 8c, there is a notably large gradient (*i.e.*, large Markstein length) in the $S_{u,\text{ref}}$ vs. K data. For $\phi > 1$, Figs. 8e and 8f show that there is a much weaker dependence of $S_{u,\text{ref}}$ to K relative to the aforementioned fuel lean cases (smaller Markstein lengths). This is to be expected as $\phi > 1$ mixture result in more vigorously burning flames that are less sensitive to stretch than the weaker burning $\phi < 1$ flames. Additionally, as mentioned in the Introduction, for $\phi < 1$ H_2/air mixtures $Le < 1.0$ and thus the overall reactivity increases with (positive) stretch.

Figures 8a to 8f also compare numerical calculations using Models I, II, and III against the present directly measured data. At all ϕ 's considered, the present models reproduce to a very high degree the Markstein lengths in the experimentally determined $S_{u,\text{ref}}$ vs. K data. This is as expected since it has been demonstrated (e.g., [42,47]) that the balance of momentum and heat, upstream of the preheat zone

where $S_{u,ref}$ is determined, should not depend, to the first order, on kinetics or transport of the chemical kinetic model. This agreement also provides confidence in the underlying physical model used in the numerical formulation of the opposed-jet. Results obtained using Model I consistently under-predict the measured $S_{u,ref}$, while for very fuel lean ($\phi = 0.35$) and very fuel rich ($\phi = 2.4$) conditions, Model II provides good agreements with the present data. Between $0.35 < \phi < 2.1$, calculations using Model II under-predict the measured $S_{u,ref}$. Calculations using Model III under-predict the data for the $\phi = 0.32$, 0.35, and 0.45 cases. Model III predicts a much stronger positive effect of increasing ϕ on the reactivity of H_2 /oxidizer mixtures compared with Models I and II. Therefore, computed $S_{u,ref}$'s using Model III under-predict the data for the leanest case (Fig. 8a) and over-predict them for the richest case (Fig. 8f).

4.3 Extinction limits of premixed fuel lean H_2 /air flames

Figure 9 compares the measured and computed K_{ext} 's for premixed H_2 /air flames in the $0.28 \leq \phi \leq 0.35$ range. There is excellent agreement between the experimental and computed results using Model II for all ϕ 's considered. Predicted K_{ext} 's by Models I and III are identical, and 20 to 55 % lower than the predictions by Model II.

The overall trends between experimental and computed K_{ext} 's of premixed H_2 /air flames are identical to the trends observed in Figs. 8a ($\phi = 0.32$) and 8b (at $\phi = 0.35$). That is, Model II reproduces the experimental results, and predictions made using Models I and III are identical but notably under-predict the experimental results. This is a different trend compared to that seen in Fig. 3a. Specifically, for S_u^0 's of H_2 /air flames, Model III exhibits the strongest reactivity, and computed S_u^0 's by Models I and II are identical and lower than Model III. This demonstrates that some of the kinetic pathways are sensitized at extinction differently compared to propagation, since extinction limits probe kinetic regimes for ultra-lean premixed flames for which propagation studies of fundamental value are not feasible due to cellular instabilities.

Figure 10 depicts the logarithmic sensitivity coefficients of K_{ext} to reaction rate coefficients computed using Models I, II, and III for H_2 /air flames at $\phi = 0.28$. There is notable sensitivity to the chain propagation R4, chain termination R2, and chain branching R1 reactions for all three models. Additionally, there is large sensitivity to chain branching reactions R3 and R5. Compared to the sensitivity coefficients of S_u^0 's at $\phi = 1.1$ or 1.75 shown in Fig. 5, K_{ext} 's at $\phi = 0.28$ are not sensitive to R10 and R11, which are chain termination reactions involving H. There is instead increased sensitivity to reactions involving HO_2 , such as HO_2 consumption by O, R7. The key difference between the

kinetics of S_u^0 and K_{ext} is the large negative sensitivity of K_{ext} 's to R2. In Fig. 5a, a small positive sensitivity of S_u^0 's to R2 can be seen, but for extinction phenomena this sensitivity is strongly negative.

In order to understand better the differences observed between the numerical predictions of the three models considered presently, it is important to look closer at the choices of the rate parameters for the elementary reactions. R1 is a relatively well-understood and extensively studied reaction, and therefore it is consistently parameterized in all three models. Most recently, Hong et al. [64] proposed a new rate coefficient for R1 with improved uncertainty bounds and this rate is used in Model III. Although all three models have selected slightly different values for the R1 rate, the resulting net reaction rate is within 7 % for all three models between 1000-1400 K and within 15 % between 1400-2500 K. Thus, discrepancies observed in predictions using these three models are unlikely due to the choice of the rate coefficient for R1.

From the results depicted in Fig. 10, it is clear that for ultra-lean H_2/air flames, the ratio of the rates R2:R1 plays a prominent role in dictating the overall predicted reactivity. Figure 11 depicts the branching ratio of R2 and R1 for Models I, II, and III between $800 < T < 2000$ and at $p = 1$ and 7 atm using (a) N_2 and (b) H_2O as the third body respectively. Note that R1 is effectively independent of pressure due to the HO_2 complex having sufficiently high energy to dissociate into $\text{OH} + \text{O}$ before collision with any third body (e.g., [12]). The branching ratios, R2:R1, for Models I and III are almost identical for $\text{M} = \text{H}_2\text{O}$ and Models II and III have strong agreement in predictions for the case of $\text{M} = \text{N}_2$. Model II has, overall, the lowest ratio of R2:R1, especially for $\text{M} = \text{H}_2\text{O}$, resulting in increased overall reactivity for calculations of fuel lean flames. The reactivity of ultra-lean mixtures predicted by all three models follows closely the trends shown in Fig. 11.

Compared to R1, there exists notable uncertainty in the rate constants of R2. This is especially the case for the 3rd body collisional efficiency of H_2O . Models II and III use the same value for the low pressure limit rate coefficient for R2 proposed by Michael et al [65] but have changed the centering factor and 3rd body efficiency of H_2O [2]. Between Models II and III, the centering factor was changed from 0.8 to 0.5 and the collisional efficiency of H_2O was updated. The collisional efficiency of H_2O relative to N_2 in R2 has been assigned a value of 11.89, 11.0, and 14 for Models I, II, and III respectively. The result of this analysis is that although Model I uses a different rate constant for R2 [10,66] compared to Models II and III, the resulting overall reaction rate for R2 between Models I and III are nearly identical. This explains the similar predictions using Models I and III, as shown in Fig. 9. Models I and III adopt the high pressure limit rate coefficient expression of R2 proposed by Troe [66].

In Model I, the pre-exponential Arrhenius factor has been optimized by a factor of 1.1. In Model II, the high-pressure limit rate constants were taken from Ref. 67.

4.4 Extinction limits of ‘wet’ premixed H_2 /air flames

The results shown in Fig. 12 illustrate the effect of H_2O addition on the extinction of premixed H_2 /air flames. A H_2 /air jet is co-flowed against a N_2 jet with H_2O added to the H_2 /air jet. Experiments in Fig. 12 were performed at $\phi = 0.38$, $p = 1$ atm, and $T_u = 343$ K. The x -axis indicates the mole fraction of H_2O in the H_2 /air/ H_2O mixture. The agreements between the data and numerical predictions are consistent with the results of Fig. 9 for premixed ultra-lean H_2 /air flames. That is, predictions using Model II are in excellent agreement with the data and the computed K_{ext} ’s using Models I and III are consistently lower than the data.

To understand better the effect of H_2O as a third body molecule, the main termination reaction was separated into R2 and R2a,

The logarithmic sensitivity coefficients of K_{ext} of H_2/H_2O /air flames to kinetics computed using Model I, are shown in Fig. 13. At $X_{H_2O} = 0.17$, the K_{ext} sensitivity to R2a is larger compared to R1 suggesting that these data can be used as targets to constrain the uncertainty associated with the collisional efficiency of H_2O . H_2O dissociation, upstream of the flame, is not important under the conditions considered.

4.5 Extinction limits of non-premixed H_2 flames

Figure 14a depicts the experimental and computed K_{ext} ’s as a function of H_2 mole fraction, X_{H_2} , in the H_2/N_2 jet for non-premixed counterflow H_2 flames with unburned fuel stream temperature, $T_{H_2/N_2} = 298$ K, oxidizer stream temperature, $T_{air} = 298$ K, and $p = 1$ atm.

Numerical calculations were performed using Models I, II, and III. For $X_{H_2} < 0.16$, Model II accurately reproduces the data similarly to the premixed flame results shown in Figs. 9 and 12. With increasing X_{H_2} , Model II slightly over-predicts the data. At $X_{H_2} > 0.175$ Models I and III predictions agree well with the experimental results.

Figure 14b depicts the experimental and computed K_{ext} 's for 'wet' non-premixed H_2 flames. The experimental conditions for these flames are $X_{\text{H}_2} = 0.17$, $T_{\text{H}_2/\text{N}_2} = 298 \text{ K}$, $T_{\text{air}/\text{H}_2\text{O}} = 353 \text{ K}$, and $p = 1 \text{ atm}$. As in Figs. 12 and 14a, using Model II provides the best agreements with the data while using Models I and III the data are under-predicted.

4.6 Pressure effects on extinction limits of non-premixed H_2 flames

Figure 15 depicts the experimental and computed K_{ext} 's for non-premixed H_2 flames for $p = 1, 4$, and 7 atm , $T_{\text{H}_2/\text{N}_2} = 298 \text{ K}$, and $T_{\text{air}} = 298 \text{ K}$. Numerical calculations were performed using Models I, Ia, II, and III. As stated earlier, Model Ia is nearly identical to Model I with the exception of the rate constants of R6. Calculated K_{ext} 's using Models I, Ia, and III are identical at $p = 1 \text{ atm}$. For all three conditions namely $p = 1, 4$, and 7 atm , using Model II results in the largest K_{ext} 's. Predicted K_{ext} 's using Model II are in good agreement with the data at $p = 1 \text{ atm}$, as discussed in the previous section, but notably over-predict, by a factor of two, the data at $p = 4$ and 7 atm . It is apparent from these results that Model II is unable to capture the pressure dependence. Additional simulations were performed using Model II with a H_2O collision efficiency of 14.0 (from Model III) with a center-broadening factor of 0.5 [2]. The results predicted that K_{ext} will decrease 5% from the original result at $p = 4 \text{ atm}$, but it is still 38% larger than predictions using Model III and 60% higher than the experimental values. There are minor differences between computed K_{ext} 's using Models I and III at all pressures. There is good agreement between calculations using Models I, Ia, and III and experimental results at $p = 4 \text{ atm}$. At $p = 7 \text{ atm}$, calculations using Models I and III over-predict the data but predictions using Model Ia are in excellent agreement with the data. Clearly, the pressure dependence is best captured by Model Ia relative to the other three models considered.

The only difference between Models I and Ia is in the rate expression of R6, which has been established to increase in importance with pressure (e.g., [68]). The rate constant for R6 in Model Ia is expressed by the combination of two Arrhenius forms [unit: $\text{cm}^3\text{mol}^{-1} \text{ s}^{-1}$]:

$$k_{R6} = (2.375 \times 10^{13}) (T^0) \exp\left(\frac{500}{RT}\right) + (10^{16}) (T^0) \exp\left(-\frac{17330}{RT}\right)$$

T : temperature, K; R : universal gas constant, $\text{cal mol}^{-1}\text{K}^{-1}$.

The first term in the above rate expression is from Keyser [69] with the original pre-exponential factor optimized by a factor of 0.82. This portion of the rate represents the low temperature portion of the rate constant. The second term in the above rate expression of R6 is from Hippler et al. [70] and represents

the intermediate and high temperature regimes. Model I uses a combination of four Arrhenius forms developed by Sivaramakrishnan et al. [68],

$$k_{R6} = 1.41 \times 10^{18} T^{-1.76} \exp\left(-\frac{60}{RT}\right) + 1.12 \times 10^{85} T^{-22.3} \exp\left(-\frac{26900}{RT}\right) \\ + 5.37 \times 10^{70} T^{-16.72} \exp\left(-\frac{32900}{RT}\right) + 2.51 \times 10^{12} T^2 \exp\left(-\frac{40000}{RT}\right) \\ + 10^{136} T^{-40} \exp\left(-\frac{34800}{RT}\right)$$

Models II and III use only the singular rate constant expression developed by Keyser [69]:

$$k_{R6} = 2.89 \times 10^{13} T^0 \exp\left(\frac{497}{RT}\right)$$

Although replacing R6 in Model I with the expression from Model Ia improves the data predictions at elevated pressures, this is not the case for Models II and III. Simply replacing R6 in Models II and III with the rate parameter for R6 from Model Ia does not result in improved predictions. Each elementary reaction in a H₂-O₂ system is tightly coupled with significant sensitivities of global flame phenomena. The challenges associated with the determination of the R6 rate constants stem from the lack of consistent experimental results and its unusual apparent temperature dependence (e.g., [71,72]). To parameterize correctly the non-Arrhenius expression for R6 over a wide range of conditions, additional experimental data are needed.

In Fig. 16, K_{ext} 's are depicted as a function of pressure for a fixed $X_{\text{H}_2} = 0.14$. The pressure range is between $p = 1$ and 7 atm and the calculations were made using Models I, Ia, and III. Calculations using Model II are not shown as its performance in Fig. 15 precludes it. Experimentally, K_{ext} increases with pressure up to $p = 3$ atm. Above $p = 3$ atm, K_{ext} decreases with pressure. For all experimental conditions depicted in Fig. 16 only calculations using Model Ia are in excellent agreement with the data. Models I and III capture the pressure dependence of K_{ext} but over-predict the reactivity above $p = 2$ atm.

A more fundamental approach, however, is considering the variation of the density-weighted extinction strain rate $\rho_u K_{\text{ext}}$ as a function of pressure [73,74,75], where ρ_u is the unburned mixture density. Law [74] and Birkan and Law [75] used a chain mechanism model to demonstrate the importance of the branching-termination coupling in flame modeling and its influence predicting pressure dependence. From the Damköhler number definition, the relevant strain rate was demonstrated to be ρK instead of K [74]. This has also been demonstrated for the pressure dependence of the mass

burning rates of CH₄/air flames (e.g., [76]), H₂/air flames (e.g., [2,77]), and $\rho_u K_{\text{ext}}$'s of non-premixed CH₄ flames (e.g., [73,74]).

Figure 17 depicts $\rho_u K_{\text{ext}}$ as a function of pressure for $X_{\text{H}_2} = 0.14$. From Fig. 17 it can be seen that the negative pressure dependence shifts to $p = 5$ atm. The turning point is still captured by Model Ia and is shifted to higher pressures, i.e. $p = 6$ and 7 atm for Models III and I respectively. The phenomena of the negative effect of pressure on the overall reactivity have been reported and discussed in number of previous studies (e.g., [2,29,30,32,73,76]).

Sohn and Chung [30] and most recently Niemann et al. [32] have discussed the negative pressure dependence of extinction limits of non-premixed H₂ flames; the former study [30] primarily expanded upon the work by Balakrishnan et al. [78]. In Refs. 30 and 32 these phenomena are explained by defining a crossover temperature, T_c , [78]. When the maximum (peak) flame temperature at extinction, $T_{f,\text{max,E}}$, is above T_c the magnitude of the rate for R1 is larger than R2, as a result there will be a positive dependence of K_{ext} on pressure. Conversely, when $T_{f,\text{max,E}}$ is below T_c , R2 has a larger rate compared to R1 and increasing pressure will retard reactivity. In Refs. 30 and 32 it has been shown that K_{ext} first increases and then decreases with pressure. The pressure at the turning point corresponds to the pressure at which $T_c > T_{f,\text{max,E}}$. This phenomenon corresponds to the turning point pressure dependence of $\rho_u K_{\text{ext}}$ and not K_{ext} as shown in Fig. 18. Figure 18 depicts the computed $T_{f,\text{max,E}}$ and T_c as a function of p using Models I, Ia, and III. T_c is identical for Models I and Ia because rate parameters for R1 and R2 are same for both models. For $X_{\text{H}_2} = 0.14$, $T_c > T_{f,\text{max,E}}$ occurs at $p = 5\sim 5.5$ atm for Models I and Ia and $p \approx 4$ atm for Model III. Model Ia has a predicted turning point of $\rho_u K_{\text{ext}}$ at $p = 5$ atm as shown in Fig.17.

To understand better the kinetics involved in the phenomena modeled in Figs. 15-17 the sensitivity of K_{ext} to kinetics for a $X_{\text{H}_2} = 0.14$ non-premixed H₂ flame was computed using Model Ia at various pressure conditions and is depicted in Fig. 19. At $p = 1$ atm the chain branching R1 and R3, and chain propagation R4 reactions involving H, O, and OH dominate the sensitivity spectrum. At $p = 3$ atm, reactions involving HO₂ are increasingly sensitized. Conversely, the sensitivities to R3 and R4 substantially decrease. At $p = 5$ atm, the rate ratio of R2 to R1 has significantly increased compared to $p = 1$ atm.

The primary cause for the pressure dependence of $\rho_u K_{\text{ext}}$ is the competing consumption pathways of H between R1 and R2. The results of Fig. 19 illustrate that reactions involving HO₂ become increasingly rate limiting at elevated pressures. In Fig. 20, H concentration decreases but HO₂ concentration is notably higher relative to H with increasing pressure. Higher HO₂ concentration, as a result, leads to increased flux through R5 and R8 that compete with R1 for the consumption of H. The

chain branching R5 is the dominant HO_2 consumption pathway. OH concentration also decreases with increasing pressure; however R9 plays an increasingly important role in OH generation at elevated pressures. Although R5 is still the dominant pathways for both HO_2 consumption and OH generation at increasing pressures, it gradually decreases in importance in favor of the chain terminating R6, as shown in Figs. 19 and 21. Furthermore, the consumption pathway of O through R9, which competes with R3, notably increases with increasing pressure, which has been previously discussed by Santner et al. [35]. Increased flux through R9 reduces H production and increases the importance of the chain terminating R6.

Figures 21a and 21b compare the mole fractions of H and HO_2 computed using Models I and Ia. Although H concentrations are similar for both models, Model Ia results in less HO_2 compared to Model I at elevated pressures. Differences in R6 result in notable differences in HO_2 radical pools at elevated pressures.

Figures 21c and 21d compare computed reaction rates for reactions involving HO_2 against R1 and R2 in a $X_{\text{H}_2} = 0.14$ non-premixed H_2/N_2 -air flames at near extinction conditions using Models I and Ia. Model I results in a smaller net rate of R6 than Model Ia. Comparing $p = 2$ atm and 6 atm, it can be seen clearly that differences caused by R6 are more profound at elevated pressures. In Model I, HO_2 is consumed to a much larger degree via R5 at 6 atm compared to Model Ia. Sheen [13] concluded that there is a significant coupling between R2, with H_2O as the third body, and R6 that has a strong effect on the ability of H_2/CO models to accurately capture the pressure dependency of the mass-burning rate.

In Fig. 22a predictions using Model Ia are compared against data for $X_{\text{H}_2} = 0.135, 0.140$, and 0.145 . As X_{H_2} decreases, the pressure at which turn over occurs shifts to lower pressures. Model Ia captures closely the experimental results and trends. Figure 22b depicts T_c and $T_{f,\text{max},E}$ as a function of pressure for various X_{H_2} computed by Model Ia. The pressure at which T_c exceeds $T_{f,\text{max},E}$ corresponds to the pressure at the turning point of $\rho_u K_{\text{ext}}$ for various X_{H_2} using Model Ia.

Therefore, accurately capturing the pressure dependent characteristic of extinction limits requires an accurate representation of HO_2 consumption pathways including R6. Sheen [13] discussed the importance of R6 to accurately capture the transition to negative pressure dependence. In addition, Sheen noted that constraining the uncertainty in R6 would have the largest impact in reducing the model uncertainties. Clearly $\rho_u K_{\text{ext}}$ of non-premixed H_2 flames provides good targets to minimize the uncertainty associated with R6.

4.7 Pressure effects on extinction limits of ‘wet’ non-premixed H_2 flames

Figure 23 depicts the experimental and computed K_{ext} ’s for a non-premixed H_2 flames with H_2O added to the oxidizer stream at $X_{H_2} = 0.15$, $p = 4$ atm, $T_{H_2/N_2} = 298$ K, and $T_{\text{air}/H_2O} = 393$ K. The x -axis values correspond to the mole fraction of H_2O in the oxidizer stream. Predictions obtained using Model II show good agreement with current experimental data at $p = 1$ atm but notably over-predict the data at $p = 4$ atm. Predictions using Models I and III slightly under-predict the data at $p = 1$ atm but provide good agreements at $p = 4$ atm. Predictions using Model Ia under-predict the data to a larger degree compared to Models I and III at elevated pressures. Comparing the trends between numerical calculations observed in Fig. 15 with those in Fig. 23 it becomes clear that the same set of kinetics is sensitized in both types of flames.

4.8. CO_2 third body effects on premixed $H_2/CO/O_2$ flames

The goal of these experiments is to sensitize the extinction limits to the main termination reaction involving CO_2 as the third body collisional molecule, i.e.,

The complication in achieving such a system is the large concentration of H_2O . Typically the sensitivity to R2a will overwhelm any sensitivity to R2b. Secondly, performing experiments using air as the oxidizer will result in large sensitivities to the main termination reaction involving N_2 , R2. To overcome these two complications the extinction limits of $H_2/CO/CO_2/O_2$ flames was experimentally determined and compared with numerical calculations. In order to minimize the sensitivity three body reactions involving H_2O , the $H_2:CO$ ratio was adjusted such that chain branching was achieved while simultaneously minimizing H_2O production. By using O_2 as the oxidizer (instead of air), sensitivity to three body reactions involving N_2 was removed. This also allowed for the presence of notably large quantities of CO_2 .

The results are shown in Fig. 24 and the reported mole fraction of CO_2 is that in the $CO/H_2/O_2/CO_2$ mixture. All experiments were performed at $T_u = 298$ K and $p = 1$ atm. The first series of experiments was for $H_2/CO = 0.15$, $\phi = 0.45$, and the mole fraction of CO_2 in the $H_2/CO/O_2/CO_2$ mixture was varied from 0.32 to 0.43 (Fig. 24a). The second series of experiments was for $H_2/CO = 0.05$, $\phi = 0.23$, and the mole fraction of CO_2 in the $H_2/CO/O_2/CO_2$ mixture was varied from 0.07 and 0.35 (Fig. 24b), with $1700 < T_{\text{ad}} < 2500$ K. There is excellent agreement between predictions obtained using Models I and II and the data.

Figure 25 depicts the sensitivity analysis of K_{ext} for to kinetics. For $\text{H}_2/\text{CO}/\text{O}_2/\text{CO}_2$ flames there is notable sensitivity to CO oxidation via R12. Additionally there is notable negative sensitivity to R2b. Although there are slight differences between the rate parameters for these two aforementioned reactions, their net reaction rates are identical.

4.9 Effect of binary diffusion coefficients on extinction limits of non-premixed H_2 flames

Figure 26 compares the experimental and computed K_{ext} 's for two sets of non-premixed H_2 flames using Models II and IIa. Model II uses a different formulation for its transport parameters when compared to Models I and III. Models I and III implement the transport parameters developed by Wang and coworkers [8,24,60]. In the trial model Model IIa the transport parameters of Model II were replaced by those used in Models I and III. Figures 26a and 26b compare computed K_{ext} 's using Model II and Model IIa to the data for selected non-premixed H_2 flames. In both cases, using Model IIa results in lower K_{ext} 's by 10-20% compared to Model II, and which are in closer agreement with the data.

To better understand the results of Fig. 26, Fig. 27 compares the $\text{H}-\text{N}_2$ and H_2-N_2 binary diffusion coefficients, D_{H,N_2} and $D_{\text{H}_2,\text{N}_2}$ respectively, of Model II and IIa at $p = 1$ atm as a function of temperature. Above ~ 1400 K there is a clear difference between both D_{H,N_2} and $D_{\text{H}_2,\text{N}_2}$ used in Model II compared to Model IIa with the diffusivities of both pairs being larger in Model IIa. Figure 28 depicts the logarithmic sensitivity coefficients of K_{ext} to binary diffusion coefficients, D_{ij} , computed using Models II and IIa. The key observation from this figure is the positive sensitivity of the K_{ext} to $D_{\text{H}_2,\text{N}_2}$ and its negative sensitivity to D_{H,N_2} . Increasing $D_{\text{H}_2,\text{N}_2}$ leads to a larger net flux of reactant, H_2 , into the reaction zone therefore increasing reactivity and making the flame more resistant to extinction. Conversely, increasing D_{H,N_2} leads to a net 'loss' of H from the reaction zone making the flame less resistant to extinction [24]. It is important to note that this is not always the case. For example, in Ref. 24 it was observed that in the case of vigorously burning H_2 flames the sensitivity of extinction to D_{H,N_2} is positive.

In summary, in Model II the D_{H,N_2} is lower compared to Model IIa resulting in a larger H radical pool within the reaction zone and thus increased resistance to extinction.

5. Concluding remarks

Although the oxidation of hydrogen has been extensively studied, there exist notable discrepancies between data sets and kinetic model predictions for propagation and extinction of hydrogen flames. Additionally, there remain significant uncertainties in the individual rate expressions in H_2 kinetic models. In the present study a wide range of fundamental flame data for premixed and non-premixed hydrogen flames were with well-quantified uncertainties were determined, and can be used towards constraining the uncertainties of kinetic models.

The first part of this study focused on premixed H_2 /oxidizer flames. It was observed that there exists a large variation in existing literature laminar flame speeds of H_2 /air flames. To better resolve this issue, the laminar flame speeds of N_2 -diluted H_2 flames were measured in the counterflow configuration. The extra inert dilution was implemented in order to reduce the mixture reactivity and increase thus the experimental accuracy. Although these data are useful for model validation, there are differences in the detailed flame structure between N_2 -diluted and H_2 /air flames. Furthermore, in order to alleviate any ambiguities caused by extrapolation methodologies to zero stretch, directly measured reference flame speeds at various strain rates were compared against computed results.

To probe the kinetics of ultra-lean H_2 /air flames that are thermo-diffusionally unstable at the limit of zero stretch, extinction strain rates of premixed H_2 /air flames were investigated. The ratio of rates of the main branching ($H + O_2 \rightarrow H + OH$) to main termination ($H + O_2 + M \rightarrow HO_2 + M$) reactions dictated the ability of the kinetic model to reproduce experimental results. To supplement these results, extinction strain rates of non-premixed H_2 flames were measured at atmospheric and elevated pressures. The computed results did not capture the pressure dependence satisfactorily. While the aforementioned competition between the main branching and termination reactions controls to great extent the extinction behavior, the chain terminating reaction $HO_2 + OH \rightarrow H_2O + O_2$ was determined also to play an important role at elevated pressures.

Experiments were designed also to specifically to sensitize three-body reactions involving H_2O and CO_2 as the third body. Such data are needed to constrain the large uncertainty in three-body termination reactions.

Finally, the importance of accurately formulating and modeling binary diffusion coefficients and their effect on the prediction of flame propagation and specially extinction has been demonstrated through detailed numerical calculations and sensitivity analysis.

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References

- [1] M. Chaos, F.L. Dryer, *Combust. Sci. Tech.* 180 (2008) 1053-1096.
- [2] M. P. Burke, M. Chaos, F.L. Dryer, Y. Ju, *Combust. Flame* 157 (2010) 618-631.
- [3] J.M. Anderlohr, A.P. da Cruz, R. Bounaceur, F. Battin-Leclerc, *Combust. Sci. Tech.* 182 (2010) 39-59.
- [4] S.M. Correa, *Proc. Combust. Inst.* 27 (1998) 1793–1813.
- [5] A. Bhargava, M. Colket, W. Sowa, K. Casleton, D. Maloney, *J. Eng. Gas Turbines Power*, ASME, 122 (2000) 405-411.
- [6] B. de Jager, J.B.W. Kok, G. Skevis, *Proc. Combust. Inst.* 31 (2007) 3123–3130.
- [7] J.Li, Z.Zhao, A. Kazakov, M. Chaos, F.L. Dryer, J.J. Scire Jr., *Int. J. Chem. Kinet.* 39 (2007) 109-136.
- [8] H. Wang, X. You, A.V. Joshi, S. G. Davis, A. Laskin, F. Egolfopoulos, C.K. Law, USC Mech Version II. High Temperature combustion Reaction Model of H₂/CO/C₁-C₄ Compound. http://ignis.usc.edu/USC_Mech_II.htm, May 2007.
- [9] M. O’Connaire, H.J. Curran, J.M. Simmie, W.J. Pitz, C.K. Westbrook, *Int. J. Chem. Kinet.* 36 (2004) 603-622.
- [10] S.C. Davis, A.V. Joshi, H. Wang, F. Egolfopoulos, *Proc. Combust. Inst.* 30 (2005) 1283-1292.
- [11] A.A. Konnov, *Combust. Flame* 152 (2008) 507-528.
- [12] M.P. Burke, M. Chaos, Y. Ju, F.L. Dryer, S.J. Klippenstein, *Int. J. Chem. Kinet.* 44 (2012) 444-474.
- [13] D.A. Sheen, Spectral Optimization and Uncertainty Quantification in Combustion Modeling, Chapter 5, Ph.D. Thesis, University of Southern California, 2011.
- [14] D.R. Dowdy, D.B. Smith, S.C. Taylor, A. Williams, *Proc. Combust. Inst.* 23 (1990) 325-332.
- [15] K.T. Aung, M.I. Hassan, G.M. Faeth, *Combust. Flame* 109 (1997) 1-24.
- [16] S.D. Tse, D.L. Zhu, C.K. Law, *Proc. Combust. Inst.* 28 (2000) 1793-1800.
- [17] N. Lamoureux, N. Djebaili-Chaumeix, C.-E. Paillard, *Exp. Therm. Fluid Sci.* 27 (2003) 385-393.
- [18] Z. Huang, Y. Zhang, K. Zenga, B. Liu, Q. Wang, D. Jiang, *Combust. Flame* 146 (2006) 302-311.
- [19] C. Tang, Z. Huang, C. Jin, J. He, J. Wang, X. Wang, H. Miao, *Int. J. Hydrogen Energ.* (2008), 33, 4906-4914.
- [20] E. Hu, Z. Huang, J. He, C. Jin, J. Zheng, *Int. J. Hydrogen Energ.* 34 (2009) 4876-4888.
- [21] G.I. Sivashinsky, C.K. Law, G. Joulin, G., *Combust. Sci. Tech.* 28 (1982), 155-159.

- [22] J.D. Buckmaster, G.S.S. Ludford, Lectures on Mathematical Combustion, Society for Industrial and Applied Mathematics, p. 62-65, Philadelphia, 1983.
- [23] C. Kaiser, J.-B. Liu, Paul D. Ronney, Paper No. 2000-0576, 38th AIAA Aerospace Sciences Meeting, Reno, NV, January 11-14, 2000.
- [24] Y. Dong, A.T. Holley, M.G. Andac, F.N. Egolfopoulos, S.G. Davis, P. Middha, H.Wang, *Combust. Flame* 142 (2005) 374-387.
- [25] G.L. Pellett, G.B., Northam, L.G., Wilson, AIAA-89-2522, AIAA/ASME/SAE/ASEE 25th Joint Propulsion Conference, Monterey, CA, July 10–12, 1989.
- [26] G.L. Pellett, G.B. Northam, AIAA-92-0877, 30th Aerospace Sciences Meeting and Exhibit, Reno, NV, January 6, 1992.
- [27] G.L. Pellett, K.M. Isaac, W.M. Humphreys, Jr., L.R. Gartrell, W.L. Roberts, C.L. Dancey, G.B. Northam, *Combust. Flame* 112 (1998) 575-592.
- [28] P. Papas, I. Glassman, C.K. Law, *Proc. Combust. Inst.* 25 (1994) 1333–1339.
- [29] G. Balakrishnan, M.D. Smooke, F.A. Williams, *Combust. Flame* 102 (1995) 329-340.
- [30] C.H. Sohn, S.H. Chung, *Combust. Flame* 121 (2000) 288-300.
- [31] R. Seiser, K. Seshadri, *Proc. Combust. Inst.* 30 (2005) 407-414
- [32] U. Niemann, K. Seshadri, F.A. Williams, *Proc. Combust. Inst.* 34 (2013) 881-886.
- [33] A.K. Das, K. Kumar, C.-J. Sung, *Combust. Flame* 158 (2011) 345-353.
- [34] D. Singh, T. Nishiie, S. Tanvir, L. Qiao, *Fuel* 94 (2012) 448-456.
- [35] J. Santner, F.L. Dryer, Y. Ju, *Proc. Combust. Inst.* 34 (2013) 719-726.
- [36] Z.M. Nikolaou, J.Y. Chen, N. Swaminathan, *Combust. Flame* 160 (2013) 56-75.
- [37] J. Natarajan, T. Lieuwen, J. Seitzman, *Combust. Flame* 151 (2007) 104-119.
- [38] V.R. Rishore, M.R. Ravi, A. Ray, *Combust. Flame* 158 (2011) 2149-164.
- [39] C. Prathap, A. Ray, M.R. Ravi, *Combust. Flame* 159 (2012) 482-492.
- [40] C.K. Wu, C.K. Law, *Proc. Combust. Inst.* 20 (1984) 1941-1949.
- [41] J.-Y. Ren, T.Y. Tsotsis, F.N. Egolfopoulos, *Combust. Sci. Tech.* 174 (2002) 181-1205.
- [42] Y.L. Wang, A.T. Holley, C. Ji, F.N. Egolfopoulos, T.T. Tsotsis, H.J. Curran, *Proc. Combust. Inst.* 32 (2009) 1035-1042.
- [43] C. Ji, E. Dames, Y.L. Wang, H. Wang, F.N. Egolfopoulos, *Combust. Flame* 157 (2010) 277-287.
- [44] O. Park, P.S. Veloo, F.N. Egolfopoulos, *Proc. Combust. Inst.* 33 (2011) 887-894.
- [45] C. Ji, F.N. Egolfopoulos, *Proc. Combust. Inst.* 33 (2011) 955-961.
- [46] C. Ji, E. Dames, B. Sirjean, H. Wang, F.N. Egolfopoulos, *Proc. Combust. Inst.* 33 (2011) 971-978.

- [47] P.S. Veloo, F.N. Egolfopoulos, *Combust. Flame* 158 (2011) 501-510.
- [48] C. Ji, E. Dames, H. Wang, F.N. Egolfopoulos, *Combust. Flame* 159 (2012) 1070-1081.
- [49] C. Ji, S.M. Sarathy, P.S. Veloo, C.K. Westbrook, F.N. Egolfopoulos, *Combust. Flame* 159 (2012) 1426-1436.
- [50] A.T. Holley, Y. Dong, M.G. Andac, F.N. Egolfopoulos, *Combust. Flame* 144 (2006) 448-460.
- [51] R.J. Kee, J.F. Grcar, M.D. Smooke, J.A. Miller, A FORTRAN Program for Modeling Steady Laminar One-Dimensional Premixed Flames, Report No. SAND85-8240, Sandia National Laboratories, 1985.
- [52] J.F. Grcar, R.J. Kee, M.D. Smooke, J.A. Miller, *Proc. Comb. Inst.* 21 (1986) 1773-1782.
- [53] R.J. Kee, J.A. Miller, G.H. Evans, G. Dixon-Lewis, *Proc. Combust. Inst.* 22 (1988) 1479-1494.
- [54] F.N. Egolfopoulos, *Proc. Combust. Inst.* 25 (1994) 1375-1381.
- [55] H. Zhang, F.N. Egolfopoulos, *Proc. Combust. Inst.* 28 (2000) 1875-1882.
- [56] R.J. Kee, F.M. Rupley, J.A. Miller, Chemkin-II: A Fortran Chemical Kinetics Package for the Analysis of Gas-Phase Chemical Kinetics, Report No. SAND89-8009, Sandia National Laboratories, 1989.
- [57] R.J. Kee, J. Warnatz, J.A. Miller, A FORTRAN Computer Code Package for the Evaluation of Gas-Phase Viscosities, Conductivities and Diffusion Coefficients, Report No. SAND83-8209, Sandia National Laboratories, 1983.
- [58] F.N. Egolfopoulos, P.E. Dimotakis, *Proc. Combust. Inst.* 27 (1998) 641-648.
- [59] M. Nishioka, C.K. Law, T. Takeno, *Combust. Flame* 104 (1996) 328-342.
- [60] P. Middha, H. Wang, *Combust. Theor. Model.* 9 (2005) 353-363.
- [61] F.N. Egolfopoulos, C.K. Law, *Proc. Combust. Inst.* 23 (1991) 333-340.
- [62] C.Ji, Y.L. Wang, F.N. Egolfopoulos, *J. Propul. Power* 27 (2011) 856-863.
- [63] R.T.E. Hermanns, A.A. Konnov, R.J.M. Bastiaans, L.P.H. de Goey, *Energ. Fuel* 21 (2007) 1977-1981.
- [64] Z. Hong, D.F. Davidson, R.K. Hanson, *Combust. Flame* 158 (2011) 633-644.
- [65] J.V. Michael, M.-C. Su, J.W. Sutherland, J.J. Carroll, A.F. Wagner, *J. Phys. Chem. A* 106 (2002) 5297-5313.
- [66] J. Troe, *Proc. Combust. Inst.* 28 (2000) 1463-1469.
- [67] C.J. Cobos, H. Hippler, J. Troe, *J. Phys. Chem.* 89 (1985) 342-349.
- [68] R. Sivaramakrishnan, A. Comandini, R.S. Tranter, K. Brezinsky, S.G. Davis, and H. Wang, *Proc. Combust. Inst.* 31 (2007) 429-437.

- [69] L.F. Keyser, *J. Phys. Chem.* 92 (1988) 1193-1200.
- [70] H. Hippler, H. Neunaber, J. Troe, *J. Chem. Phys.* 103 (1995) 3510-3516.
- [71] M.P. Burke, S.J. Klippenstein, L.B. Harding, *Proc. Combust. Inst.* 34 (2013) 547-555.
- [72] Z. Hong, K-Y. Lam, R. Sur, S. Wang, D.F. Davidson, R.K. Hanson, *Proc. Combust. Inst.* 34 (2013) 565-571.
- [73] H.K. Chelliah, C.K. Law, T. Ueda, M.D. Smooke, F.A. Williams, *Proc. Combust. Inst.* 23 (1990) 503-511.
- [74] C.K. Law, *Mathematical Modeling in Combustion Science* (J.D. Buckmaster and T. Takeno Eds., p. 47, Springer-Verlag, New York, 1987.
- [75] M.A. Birkan, C.K. Law, *Combust. Flame* 73 (1988) 127-146.
- [76] F.N. Egolfopoulos, C.K. Law, *Combust. Flame* 80 (1990) 7-16.
- [77] F.N. Egolfopoulos, C.K. Law, *Proc. Combust. Inst.* 23 (1990) 333-340.
- [78] G. Balakrishnan, C. Treviño, F. Mauss, *Combust. Flame* 91 (1992) 246-256.

Table and figures

Lower Jet	Upper Jet	P [atm]	T_u [K]	T_{N_2} [K]	D [mm]	L [mm]
H ₂ / (9.5% O ₂ +90.5% N ₂)	N ₂	1	298	298	10	11
H ₂ /air	N ₂	1	298	298	10 ($K_{ext} > 400 \text{ s}^{-1}$)	10
					14 ($K_{ext} \leq 400 \text{ s}^{-1}$)	14
H ₂ /air/H ₂ O	N ₂	1	343	298	10 ($K_{ext} > 400 \text{ s}^{-1}$)	10
					14 ($K_{ext} \leq 400 \text{ s}^{-1}$)	14
H ₂ /CO/O ₂ /CO ₂	N ₂	1	298	298	10 ($K_{ext} > 400 \text{ s}^{-1}$)	10
					20 ($K_{ext} \leq 300 \text{ s}^{-1}$)	20

Table 1. Experimental configuration and conditions (premixed flames).

Lower Jet	Upper Jet	p [atm]	T_{lower} [K]	T_{upper} [K]	D [mm]	L [mm]
Air	H_2/N_2	1	298	298	10	10
		2-7	298	298	7	9
Air/ H_2O	H_2/N_2	1	353	298	10	10
		4	393	298	7	9

Table 2. Experimental configuration and conditions (non-premixed flame).

p [atm]	X_{H_2}	α [s^{-1}]
1 atm	0.135	10 ± 6
	0.140	20 ± 8
	0.145	25 ± 12
4 atm	0.135	30 ± 10
	0.140	50 ± 10
	0.145	65 ± 15
7 atm	0.135	35 ± 10
	0.140	41 ± 10
	0.145	60 ± 15

Table 3. The axial velocity gradient at the burner exit, α , for the extinction experiments.

Model	Reference
I	USC Mech II [8]
Ia	Davis et al. [10]
II	Li et al. [7]
IIa	Li et al. + Model I transport
III	Burke et al. [12]

Table 4. Kinetic models used.

List of reactions	
(R1)	$\text{H} + \text{O}_2 \rightarrow \text{O} + \text{OH}$
(R2)	$\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$
(R2a)	$\text{H} + \text{O}_2 + \text{H}_2\text{O} \rightarrow \text{HO}_2 + \text{H}_2\text{O}$
(R2b)	$\text{H} + \text{O}_2 + \text{CO}_2 \rightarrow \text{HO}_2 + \text{CO}_2$
(R3)	$\text{O} + \text{H}_2 \rightarrow \text{OH} + \text{H}$
(R4)	$\text{H}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{H}$
(R5)	$\text{HO}_2 + \text{H} \rightarrow \text{OH} + \text{OH}$
(R6)	$\text{HO}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{O}_2$
(R7)	$\text{HO}_2 + \text{O} \rightarrow \text{O}_2 + \text{OH}$
(R8)	$\text{HO}_2 + \text{H} \rightarrow \text{H}_2 + \text{O}_2$
(R9)	$\text{O} + \text{H}_2\text{O} \rightarrow \text{OH} + \text{OH}$
(R10)	$\text{H} + \text{OH} + \text{M} \rightarrow \text{H}_2\text{O} + \text{M}$
(R11)	$\text{H} + \text{H} + \text{M} \rightarrow \text{H}_2 + \text{M}$
(R12)	$\text{CO} + \text{OH} \rightarrow \text{CO}_2 + \text{H}$

Table 5. Reaction labels.

Figure 1. Schematic of the atmospheric pressure experimental configuration (single flame configuration).

Figure 2. A schematic of the high-pressure experimental configuration, including the vaporization system.

Figure 3. Comparison of measured and computed S_u° 's for H_2 /air flames at $T_u = 298$ K and $p = 1$ atm. Lines: simulations using Models I (—), II (---), and III (-.-). Symbols: data from Refs. 14(□), 15(▽), 16(△), 17(+), 18(O), 19(◇), 20(●), and 61(◊). All data except Ref. 61(◊, counterflow technique) were determined by spherically expanding flame technique.

Figure 4. Comparison of measured and computed S_u^o 's of (a) $\text{H}_2/(7.7\%\text{O}_2+92.3\%\text{N}_2)$ flames and (b) $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ flames, at $T_u = 298$ K and $p = 1$ atm. Lines: simulations using Models I (—), II (---), and III (-.-). Symbols: data from Refs. 55(□), 57(●), and present experimental results (○).

Figure 5. Logarithmic sensitivity coefficients of S_u^o to kinetics at $\phi = 1.1$ and 1.75 for H₂/air flames and H₂/(9.5%O₂+90.5%N₂) flames at $T_u = 298$ K, and $p = 1$ atm computed using Models I, II, and III.

Figure 6. Computed species mole fraction profiles, reaction rates, and flame temperatures for flames of H_2/air and $\text{H}_2/(9.5\%\text{O}_2+90.5\%\text{N}_2)$ at $\phi = 1.1$, $T_u = 298$ K, and $p = 1$ atm computed using Model III.

Figure 7. Comparison of non-linear and linear extrapolation techniques for the experimental determination of S_u^0 's of H_2/air and $H_2/(9.5\%O_2+90.5\%N_2)$ flames at $T_u = 298$ K and $p = 1$ atm. Lines: extrapolation curves. Symbols: present experimental data.

Figure 8. Experimental and computed reference flame speeds for H_2/air and $H_2/(9.5\%O_2+90.5\%N_2)$ mixtures at $\phi = 0.32, 0.35, 0.45, 1.1, 1.75$, and 2.4 at $T_u = 298$ K and $p = 1$ atm. Lines: simulations using Models I (—), II (---), and III (-.-). Symbols: present experimental data.

Figure 9. Experimental and computed K_{ext} 's of opposed-jet premixed H_2/air flames at $T_u = 298 \text{ K}$ and $p = 1 \text{ atm}$. Lines: simulations using Models I (—), II (---), and III (-.-).

Figure 10. Logarithmic sensitivity coefficients of (a) K_{ext} to kinetics for opposed-jet premixed H_2/air flames at $\phi = 0.28$, $T_u = 298$ K, and $p = 1$ atm computed using Models I, II, and III.

Figure 11. Branching $R2/R1$ ratios, computed using Models I (—), II (---), and III (-.-).

Figure 12. Experimental and computed K_{ext} 's of opposed-jet premixed $\text{H}_2/\text{H}_2\text{O}/\text{air}$ flames at $\phi = 0.38$, $T_u = 343 \text{ K}$, and $p = 1 \text{ atm}$. Lines: simulations using Models I (—), II (---), and III (-.-).

Figure 13. Logarithmic sensitivity coefficients of K_{ext} 's to kinetics for opposed-jet premixed $\text{H}_2/\text{air}/\text{H}_2\text{O}$ flames at $\phi = 0.38$, $T_u = 343$ K, and $p = 1$ atm computed using Model I.

Figure 14. Experimental and computed K_{ext} 's of opposed-jet non-premixed (a) H_2 flames at $T_{\text{air}} = 298 \text{ K}$ and $p = 1 \text{ atm}$, and (b) H_2 flames with H_2O added to air jet at $X_{\text{H}_2} = 0.17$, $T_{\text{air}/\text{H}_2\text{O}} = 353 \text{ K}$, and $p = 1 \text{ atm}$. Lines: simulations using Models I (—), II (---), and III (-.-). Symbols: present experimental data.

Figure 15. Experimental and computed K_{ext} 's of opposed-jet non-premixed H₂ flames at $T_{\text{air}} = 298$ K, and $p = 1, 4$, and 7 atm. Lines: simulations using Models I (—), II (---), III (-.-), and Ia (....). Symbols: present experimental data.

Figure 16. Experimental and computed K_{ext} 's of opposed-jet non-premixed H_2 flames as a function of ambient pressure at $X_{\text{H}_2} = 0.14$ and $T_{\text{air}} = 298$ K. Lines: simulations using Models I (—), Ia (---), and III (-.-). Symbols: present experimental data.

Figure 17. Experimental and computed $\rho_u K_{ext}$'s of opposed-jet non-premixed H_2 flames as a function of ambient pressure at $X_{H_2} = 0.14$ and $T_{air} = 298$ K. Lines: simulations using Models I (—), Ia (---), and III (-.-). Symbols: present experimental data.

Figure 18. Variation of computed peak flame temperature at extinction, $T_{f,max,E}$ and the crossover temperature, T_c as a function of pressure computed with detailed chemistry. Solid lines are T_c 's computed by Models I and Ia (—), and Model III (—). Dashed lines are $T_{f,max,E}$'s; computed by Model I (---), Model Ia (---), and Model III (---).

Figure 19. Logarithmic sensitivity coefficients of K_{ext} to kinetics for opposed-jet non-premixed H_2 flames at $p = 1, 3, 5,$ and 8 atm, $X_{\text{H}_2} = 0.14$, and $T_{\text{air}} = 298$ K computed using Model Ia.

Figure 20. Mole fraction of H, OH, and HO₂ for $X_{\text{H}_2} = 0.14$ at $p = 2$ and 4 atm computed using Model Ia.

Figure 21. Mole fraction of (a) H and (b) HO₂ with various pressures, $X_{H_2} = 0.14$. Net reaction rates of $H + O_2 \rightarrow OH + O$ (R1), $H + O_2 + M \rightarrow HO_2 + M$ (R2), $HO_2 + H \rightarrow OH + OH$ (R5), $HO_2 + OH \rightarrow H_2O + O_2$ (R6), and $HO_2 + H \rightarrow H_2 + O_2$ (R8) for non-premixed H₂/N₂-air flames at $X_{H_2} = 0.14$ for (c) $p = 2$ atm and (d) $p = 6$ atm computed using model I (solid line) and Ia (dashed line).

Figure 22. (a) Experimental and computed $\rho_u K_{\text{ext}}$'s of opposed-jet non-premixed H₂ flames (b) Computed $T_{f,\text{max},E}$ and T_c as a function of ambient pressure at and $T_{\text{air}} = 298$ K. $X_{\text{H}_2} = 0.135$ (— · — · —, Δ), 0.140 (— · — · —, $\circ$), and 0.145 (—, $\square$). Lines: simulations using Model Ia. Symbols: present experimental data.

Figure 23. Experimental and computed K_{ext} 's of opposed-jet non-premixed H_2 flames with H_2O added to the oxidizer jet at (a) $T_{\text{air}/\text{H}_2\text{O}} = 353 \text{ K}$, $p = 1 \text{ atm}$, and $X_{\text{H}_2} = 0.17$ and (b) $T_{\text{air}/\text{H}_2\text{O}} = 393 \text{ K}$, $p = 4 \text{ atm}$, and $X_{\text{H}_2} = 0.15$. Numerical simulations by Models I (—), II (---), III (-.-), and Ia (....). Symbols: present experimental data.

Figure 24. Experimental and computed K_{ext} 's of opposed-jet premixed $CO/H_2/CO_2/O_2$ flames at (a) $\phi = 0.45$, $H_2/CO = 0.15$ (b) $\phi = 0.23$, $H_2/CO = 0.05$. $T_u = 298$ K, and $p = 1$ atm. Lines: simulations using Models I (—) and II (---). Symbols: present experimental data.

Figure 25. Logarithmic sensitivity coefficients of K_{ext} with respect to kinetics for $\text{H}_2/\text{CO}/\text{CO}_2/\text{O}_2$ flames with $\text{CO}/\text{H}_2 = 0.05$ at $\phi = 0.23$, $T_u = 298$ K, and $p = 1$ atm computed using Model I.

Figure 26. Experimental and computed K_{ext} 's of non-premixed H_2/N_2 -Air flames at T_{air} and $T_{\text{N}_2/\text{H}_2} = 298$ K and $p = 1, 4$, and 7 atm. Lines: simulations using Models II (—) and IIa (····). Symbols: present experimental data.

Figure 27. Binary diffusion coefficients of pairs (H, N₂) and (H₂, N₂) as a function of temperature computed using Models IIa (—) and II (---) at $p = 1$ atm.

Figure 28. Logarithmic sensitivity coefficients of K_{ext} to binary diffusion coefficients for opposed-jet non-premixed H₂ flames at $X_{H_2} = 0.145$, $T_{air} = 298$ K, and $p = 1$ atm computed using Models II and IIa.